



Spectral correction factors for the removal of glint perturbations in above-water radiometry

Barbara Bulgarelli¹, Davide D'Alimonte², Giuseppe Zibordi^{3,4}, Tamito Kajiyama²

¹European Commission, Joint Research Centre, Ispra, Italy

5 ²Aequora, Lisbon, Portugal

³National Aeronautics and Space Administration, Goddard Space Flight Center, Greenbelt, MD, USA

⁴Southeastern Universities Research Association, Washington, DC 20005, USA

Correspondence to: Barbara Bulgarelli (barbara.bulgarelli@ec.europa.eu)

Abstract. Spectral correction factors for the removal of glint perturbations in above-water radiometric measurements are theoretically computed for representative inland, coastal and open-ocean waters, accounting for spectral and atmospheric dependences. The simulation framework relies on the measurement protocol adopted by AERONET-OC and endorsed by the ocean color community to support the validation of satellite aquatic radiometric products. The theoretical computation of the correction factors, here termed *glint correction factors* or *p-factors*, is performed in the 340–1020 nm spectral range by coupling *i.* a highly accurate plane-parallel scalar code to simulate the angular distribution of the spectral sky-radiance impinging at the water surface, with *ii.* a three-dimensional Monte Carlo code to model radiance reflections at a wind-roughened water surface. The impact of glint due to sky-radiance originating from the sun region (conventionally termed *sun-glint*) is separately discussed. Computed glint correction factors—for both the total sky radiance and its sole diffuse component—are available at Zenodo (<https://doi.org/10.5281/zenodo.20609990>).

1 Introduction

The primary data product of aquatic optical remote sensing is the light emerging from the water, the so-called water-leaving radiance L_w . This carries information on the water optically significant components, such as the concentration of pigmented particles, which is a proxy for phytoplankton biomass.

While L_w only accounts for a small fraction of the total signal at the sensor, it must be determined with high accuracy to meet the requirements for environmental and climate applications. Pivotal to the fulfillment of these accuracy requirements is the validation of satellite data products through comparison with in situ reference measurements.

Among the different methodologies established to acquire accurate in situ measurements of L_w , above-water radiometry relies on optical instruments deployed from ships or fixed platforms (Zibordi and Voss, 2014), and more recently from unmanned aerial vehicles (Sciuto et al., 2026).

Radiometric measurements performed from above the water are perturbed by the sky radiance reflected by the water surface (the *glint*), conventionally distinguished into glint from radiance originating in the sun region (*sun-glint*) and glint from radiance originating in the remaining portion of the sky-dome (*sky-glint*). These perturbations must be removed to accurately determine the target signal L_w .

The protocols commonly applied to determine L_w from above-water measurements require acquisitions of the total radiance from the water L_T in direction θ and ϕ , and of the sky radiance L_i in the direction specular to L_T (i.e., in direction $\theta' = 180^\circ - \theta$ and ϕ). The angle of observation θ is measured with respect to nadir, while the azimuth ϕ is the angle between the solar and the measurement plane (see Fig. 1a). Recommendations for ϕ and θ minimizing glint perturbations are provided in Mobley (1999) and IOCCG (2019).

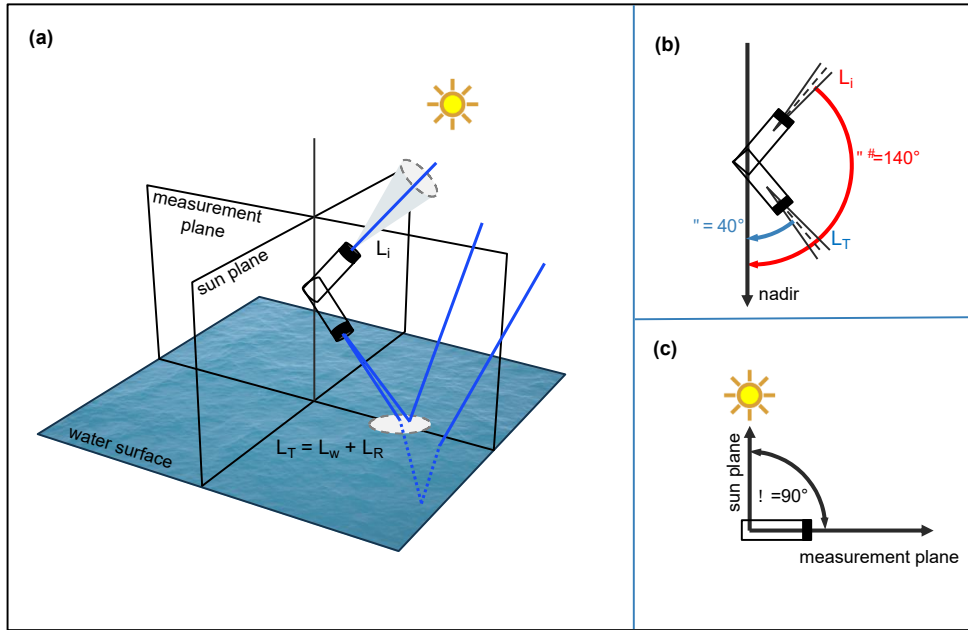


Figure 1: (a) Typical above-water measurement geometry. (b) Side- and (c) top-view measurement geometry applied to AERONET-OC measurements and supported by current measurement protocols.

- 50 The water-leaving radiance L_W at wavelength λ is derived by removing from L_T the radiance L_R reflected by the water surface, which is assumed proportional to L_i :

$$L_W(\theta, \phi, \lambda) = L_T(\theta, \phi, \lambda) - L_R(\theta, \phi, \lambda) = L_T(\theta, \phi, \lambda) - \rho(\theta, \phi, \lambda) \cdot L_i(\theta', \phi, \lambda), \quad (1)$$

- 55 The proportionality factor ρ (here termed the *glint correction factor*) in addition to wavelength and viewing geometry, depends on the sun zenith angle θ_0 , the wind speed v_w and the atmospheric optical properties expressed by the aerosol type and the aerosol optical depth τ_a , which were omitted in Eq. (1) for simplicity. It is highlighted that for a flat water surface, ρ would reduce to the Fresnel reflectance, and L_R would be entirely determined by the specular reflection of L_i . For a wind-roughened water surface, each surface facet still obeys Fresnel's law, but the wind-driven distribution of facet slopes causes L_R to originate from a broader region of the sky-dome around the specular direction (θ', ϕ) . The glint correction factor ρ thus generalizes the Fresnel reflectance by accounting for the roughness of the water surface and for the angular distribution of sky radiance, and is theoretically computed according to:

$$\rho(\theta, \phi, \lambda) = \frac{\int_0^{2\pi} \int_0^{\pi/2} L_{sky}(\theta^*, \phi^*, \lambda) \cdot r(\theta^*, \phi^* \rightarrow \theta, \phi; \lambda; v_w) \sin \theta^* d\theta^* d\phi^*}{L_{sky}(\theta', \phi, \lambda)}. \quad (2)$$

- The numerator in Eq. (2) theoretically represents the radiance $L_R(\theta, \phi, \lambda)$ reflected by the water surface in direction (θ, ϕ) , and $r(\theta^*, \phi^* \rightarrow \theta, \phi; \lambda; v_w) \sin \theta^*$ indicates the probability density that the sky radiance L_{sky} impinging from direction (θ^*, ϕ^*) on a water surface roughened by wind speed v_w is reflected in the direction (θ, ϕ) . Term L_{sky} includes both the direct and diffuse components, and the integration is performed over the whole sky-dome. The denominator is the theoretical quantification of $L_i(\theta', \phi, \lambda)$.

- In the following, ρ -factors accounting for both direct and diffuse (i.e., total) L_{sky} will be denoted by ρ_T , while ρ -factors accounting for the sole diffuse sky-radiance will be denoted by ρ_d .



Terms L_{sky} , r , ρ_d and ρ_T are theoretically computed via radiative transfer simulations.

- Glint correction factors (alternatively called *sea-surface reflectance factors* or *surface-to-sky radiance ratios*) regularly utilized by the scientific community in the processing of above-water radiometric data were computed by Mobley (1999) using the scalar Hydrolight code (Mobley, 1994) accounting for both direct and diffuse sky-radiance contributions. The sky radiance was simulated at $\lambda = 550$ nm according to Harrison and Coombes (1988) and assuming a fixed aerosol optical depth $\tau_a^{550} = 0.26$ (D'Alimonte et al., 2021). The wave-slope distribution was modeled according to Cox and Munk (1954), neglecting the constant background term. The same author subsequently provided vectorial simulations of ρ_T at the same wavelength (Mobley, 2015) by assuming a pure molecular atmosphere and by modelling the wave-slope distribution according to Elfouhaily et al. (1997). An experimental evaluation of the impact on above-water data products of these two sets of ρ_T values, restricted to θ_0 larger than 20° and to wind v_w generally lower than 5 m s^{-1} , indicated slightly better performance of the scalar factors accounting for aerosols and multiple scattering than the vectorial ones computed under a pure molecular atmosphere (Zibordi, 2016).
- Acknowledging experimental evidence of the spectral dependency of ρ (Lee et al., 2010), alternative ρ -factors were proposed. Zhang et al. (2017) applied a Monte Carlo simulation framework with spectrally explicit sky-radiance distributions, separating sky-glint from sun-glint contributions. The study showed that the spectral dependence of ρ_T shifts from a slight decrease with wavelength at low wind speeds to a marked increase with wavelength at higher wind speeds and lower solar zenith angles. This behavior is primarily driven by the spectral distribution of skylight, with a minor contribution from the spectral dependence of the water refractive index. Simulations were performed over the 350–1000 nm range adopting a MODerate resolution atmospheric TRANsmission (MODTRAN; Berk et al., 2006) atmosphere with maritime aerosol and $\tau_a^{550} = 0, 0.05$ and 0.1 . A vector radiative transfer model was additionally applied to perform an exploratory investigation of the impact of polarization, suggesting a moderate increase of sky-glint in the blue.
- Gilerson et al. (2018) applied a one-dimensional vector radiative transfer code to simulate ρ_T factors in the 400–900 nm spectral range for oceanic and partially continental aerosols with τ_a^{440} ranging from 0 to 1.0, demonstrating a significant impact of aerosol optical depth and type on the spectral values of ρ_T . Harmel (2023) applied the vectorial plane-parallel Ordres Successifs Océan Atmosphère Avancé code (OSOAA; Chami et al., 2015) to compute ρ_d factors between 350 and 1000 nm for OPAC (Optical Properties of Aerosols and Clouds; Hess et al., 1998) pure maritime, continental, desert dust and urban polluted aerosols, with τ_a^{550} from 0 to 1.5.
- The authors of the present work proposed scalar ρ_T factors (D'Alimonte et al., 2021; Bulgarelli et al., 2022; Bulgarelli et al., 2024) accounting for spectral and atmospheric dependences obtained by coupling the scalar plane-parallel Finite Element Method radiative transfer code (FEM; Bulgarelli et al., 1999; Kisselev et al., 1995) with the three-dimensional Monte Carlo for Ocean Color Simulation code (MOX; D'Alimonte et al., 2010, 2021; Kajiyama et al., 2016). This development, which specifically refers to the measurement protocol applied by the Ocean Color component of the Aerosol Robotic Network (AERONET-OC; Zibordi et al., 2009; Zibordi et al., 2021), adopted pure and mixed continental and maritime aerosols from the OPAC database with τ_a^{500} ranging between 0 and 0.5.
- Utilizing the same simulation framework, companion ρ_d factors were computed to support investigations into the impact of alternative processing solutions on AERONET-OC data (Zibordi et al., 2025), but were never formally published. The investigation indicated a slightly better agreement with independent field reference measurements when scalar ρ_d from FEM-MOX are applied with respect to ρ_d accounting for polarization effects (Harmel, 2023). This supports the publication of FEM-MOX scalar ρ_d factors and their operational use for AERONET-OC data processing, which implements a quality-control procedure to remove measurements affected by appreciable sun-glint contamination.

Building on previous investigations on ρ_T (Bulgarelli et al., 2024), the present study advances in several directions. First, the atmospheric model is updated to provide a more realistic representation of



130 atmospheric aerosol and gas molecules. Second, values of $\rho_D = \rho_T - \rho_d$ are used to investigate sun-
 glint contamination under diverse measurement conditions. Third, and most importantly, the ρ_d factors
 are formally presented and discussed for the first time, together with updated ρ_T values.

135 Values of ρ_T and ρ_d simulated for typical observation conditions in inland, coastal and open-ocean
 regions and for the specific AERONET-OC measurement geometry (namely $\theta = 40^\circ$ and $\phi = 90^\circ$,
 as in Fig. 1b and c) are made available at Zenodo.

The methodology applied is described in Sect. 2, while results are illustrated and discussed in Sect. 3. A
 detailed description of the dataset comprising the ρ_T and ρ_d factors is given in Sect. 4. In Sect. 5
 140 conclusions are drawn.

2 Methodology

2.1 The simulation framework

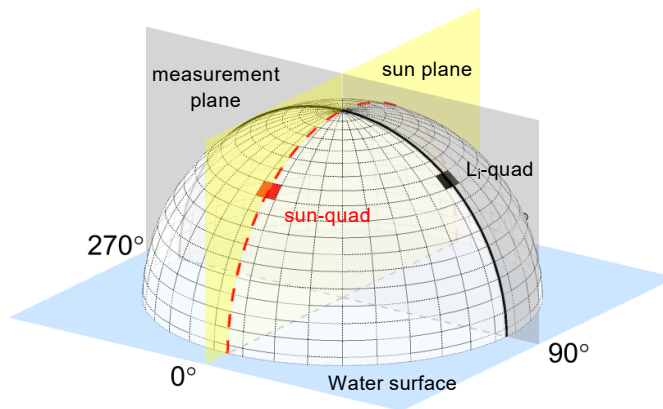
For computational purposes, the sky-dome is divided into a discrete number of quads of dimension
 $\Delta\theta_k \times \Delta\phi_m$ (for $k = 1, \dots, N_\theta = 19$ and $m = 1, \dots, N_\phi = 36$), so that Eq. (2) can be rewritten as:

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$$\rho = \frac{\sum_k^{N_\theta} \sum_m^{N_\phi} \mathcal{R}(k, m) \cdot \mathcal{L}(k, m)}{\mathcal{L}(k_i, m_i)}. \quad (3)$$

In Eq. (3), $\mathcal{R}$ indicates the *water-surface reflectance matrix*, with $\mathcal{R}(k, m) = r(\theta_k, \phi_m \rightarrow$
 $\theta, \phi; \lambda; v_W) \sin\theta_k \Delta\theta_k \Delta\phi_m$; $\mathcal{L}$ the *sky-radiance matrix*, where $\mathcal{L}(k, m)$ corresponds to values of L_{sky}
 150 computed at the barycenter of the (k, m) -quad and rescaled to preserve diffuse and direct irradiances;
 and $\mathcal{L}(k_i, m_i)$ corresponds to the value of $\mathcal{L}$ at the quad encompassing $L_i(\theta', \phi, \lambda)$, hereafter referred to
 as the L_i -quad (see Fig. 2).

Term $\mathcal{L}$ is calculated with FEM in its SkyFEM configuration, while term $\mathcal{R}$ is computed with MOX.



155 **Figure 2:** Partitioning of the sky-dome into quads. The black thick solid and red dashed lines indicate the measurement and the solar planes, respectively. The black L_i -quad encompasses the direction of L_i (which is specular to the down-looking direction of the virtual radiometer). The red sun -quad encompasses the sun position (θ_0, ϕ_0) , while the solar plane is identified by ϕ_0 and $180^\circ + \phi_0$; for convenience ϕ_0 is set to 0° .

160 FEM is a radiative transfer code (Bulgarelli et al., 1999; Kisselev et al., 1995) designed to simulate the
 propagation of unpolarized monochromatic radiation at ultraviolet, visible, and near-infrared
 wavelengths in a vertically inhomogeneous medium with one change in the refractive index (e.g., the
 atmosphere-water system). Comprehensively tested and benchmarked with various codes (Bulgarelli et



al., 1999, 2003; Bulgarelli and Doyle, 2004), FEM applies the finite-element deterministic approach to
 165 solve the radiative transfer equation, fully accounting for multiple scattering, and reflection and
 refraction at the water surface. In its SkyFEM configuration, FEM is coupled with the PERSEA
 (Propagating Environment for Radiance Simulations in atmosphEre and wAter) code, allowing the
 generation of sky-radiance angular distributions for different atmospheric models, relying on existing
 parameterizations, external databases, or user-provided inputs (Bulgarelli, 2024).
 170
 MOX is a three-dimensional stochastic code developed to support investigations on in situ ocean color
 measurements (D’Alimonte et al., 2010; Kajiyama et al., 2016). The code can perform both forward and
 backward ray tracing. In the first case, equivalent to physical measurement conditions, rays are traced
 from the source in the sky-dome to the virtual radiometer. In the latter case (adopted in the present
 175 study), rays are traced from the virtual radiometer back to the source. MOX fully accounts for the field-
 of-view of the radiometer and for multiple reflections at the water surface. The latter is defined over a
 square domain of side $L = 50\text{ m}$ discretised in approximately 1000 intervals along the x - and y -axis.
 Each surface element is further split into two triangular elements whose vertices are elevated based on
 the adopted water-surface model (see Sect. 2.1.1). The reader is referred to D’Alimonte et al. (2021) for
 180 further details.

2.1.1 Atmosphere and water surface modelling

Modelling is performed by assuming clear-sky conditions, using the spectral extra-terrestrial solar
 irradiance from Thuillier et al. (2003), and dividing the atmosphere into 32 plane-parallel layers to
 resolve the vertical distribution of aerosols and gas molecules.
 185 The spectral properties and the vertical distribution of gas molecules are taken from the Air Force
 Geophysics Laboratory (AFGL) model (Anderson et al., 1986). The optical properties and vertical
 distribution of aerosols are taken from the Optical Properties of Aerosol and Clouds (OPAC) software
 package (Hess et al., 1998), which models distinctive aerosol mixtures through the combination of ten
 individual components (e.g., soot, sea-salt, mineral, water-soluble,...) at different relative humidity
 190 (RH), and which assumes three distinct aerosol layers — tropospheric, free-tropospheric and
 stratospheric. The optical properties of each aerosol mixture are theoretically calculated from the size
 distribution and the spectral refractive index of its reference optical components by applying the Mie
 theory under the assumption of spherical particles. Selected OPAC aerosol output parameters are the
 extinction coefficient, the single scattering albedo, the phase function asymmetry parameter, and the
 195 phase function at 112 scattering angles. The Ångström exponent (Ångström, 1961) $\alpha_{350-500}$, for the
 350–500 nm range, and $\alpha_{500-800}$, for the 500–800 nm range, are also utilized.
 Each aerosol phase function derived from the OPAC database is modeled using 1000 Legendre
 polynomials without applying any truncation. Relative differences between original phase function
 values and those obtained through Legendre expansion never exceed $\pm 11\%$ with a standard deviation
 200 of $1.5 \pm 1.8\%$ across all models and all angles. Absolute percent differences in the integral between
 original and reconstructed phase functions never exceed 0.9 %.

Atmospheric modeling updates with respect to Bulgarelli et al. (2024) include the use of the AFGL
 205 model for the gas molecule properties and the inclusion of the free-tropospheric and stratospheric
 aerosol layers.

The water surface model accounts for the spectral dependence of the refractive index, and adopts the
 slope distribution of surface waves from Cox and Munk (1954) expressed as a Gaussian function with
 variance σ^2 :

$$\sigma^2 = 0.003 + 0.00512 \cdot v_w. \quad (4)$$

where v_w is the wind speed in units of m s^{-1} and 0.003 is referred to as *the background term*.



215 2.2 Simulation cases and parameter space

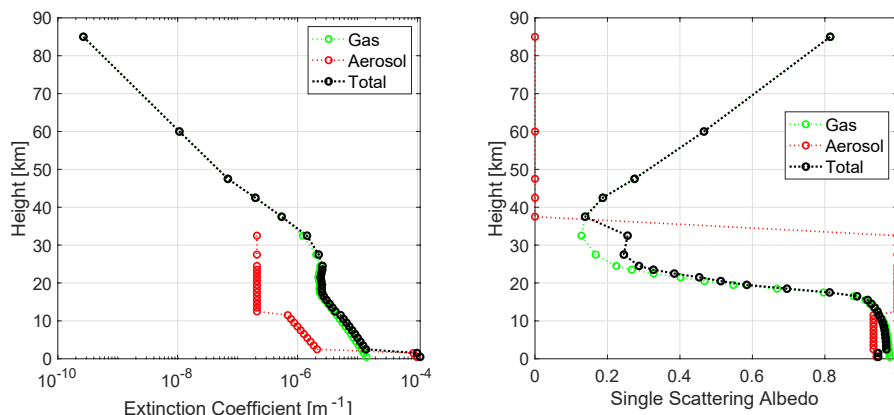
Representative cases were selected to cover typical measurement conditions in inland, coastal and open-ocean regions (Table 1). These include the nominal center-wavelengths of relevance for AERONET-OC measurements; sun zenith angle θ_0 ranging between 10° and 80° ; sun azimuth angle ϕ_0 set to 0° (consistent with above-water radiometric measurements at $\pm 90^\circ$ with respect to ϕ_0 , as defined by community protocols); omnidirectional wind speed v_w varying between 0 and 10 m s^{-1} in the absence of whitecaps or surface scum; total aerosol optical depth at 560 nm, τ_a^{560} , in the 0.05–0.5 range; and three distinct OPAC tropospheric aerosol mixtures at RH = 80 % (Hess et al., 1998):

- Clean maritime aerosol (MA),
- A mix of 80 % average continental and 20 % clean maritime aerosols (MX),
- Polluted continental aerosol (CO).

Table 1 Values of the main parameters adopted for the computation of the ρ -factors; g_{500} represents the phase function asymmetry parameter at 500 nm.

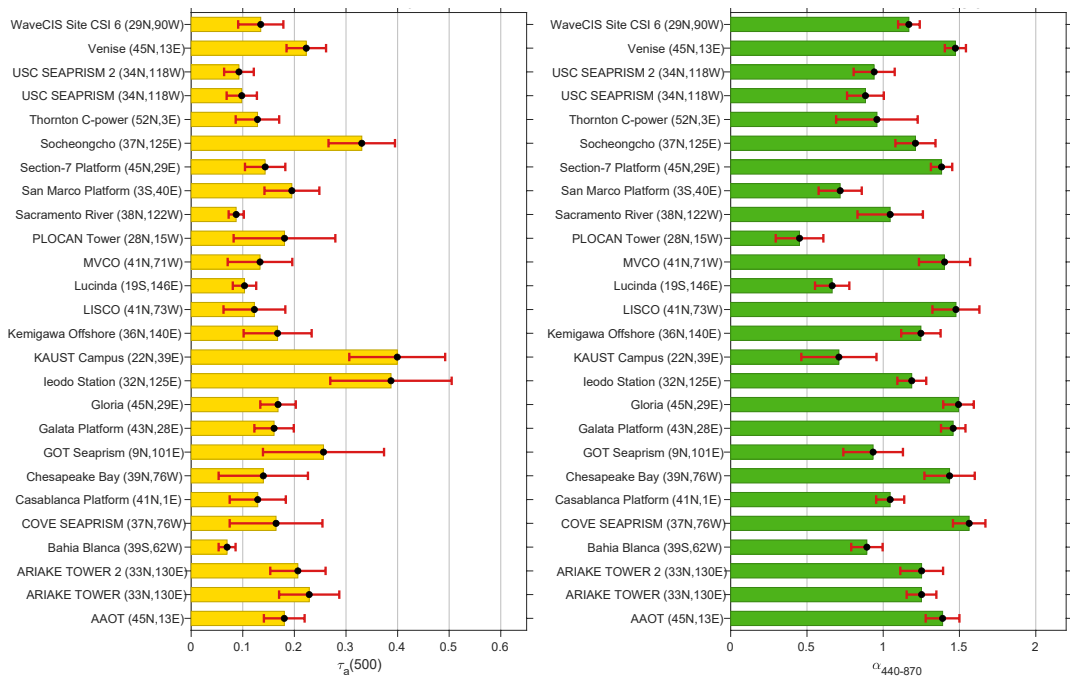
Center-wavelength λ [nm]	340, 380, 400, 412, 440, 443, 490, 500, 510, 531, 532, 551, 560, 620, 667, 675, 681, 709, 779, 865, 870, 1020
Sun zenith θ_0 [deg]	10, 20, 30, 40, 50, 60, 70, 80
Sun azimuth ϕ_0 [deg]	0
Wind speed v_w [m s^{-1}]	From 0 to 10 with a step of 2
Aerosol optical depth at 560 nm, τ_a^{560}	0.05, 0.1, 0.2, 0.3, 0.4, 0.5
Tropospheric aerosol model (RH = 80 %)	Maritime (MA): $\alpha_{350-500} = 0.12$; $\alpha_{500-800} = 0.08$; $g_{500} = 0.77$ Mixed (MX): $\alpha_{350-500} = 0.93$; $\alpha_{500-800} = 1.06$; $g_{500} = 0.72$ Continental (CO): $\alpha_{350-500} = 1.13$; $\alpha_{500-800} = 1.45$; $g_{500} = 0.70$

The adoption of MA, MX and CO tropospheric aerosols yields a columnar Ångström exponent in the 440–870 nm interval $\alpha_{440-870}^{col} = -\log\left(\frac{\tau_a^{440}}{\tau_a^{870}}\right) / \log\left(\frac{440}{870}\right) = 0.19, 1.08, 1.42$ for $\tau_a^{560} = 0.2$, respectively, where τ_a^λ represents the columnar aerosol optical depth at λ . These values characterize a range of cases, spanning from open ocean to inland water environments, with the mixed model (MX) representative of coastal sites where marine and continental aerosol contributions are both significant. Examples of the vertical profiles of the atmospheric inherent optical properties are shown in Fig. 3.



240 **Figure 3:** Vertical profile at 560 nm of extinction coefficient and single scattering albedo for gas molecules, aerosols, and the whole atmosphere when adopting the MX tropospheric aerosol model.

The selected atmospheric parameters were confirmed via comparison with *i)* maritime aerosol occurrences registered in the open ocean (see Smirnov et al. (2009) and dedicated AERONET Maritime
 245 Aerosol Network (MAN) web page) and *ii)* field data from AERONET-OC sites (Zibordi et al., 2009) assumed representative of atmospheric optical conditions in inland and coastal regions.
 Multi-annual yearly averages of τ_a^{500} and $\alpha_{440-870}$ for representative AERONET-OC sites, as extracted from AERONET climatological Level 2.0 data (Holben et al., 1998), are displayed in Fig. 4. The average values with standard deviation across all the considered sites are $\tau_a^{500} = 0.18 \pm 0.09$, and
 250 $\alpha_{440-870}^{col} = 1.14 \pm 0.30$.



255 **Figure 4:** AERONET climatological aerosol optical data at reference AERONET-OC sites. The left and right panels display multi-annual yearly average values of τ_a^{500} and $\alpha_{440-870}$, respectively. The red bars indicate ± 1 standard deviation.



2.3 Computed quantities

Glint correction factors ρ were computed accounting for (see Eq. (2) and (3)):

- the total sky-radiance (ρ_T),
- the sole diffuse sky-radiance (ρ_d).

Overall, sky-radiance distributions were determined for 18 atmospheric cases at 22 center-wavelengths, assuming 8 different sun zenith angles for a total of 3168 sky-radiance angular distributions (at 684 discrete angles). The values of ρ_T and ρ_d were further computed for 6 different water surface conditions for a total of 19008 values of each of ρ_T and ρ_d .

The sky radiance impinging on the water surface from the sun direction naturally contains both a direct and a diffuse component, where the latter corresponds to the narrow peak of forward-scattered direct sun radiance (see Fig. 5 and Fig. 6). As a consequence, any quality-control procedure to remove above-water radiometric measurements affected by sun-glint contamination would implicitly filter out contributions from the diffuse sky-radiance peak, too. Yet, simulations of ρ_d account for diffuse radiance contributions from the entire sky-dome, thus including this same peak. This potentially introduces an inconsistency when ρ_d is applied to above-water radiometric measurements filtered for sun-glint contamination.

Still recognizing that in the adopted simulation framework the dimension of the quad containing the sun (*sun-quad*) is larger than the actual sun dimension, possible implications of discrepancies between operational and simulation frameworks are analyzed by comparing the values of ρ_d with glint correction factors simulated by masking the sun-quad (ρ_{sq}).

Differences between ρ_{sq} and ρ_d show percent values not exceeding -1.2% across all measurement conditions, and decreasing below -0.02% for cases characterizing AERONET-OC quality-controlled data (tentatively, $v_w \leq 4 \text{ m s}^{-1}$ and $\theta_0 \geq 20^\circ$; hereafter *typical AERONET-OC measurement conditions*) performed in the 400–709 nm spectral interval.

Given these negligible differences, ρ_d can be confidently utilized to determine the sky-glnt contributions to L_T .

The newly computed ρ_d values are slightly lower than those used in Zibordi et al. (2025), with mean percent differences never exceeding -1.2% for typical AERONET-OC measurement conditions between 400 and 709 nm. The update in the vertical aerosol profile has a minimal impact on the computation of ρ_d , while the adoption of the AFGL gas molecule model is responsible for the overall slight decrease, with the largest differences occurring for clear atmospheres in the ultraviolet.

As expected, the revisions applied to the atmospheric model have a larger impact on ρ_T , with a mean percent decrease up to -4.2% across all cases, narrowing to -1.1% for typical AERONET-OC measurement conditions in the 400–709 nm spectral interval.

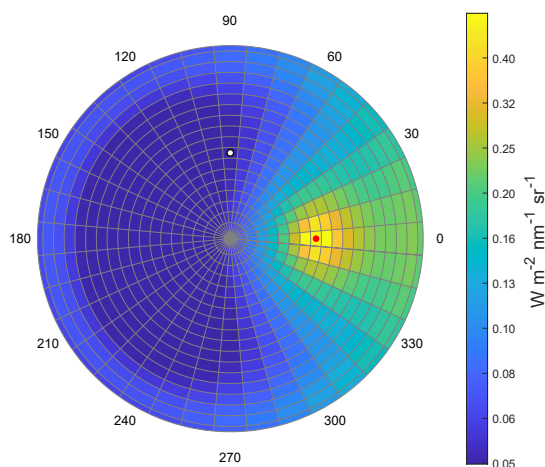
3 Results and discussion

Results are presented by first illustrating the main components of Eq. (3) — the diffuse sky-radiance and the water-surface reflectance matrices — followed by a detailed analysis of the ρ_T and ρ_d values and their dependence on environmental parameters.

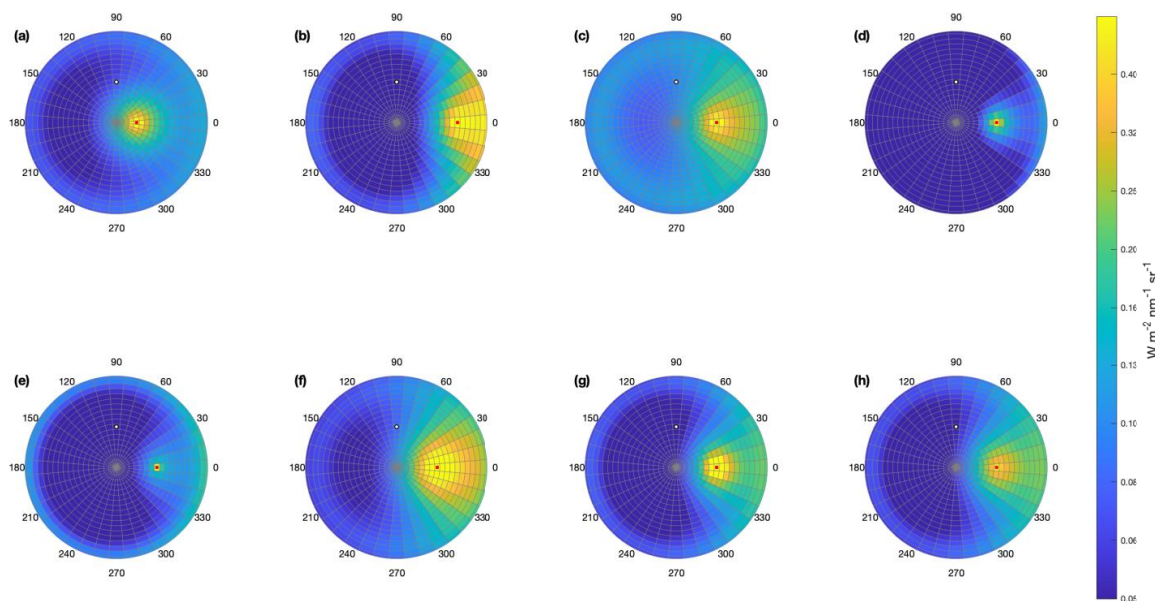
Figure 5 displays the angular distribution of the diffuse sky radiance (i.e., matrix $\mathcal{L}$ for diffuse L_{sky}) at $\lambda = 560 \text{ nm}$, for the MX aerosol model, $\tau_a^{560} = 0.2$, and $\theta_0 = 40^\circ$. The additional plots in Fig. 6 illustrate the dependence of the diffuse sky radiance on sun elevation, wavelength, aerosol load and type. Under conditions characterized by reduced multiple scattering (low θ_0 , large λ , low τ_a^{560} , and more forward-scattering aerosol), the angular distribution of the diffuse sky radiance shows a narrower peak near the sun-quad.



305



310 **Figure 5:** Angular distribution of the diffuse sky radiance at 560 nm for the MX aerosol model, $\tau_a^{560} = 0.2$, and $\theta_0 = 40^\circ$. The solar plane crosses the hemisphere from $\phi = 0^\circ$ to $\phi = 180^\circ$. The measurement plane crosses the hemisphere from $\phi = 90^\circ$ to $\phi = 270^\circ$. The red dot indicates the sun-quadrant; the white dot the L_i -quadrant.



315 **Figure 6:** As in Figure 5, but for (a) $\theta_0 = 20^\circ$, (b) $\theta_0 = 60^\circ$, (c) 412 nm, (d) 865 nm, (e) $\tau_a^{560} = 0.05$, (f) $\tau_a^{560} = 0.5$, (g) the MA aerosol model, (h) the CO aerosol model.

Examples of *water-surface reflectance matrices* $\mathcal{R}$ at 560 nm are given in Fig. 7, clearly depicting the consistent enlargement with wind speed of the portion of the sky-dome contributing to L_R .

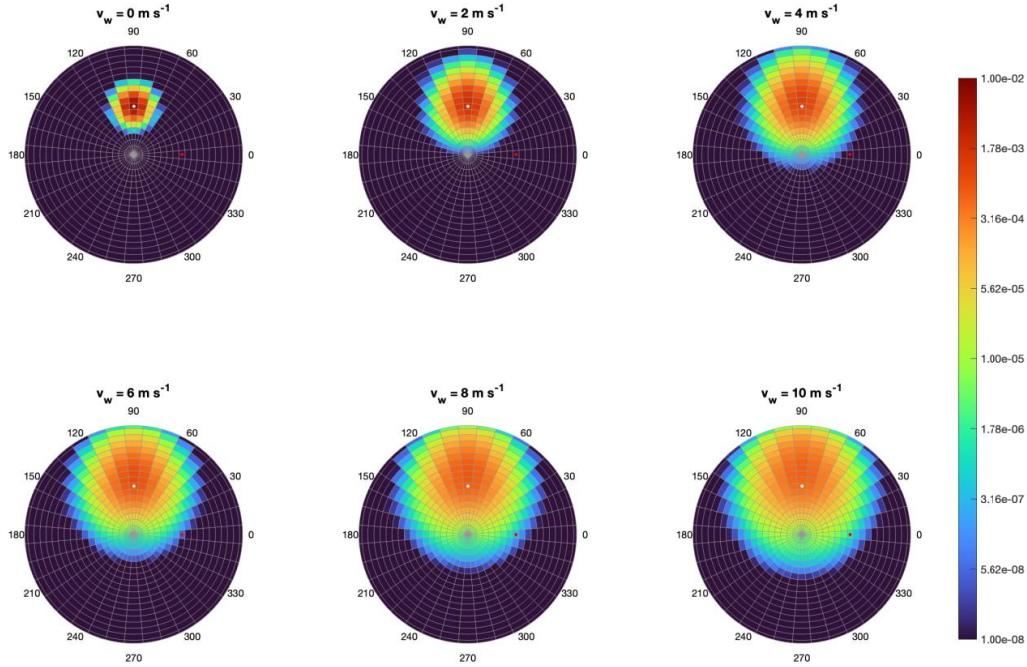


Figure 7: Water-surface reflectance matrix $\mathcal{R}$ determined at $\lambda = 560$ nm for v_w ranging from 0 to 10 m s^{-1} , at 2 m s^{-1} increment. The solar plane crosses the hemisphere from $\phi = 0^\circ$ to $\phi = 180^\circ$. The measurement plane crosses the hemisphere from $\phi = 90^\circ$ to $\phi = 270^\circ$. The white dot indicates the L_l -quad; the red dot the sun-quadrant when $\theta_0 = 40^\circ$. Results for $v_w = 0 \text{ m s}^{-1}$ are explained by the background term of Eq. (4).

3.1 Considerations on sun-glint contributions

The probability to sample the sun-quadrant — identified by (k_s, m_s) — is here expressed as $\mathcal{R}_{sq} = \frac{\mathcal{R}(k_s, m_s)}{\sum_k \sum_m \mathcal{R}(k, m)} \cdot 100$. Representative values of $\mathcal{R}_{sq}$, together with their statistical uncertainty, are provided in Table 2 for $\lambda = 560$ nm and $\theta_0 = 40^\circ$. Within the MC statistical uncertainties, $\mathcal{R}_{sq}$ shows a strong increase with wind speed, yet remains within 0.005 % even for $v_w = 10 \text{ m s}^{-1}$. Nonetheless, plots of Fig. 8, which display the angular origin of direct and diffuse sky-radiance contributions to L_R (i.e., $L_R(k, m) = \mathcal{R}(k, m) \cdot \mathcal{L}(k, m)$), highlight how contributions to L_R from the sun-quadrant (i.e., the sun-glitter $L_R(k_s, m_s) = \mathcal{R}(k_s, m_s) \cdot \mathcal{L}(k_s, m_s)$) are already significant for $v_w = 6 \text{ m s}^{-1}$, and how they become the most important contribution for $v_w = 8 \text{ m s}^{-1}$, as evidenced by the sun-quadrant being the brightest element in the figure.

These findings further underline the need to carefully apply quality-control protocols to filter out measurements affected by sun-glitter contamination.

Table 2 Probability $\mathcal{R}_{sq} \pm \sigma$ (in percent) of sampling the sun-quadrant for $\lambda = 560$ nm and $\theta_0 = 40^\circ$.

$v_w [\text{m s}^{-1}]$	0	2	4	6	8	10
$\mathcal{R}_{sq} \pm \sigma$	0.0 ± 0.0	$8.4\text{e-}7 \pm 8.2\text{e-}7$	$1.6\text{e-}5 \pm 4.5\text{e-}6$	$2.0\text{e-}4 \pm 1.9\text{e-}5$	$1.4\text{e-}3 \pm 3.8\text{e-}5$	$4.8\text{e-}3 \pm 8.3\text{e-}5$

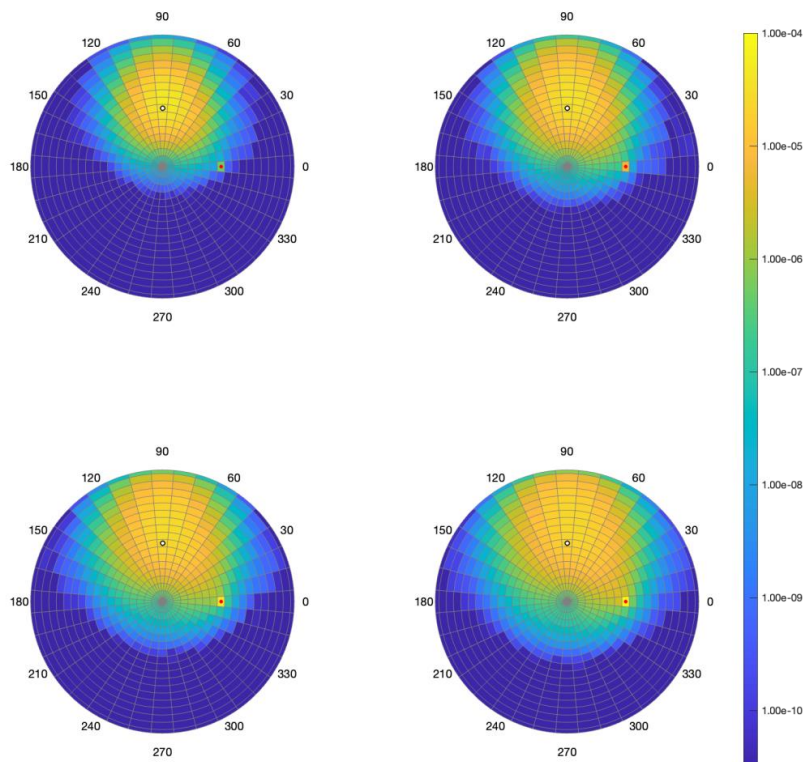


Figure 8: Angular distribution of the sky-dome origin of direct and diffuse radiance contributions to L_R , $L_R(k, m)$, as determined for the MX aerosol at 560 nm with $\theta_0 = 40^\circ$ and (from top-left to bottom-right) $v_w = 4, 6, 8, 10 \text{ m s}^{-1}$. The red dot indicates the sun-quad. The white dot indicates the L_i -quad.

Acknowledging that values of $\rho_D = \rho_T - \rho_d$ might be used to theoretically estimate sun-glint contributions to L_T , Fig. 9 presents ρ_D for the MX aerosol model and for representative wavelengths and aerosol loads. Plotted results confirm that sun-glint contributions strongly increase with wind speed and with conditions favoring larger direct sky-radiance contributions, i.e., for longer wavelengths, low aerosol optical depth and low solar zenith angles.

Notably, the most favorable measurement conditions intrinsically confirmed by AERONET-OC quality-controlled data (Zibordi et al., 2022a) correspond to conditions of negligible sun-glint contamination: low-to-mild wind speeds v_w tentatively not exceeding 4 m s^{-1} , and sun zenith angles θ_0 larger than approximately 20° .

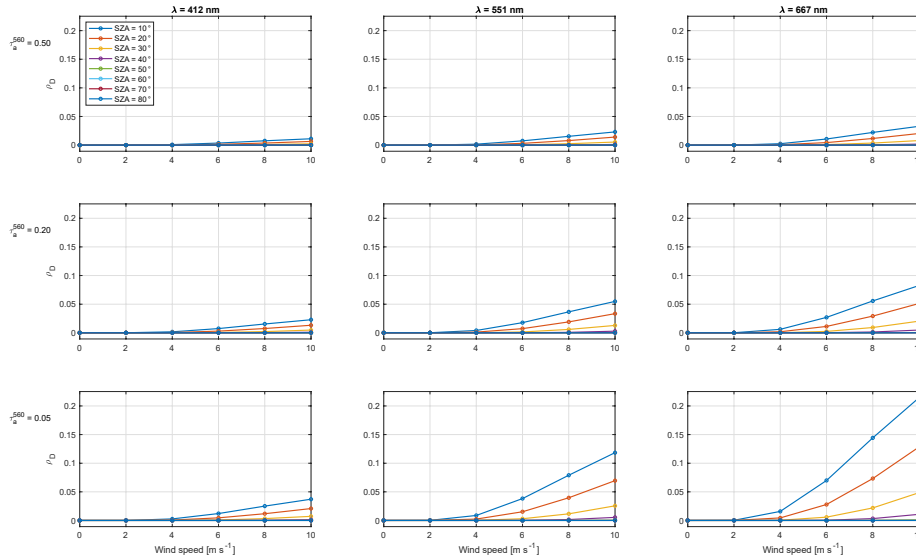


Figure 9: Plots of ρ_D as a function of wind speed for different values of θ_0 . Results are for the MX aerosol model at representative wavelengths and for different values of τ_a^{560} .

3.2 Overall characterization of ρ_T and ρ_d factors

Assuming that quality-control procedures allow for removing measurements affected by sun-glint, the correction for surface perturbations in above-water radiometry should rely on ρ_d . Yet, the long-standing community-wide application of ρ -factors accounting for total sky-radiance contributions suggests the determination and provision of both ρ_T and ρ_d .

Full and conditional distributions of ρ_T are summarized in Fig. 10. The histogram distribution of ρ_T (displayed in logarithmic scale in Fig. 10a) is extremely skewed, with a long tail of rare, yet extremely large values, corresponding to conditions of high wind speeds, low solar zenith angles, low aerosol loads and large wavelengths, as reflected in the longest right whiskers of the box plots of Fig. 10b-f. These environmental conditions are associated with sun-glint contamination. Fig. 10b additionally shows clearly distinct distributions for the lowest ρ_T values.

Apart from the strong increase of ρ_T with wind speed and decreasing sun zenith angle, explained by sun-glint contamination, the plots further show a noticeable overall ρ_T decrease with increasing aerosol load (as a consequence of a more isotropic distribution of the sky-radiance) and an appreciable increase with wavelength (as a consequence of aerosol optical depth decrease).

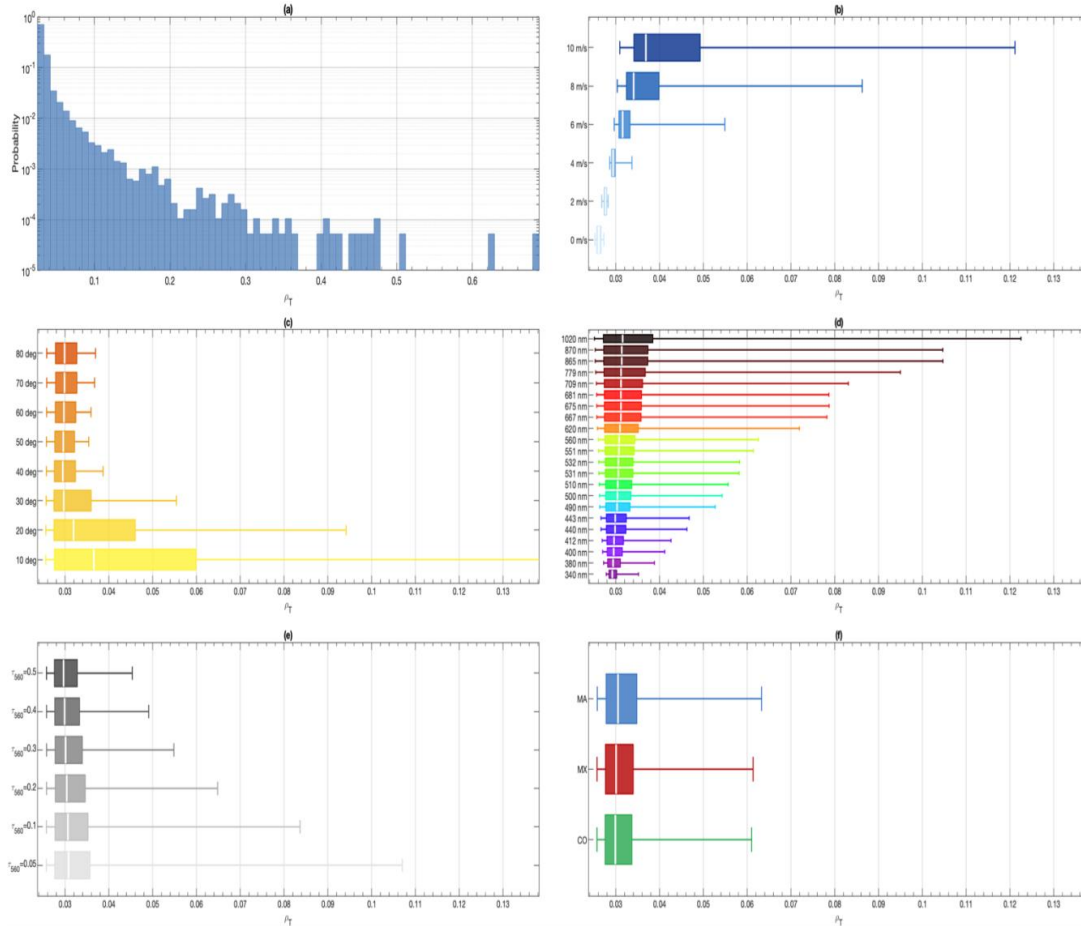
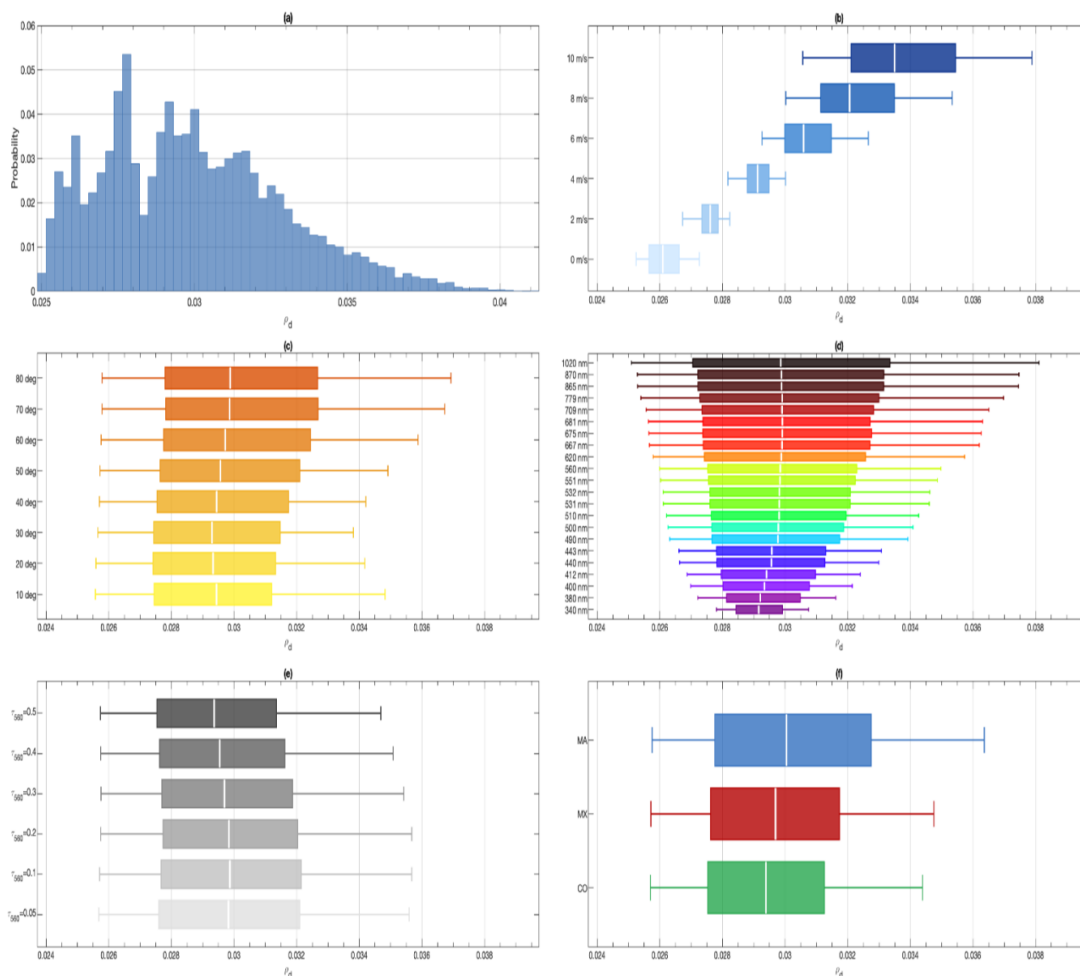


Figure 10. Panel (a) shows the histogram distribution of ρ_T on a logarithmic scale. The other panels display the box plots of ρ_T for different values of (b) wind speed v_w , (c) solar zenith angle θ_0 , (d) wavelength λ , (e) aerosol optical depth τ_a^{560} , and (f) aerosol type, while pooling over all other parameters. In the box plots, the vertical line indicates the median, the box extends over the interquartile range (IQR), while the whiskers extend to the 5th and 95th percentiles.

When considering the sole diffuse sky-radiance contributions to water-surface reflection, the histogram distribution of ρ_d (displayed on a linear scale in Fig. 11a) does not exhibit the long tail observed for ρ_T . The more symmetric distribution shows well-separated box plots at low wind speeds, which increasingly overlap for larger v_w (Fig. 11b), confirming wind speed as the major driver of ρ_d variability (Fig. 11). The box plots of Fig. 11c-f show how the overall dependence of ρ_d on θ_0 , λ , and aerosol type and load, is considerably lower than that of ρ_T . Still noticeable is a slight increase in ρ_d median and IQR values for decreasing sun elevation, increasing wavelength, decreasing aerosol load and for the maritime aerosol.

Acknowledging the significant dependence of ρ_d on the wind speed, a detailed analysis is presented in Sect. 3.3 for each wind speed value separately.



395 **Figure 11.** As in Fig. 10, but for ρ_d . Note that the scale of the distribution of ρ_d is now linear, and the x-axis range is consistently
 400 smaller.

To facilitate the direct comparison between the ρ_T and ρ_d values, Fig. 12 shows box plots of their
 400 respective full distributions, with summary statistics.

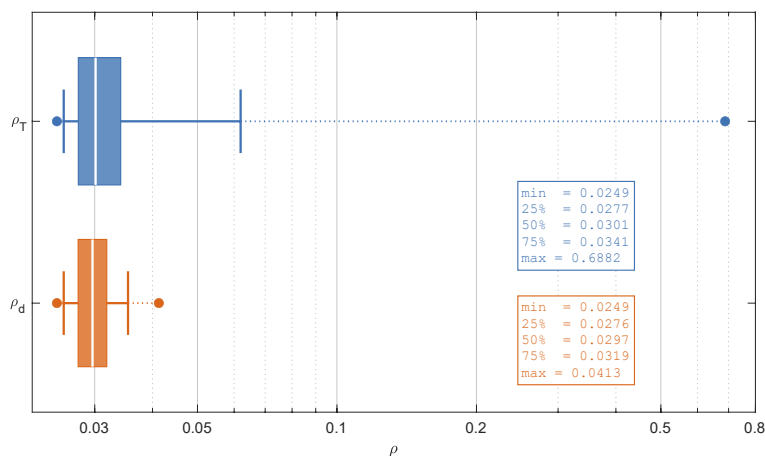
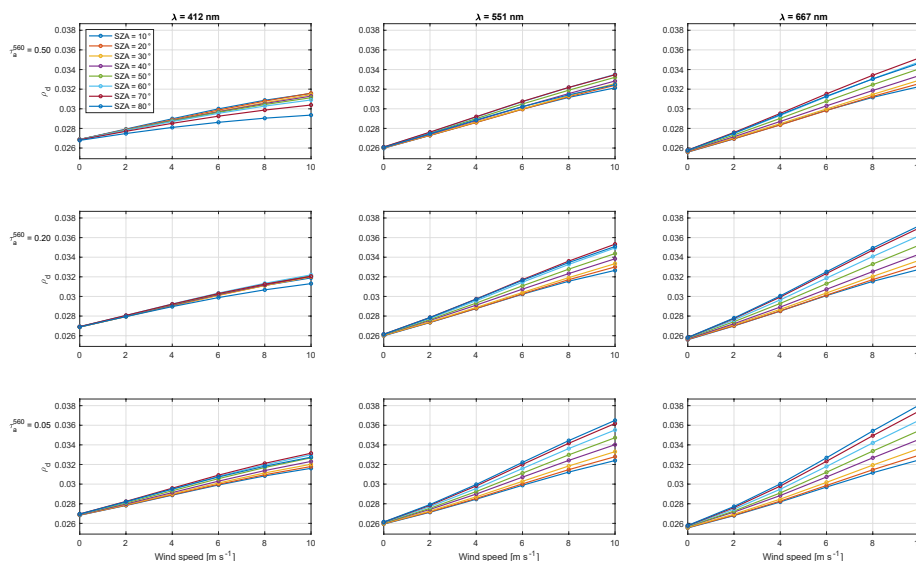


Figure 12: Box plots of the full distribution of ρ_T and ρ_d with statistical values.

405 Examples of ρ_d values are given in Fig. 13 for the same simulation conditions applied to the ρ_D values plotted in Fig. 9 (note that the scale is one order of magnitude lower).



410 Figure 13: As in Fig. 9, but for ρ_d . Note that the scale is one order of magnitude lower.

3.3 Detailed analysis of atmospheric and spectral dependences

In Bulgarelli et al. (2024), values of ρ_T were presented and discussed with a specific focus on spectral and atmospheric changes with respect to reference values ρ_T^{REF} computed at 551 nm for average climatological atmospheric conditions ($\tau_a^{560} = 0.2$ and MX aerosol model), i.e., the simulation
 415 conditions best matching those adopted for the computation of community ρ_T -factors by Mobley



(1999). The analysis highlighted an overall variation of $\Delta\rho_T = \frac{\rho_T - \rho_T^{REF}}{\rho_T^{REF}} \cdot 100$ up to sixfold, narrowing drastically to within a few percent for the typical AERONET-OC measurement conditions in the 400–709 nm spectral interval.

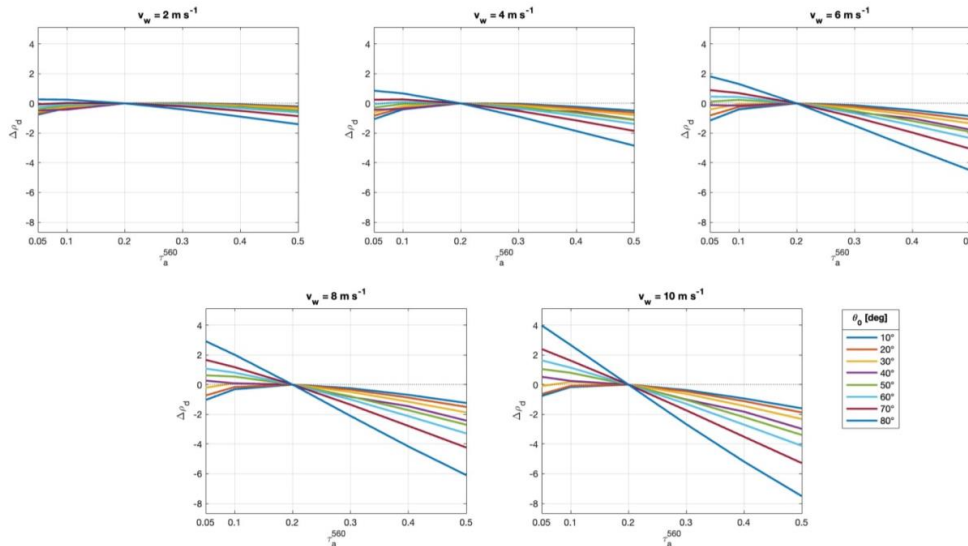
- 420 The same analysis is here conducted on ρ_d , further noting that the selected spectral and atmospheric conditions (551 nm, $\tau_a^{560} = 0.2$, MX aerosol model) correspond to conditions around which mean ρ_d values occur. For each v_w and θ_0 , changes of ρ_d with respect to ρ_d^{REF} are computed through the percent relative difference

$$425 \quad \Delta\rho_d(\theta_0; v_w; \lambda; \tau_a^{560}; A) = \left(\frac{\rho_d(\theta_0; v_w; \lambda; \tau_a^{560}; A)}{\rho_d^{REF}(\theta_0; v_w; \lambda=551; \tau_a^{560}=0.2; A=MX)} - 1 \right) \cdot 100, \quad (5)$$

where A stands for the aerosol type.

3.3.1 Dependence on the aerosol load

- 430 For reference aerosol type and wavelength, results of Fig. 14 indicate that when $v_w \leq 4 \text{ m s}^{-1}$, $\Delta\rho_d$ ranges from -2.8% to $+0.9\%$, confirming low sensitivity to the aerosol optical depth regardless of θ_0 . Yet, for larger wind speeds $\Delta\rho_d$ displays an appreciable decrease with τ_a^{560} that becomes more pronounced at high sun zenith angles. For extreme measurement conditions ($v_w = 10 \text{ m s}^{-1}$ and $\theta_0 = 80^\circ$) $\Delta\rho_d$ ranges from -7.5% to $+4.0\%$ when τ_a^{560} decreases from 0.5 to 0.05.
- 435 As expected, the dependence of ρ_T on the aerosol load (not shown here) is consistently more pronounced when v_w exceeds 4 m s^{-1} , reaching -36.9% (for $\tau_a^{560} = 0.05$) and $+72.5\%$ (for $\tau_a^{560} = 0.5$) when $v_w = 10 \text{ m s}^{-1}$ and $\theta_0 = 10^\circ$.



440 **Figure 14:** Values of $\Delta\rho_d$ (in percent) determined with respect to ρ_d^{REF} as a function of τ_a^{560} for different values of v_w and θ_0 . Each panel refers to a different value of v_w .

3.3.2 Spectral dependence

The spectral dependence of glint correction factors is induced by the spectral variation of both the atmospheric optical properties and, to a lesser extent, the water refractive index.

- 445 Fig. 15 shows plots of $\Delta\rho_d$ for reference aerosol type and load. Results for $v_w = 0 \text{ m s}^{-1}$ highlight the influence due to the sole spectral change of the water refractive index, which leads to a slight decrease



of ρ_d with wavelength. Opposite is the effect of the optical depth: the spectral decrease of τ_d induces a spectral increase of ρ_d (in agreement with Sect. 3.3.1). This spectral dependence of ρ_d is more pronounced for high θ_0 and v_w : spectral values of $\Delta\rho_d$ range within -3.8% and $+7.1\%$ for $v_w \leq 4\text{ m s}^{-1}$, but within -16.6% and $+14.0\%$ for $\theta_0 = 80^\circ$ and $v_w = 10\text{ m s}^{-1}$. As expected, the spectral dependence of ρ_T is consistently more pronounced for wind speeds larger than 4 m s^{-1} , reaching up to -53.8% (at 340 nm) and $+129.8\%$ (at 1020 nm) when $v_w = 10\text{ m s}^{-1}$ and $\theta_0 = 10^\circ$.

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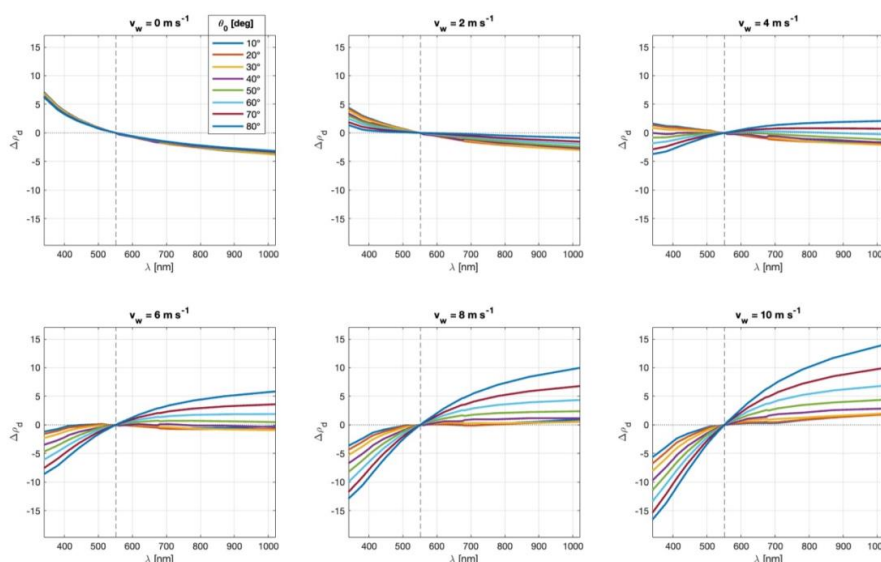


Figure 15: Values of $\Delta\rho_d$ (in percent) as a function of λ for the MX aerosol model with $\tau_d^{560} = 0.2$ and for different values of v_w and θ_0 . Each panel refers to a specific value of v_w .

3.3.3 Dependence on the aerosol type

460 The optical properties of continental aerosols exhibit stronger spectral variations in comparison to those of mixed and maritime aerosols, while the phase function is less forward-peaked: this clearly affects the spectral dependence of ρ_d . Illustrative results are provided in Fig. 16 for pure maritime (MA) and pure continental (CO) aerosols with $\tau_d^{560} = 0.2$ and $v_w = 10\text{ m s}^{-1}$. Although in both cases $\Delta\rho_d$ varies between -16.8% and $+15.3\%$, in the presence of maritime aerosol $\Delta\rho_d$ shows a much lower
 465 dependence on θ_0 . Remarkably, the sensitivity of ρ_T to the aerosol type is much higher, with values of $\Delta\rho_T$ ranging between -56.7% and $+52.4\%$ for the maritime aerosol, and between -53.5% and $+175.1\%$ for the continental aerosol.

470

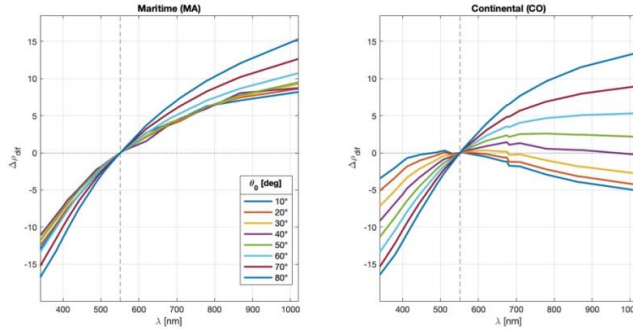


Figure 16: Spectral values of $\Delta\rho_d$ (in percent) for diverse aerosol types and θ_0 and for $\tau_a^{560} = 0.2$ and $v_w = 10 \text{ m s}^{-1}$.

3.3.4 Overall spectral and atmospheric variability

The overall variability of ρ_d with respect to reference values (i.e., those determined from average climatological conditions at 551 nm) is summarized in the histogram distribution of Fig. 17a. $\Delta\rho_d$ varies between -20.2% and $+19.3\%$, with a mean of -0.5% and a standard deviation of 3.9% . Updated values of $\Delta\rho_T$ (computed with the revised atmospheric model) span from -59.6% to $+687\%$, with a mean of $+2.7\%$ and a standard deviation of 31.0% , relative to reference conditions, which best match those applied by Mobley (1999).

When restricting the analysis to typical AERONET-OC measurement conditions in the 400–709 nm spectral interval, the distribution of $\Delta\rho_d$ significantly narrows, exhibiting a standard deviation of 1.2% (Fig. 17b).

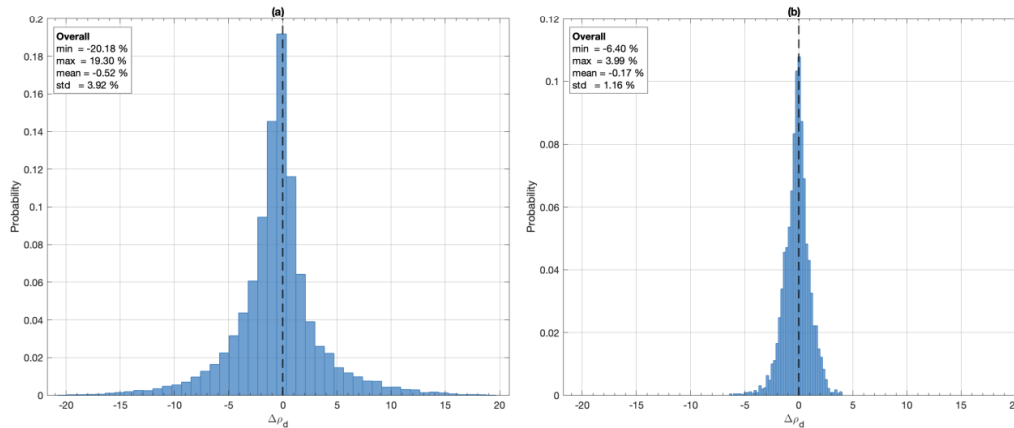


Figure 17: Normalized histograms of $\Delta\rho_d$ (in percent) for (a) overall data and (b) data characterized by $v_w \leq 4 \text{ m s}^{-1}$ and λ within 400–709 nm. Statistical values refer to maximum (max), minimum (min), average (mean), and standard deviation (std).

3.4 Considerations on uncertainties

The weak dependence of ρ_d on τ_a^{560} (see Sect. 3.3.1) implies low ρ_d sensitivity to uncertainties in the aerosol load. Percent relative differences $\Delta\tau_a$ induced on ρ_d by an absolute uncertainty $u(\tau_a) = 0.02$ (Eck et al., 1999) are always below 1% . Different is the case for ρ_T , where $\Delta\tau_a$ may reach 8% for extreme measurement conditions defined by $v_w = 10 \text{ m s}^{-1}$ and $\theta_0 = 10^\circ$.

The variability of ρ_d with wind speed is more significant, and a realistic absolute uncertainty $u(v_w) = 2 \text{ m s}^{-1}$ on v_w (Vis et al., 2022; Cazzaniga and Zibordi, 2023) leads to more appreciable percent



relative differences Δ_{v_w} on ρ_d , ranging from 4 % to 7 % at the reference conditions (see Fig. 18a). The more pronounced dependence of ρ_T on v_w implies a much stronger sensitivity of ρ_T to uncertainties in the wind speed: for the same absolute uncertainty $u(v_w) = 2 \text{ m s}^{-1}$, Δ_{v_w} on ρ_T reaches 46 % for the reference conditions (Fig. 18b).

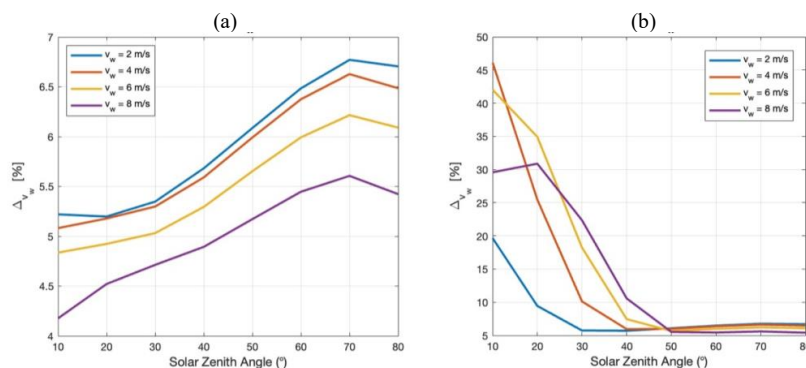


Figure 18: Relative percentage differences Δ_{v_w} on (a) ρ_d and (b) ρ_T induced by an absolute uncertainty $u(v_w) = 2 \text{ m s}^{-1}$ on v_w at the reference conditions. Note that the scale is different.

4 Data availability

The newly computed spectral glint correction factors for above-water radiometric measurements are accessible at Zenodo (Bulgarelli et al., 2026; <https://doi.org/10.5281/zenodo.20609990>). The dataset is provided as a single HDF5 file (`rho_factors.h5`) containing two datasets: `rho_dif`, the glint correction factors ρ_d computed using diffuse sky radiance, and `rho_tot`, the glint correction factors ρ_T computed using total sky radiance (diffuse and direct components). Values are tabulated as a function of tropospheric aerosol type (MA, CO, MX), aerosol optical depth at 560 nm (0.05–0.50), wavelength (340–1020 nm), solar zenith angle (10°–80°), and wind speed (0–10 m s^{-1}). A README file documents the database structure and provides usage examples in Python.

5 Summary and conclusions

Glint correction factors ρ_T and ρ_d for the removal of water-surface reflection of total and diffuse sky-radiance in above-water radiometric measurements, respectively, were spectrally simulated in the 340–1020 nm region for a wide range of atmospheric, water-surface and illumination conditions typical of inland, coastal and open-ocean regions. Values of $\rho_D = \rho_T - \rho_d$ were additionally used to provide physical insight into the origin and magnitude of sun-glint contamination. Computations were performed by adopting the AERONET-OC observation geometry supported by current measurement protocols, and relying on *i*) the scalar FEM plane-parallel radiative transfer code in its SkyFEM configuration for the simulation of the angular distribution of the sky radiance impinging at the water surface and *ii*) the MOX three-dimensional Monte Carlo code for the simulation of the water-surface reflecting properties under different wind conditions. The impact of sun-glint perturbations was separately discussed, confirming its increase with wind speed and wavelength, and with decreasing solar zenith angle and aerosol load. Notably, it was also confirmed that AERONET-OC quality-controlled measurement conditions, typically referring to $v_w \leq 4 \text{ m s}^{-1}$ and $\theta_0 \geq 20^\circ$, inherently correspond to conditions of minor sun-glint contamination.

Acknowledging the long-standing application of ρ -factors accounting for total sky-radiance contributions, and, in turn, the advantage of solely considering the diffuse sky-radiance contributions when quality-control procedures enable flagging measurements affected by sun-glint, both ρ_T and ρ_d values were presented and discussed.



535 The comparative analysis of ρ_T and ρ_d data highlighted *i.* an extremely skewed distribution of ρ_T (due to sun-glint) exhibiting a strong dependence on environmental parameters, particularly on wind speed and solar zenith angle; *ii.* a considerably narrower distribution of ρ_d with a more regular shape still exhibiting a significant dependence on wind speed, but an overall lower dependence on the other environmental parameters.

540 The remarkable dependence of ρ_d on wind speed motivated a further analysis at discrete wind speed values. Specifically, spectral and atmospheric changes of ρ_d were analyzed with respect to reference values at 551 nm for average atmospheric conditions, defined by $\alpha_{440-870}^{col} = 1.08$ and $\tau_a^{560} = 0.2$. It is recalled that these reference conditions best correspond to those adopted by Mobley (1999) for the simulation of the community ρ_T -factors, and to conditions around which mean ρ_d values occur. The

545 analysis showed low sensitivity of ρ_d to atmospheric optical properties, with a slight decrease with increasing aerosol load. Conversely, results showed a slight spectral decrease of ρ_d in the absence of wind, and a more consistent spectral increase with v_w . For reference aerosol load and type, a maximum spectral variation from -16.6% to $+14.0\%$ occurred for $\theta_0 = 80^\circ$ and $v_w = 10 \text{ m s}^{-1}$. Overall results indicated changes of ρ_d with respect to reference values distributed around -0.5% with

550 a standard deviation of 3.9% . The standard deviation drops to 1.2% for typical AERONET-OC observation conditions in the $400\text{--}709 \text{ nm}$ spectral interval. Positive changes occur for pure maritime aerosol and longer wavelengths, while negative changes occur for optically thicker atmospheres, pure continental aerosol and shorter wavelengths. Evident are the much larger changes of ρ_T with respect to reference values, ranging from -59.6% to

555 $+687\%$, with a mean of $+2.7\%$ and a standard deviation of 31.0% . This has clear implications for the sensitivity of glint correction factors to uncertainties in input parameters. While ρ_T shows high sensitivity to uncertainties in wind speed and/or aerosol optical depth, values of ρ_d exhibit relative stability. Notably, the newly computed ρ_d values are slightly lower than those utilized in Zibordi et al. (2025),

560 with mean percent differences never exceeding -1.2% for the typical AERONET-OC measurement conditions in the $400\text{--}709 \text{ nm}$ spectral range. Acknowledging this, and recalling results from Zibordi et al. (2025), the impact of the newly computed ρ_d in the determination of L_w is expected to be particularly significant in regions exhibiting optically complex waters, with a general increase of the derived normalized water-leaving radiance L_{WN} from a few to tens of percent for sites characterized by

565 highly absorbing or scattering waters.

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Author Contribution

GZ, BB and DD contributed to the conceptualization of the study. BB performed the formal data analysis and prepared the original draft. BB and DD contributed to data curation; BB, DD and TK to the software development. All authors contributed to the review and editing.

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Competing interests

The contact author has declared that none of the authors has any competing interests.



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