



### Bowen ratio-constrained global dataset of air-sea turbulent heat 1 2 fluxes from 1993 to 2017 Yizhe Wang<sup>a, b</sup>, Ronglin Tang<sup>a, b, \*</sup>, Meng Liu<sup>c</sup>, Lingxiao Huang<sup>a, b</sup>, Zhao-Liang Li<sup>a, b, c</sup> 3 4 <sup>a</sup> State Key Laboratory of Resources and Environment Information System, Institute of 5 Geographic Sciences and Natural Resources Research, Chinese Academy of Sciences, 6 Beijing 100101, China <sup>b</sup> University of Chinese Academy of Sciences, Beijing 100049, China 7 8 <sup>c</sup> State Key Laboratory of Efficient Utilization of Arable Land in China, Institute of 9 Agricultural Resources and Regional Planning, Chinese Academy of Agricultural 10 Sciences, Beijing 100081, China \* Authors to whom correspondence should be addressed: tangrl@lreis.ac.cn 11 12 13 14



### 15 Abstract

16 Air-sea turbulent heat fluxes, including the sensible heat flux (SHF) and latent heat 17 flux (LHF), along with the Bowen ratio ( $\beta$ , ratio of SHF to LHF), are crucial for 18 understanding air-sea interaction and global energy and water budgets. However, the 19 existing products, primarily developed using the semi-empirical bulk aerodynamic 20 methods and data-driven machine learning approaches, are often weak in accuracy and 21 physical rationality, due to the uncertainties in the environmental forcings and 22 inappropriate parameterizations. In this study, we generated a global daily 0.25° product 23 of air-sea turbulent heat fluxes using the Bowen ratio-constrained Neural Network (NN) 24 model (referred to as the BrTHF model) that could coordinately estimate the SHF and 25 LHF, along with the observations from 197 globally distributed buoys and multi-source 26 remote sensing and reanalysis forcings. The spatial ten-fold cross-validation results 27 showed that the BrTHF model, achieving root mean square errors of 6.05 W/m<sup>2</sup>, 23.67 28 W/m<sup>2</sup> and 0.22 and correlation coefficients of 0.93, 0.91 and 0.25 for the SHF, LHF and 29  $\beta$ , respectively, outperformed the physics-agnostic NN model and seven widely used 30 air-sea turbulent heat flux products (including JOFURO3, IFREMER, SeaFlux, ERA5, 31 MERRA2, OAFlux, and OHF). Furthermore, the inter-comparison of the spatial 32 distribution of multi-year means, as well as intra-annual and inter-annual change 33 patterns showed that the BrTHF product reliably simulated global SHF, LHF and  $\beta$ , in 34 contrast to the machine learning-based OHF product that failed to replicate these 35 patterns. The main advantage of the BrTHF model lies in its improved rationality of  $\beta$ 36 estimates, successfully eliminating the outliers observed in the physics-agnostic NN 37 model and the seven typical products. The improved SHF, LHF, and  $\beta$  estimates can 38 allow for more accurate quantification of the global air-sea energy and water budgets, 39 enhance our understanding of air-sea interaction, and improve projections of climate 40 change under global warming. The 0.25° daily global product from 1993 to 2017 can 41 be freely accessed from the National Tibetan Plateau Data Center (TPDC) 42 [https://doi.org/10.11888/Atmos.tpdc.302578, Tang and Wang (2025)].





43 Keywords: Air-sea turbulent heat fluxes; Sensible heat flux; Latent heat flux; Bowen

- 44 ratio
- 45 **1. Introduction**

46 Air-sea turbulent heat fluxes (THF), comprising the evaporative latent heat flux 47 (LHF) and conductive sensible heat flux (SHF), play vital roles in the Earth's climate 48 system by characterizing the exchange of energy and water between the ocean and 49 atmosphere (Wild et al., 2014; Loeb et al., 2021; Fasullo et al., 2014). The ratio, 50 commonly referred to as the Bowen Ratio ( $\beta = SHF/LHF$ ), serves as a key indicator 51 revealing the partitioning of water and energy over the ocean and atmosphere (Jo, 2002; 52 Andreas et al., 2013; Liu and Yang, 2021). Accurate estimation of these three 53 parameters is an essential prerequisite for advancing our understanding of 54 atmosphere-sea interaction (Gentemann et al., 2020), improving the quantification of 55 global water and energy budget (Zhang, 2023), and enhancing the predictability of 56 extreme weather events (Yu, 2019).

57 To map global air-sea turbulent heat fluxes, the semi-empirical bulk aerodynamic 58 method, which establishes scaling relationships between flux and profiles of easily 59 measured mean metrological quantities, such as near-surface gradients of humidity, 60 temperature and wind (Yu, 2019), based on the Monin-Obukhov similarity theory (Monin and Obukhov, 1954), was developed and widely adopted as a primary approach. 61 62 This method, for its ease of application, has been applied to generate tens of widely 63 used products in the past few decades (Shie et al., 2009; Liman et al., 2018; Yu and Weller, 2007; Berry and Kent, 2011; Tomita et al., 2018; Crespo et al., 2019). However, 64 65 there were huge discrepancies in the global and regional magnitude and patterns of SHF and LHF among these products, which seriously imped our understanding of the key 66 67 process of the air-sea interaction and the global budget of water and energy (Bentamy 68 et al., 2017; Tang et al., 2024; Yu, 2019). The discrepancies could be partly ascribed to 69 the substantial uncertainties in the environmental forcings used to develop these 70 products (Robertson et al., 2020) and the inappropriate parameterizations regarding





71 regional atmospheric stability and boundary layer dynamics, across diverse and 72 complex environmental conditions (Brodeau et al., 2017; Jiang et al., 2024a; Jiang et 73 al., 2024b; Yang et al., 2024). Furthermore, these problems contribute a lot to the biases 74 in the SHF and LHF estimates which can even lead to the unphysical estimations of  $\beta$ , 75 as Wang et al. (2024) reported. To better describe and comprehend the air-sea 76 interaction and the energy and water budgets, the existing mode to produce global air-77 sea turbulent heat fluxes needs improvement urgently.

78 Machine learning techniques have been extensively applied in up-scaling in situ 79 measurements of a single variable (e.g. soil moisture, roughness or temperature) to the 80 globe (Wang et al., 2023; Peng et al., 2022; O and Orth, 2021; Nelson et al., 2024; Fu 81 et al., 2023). These efforts highlight the great potential of machine learning for more 82 accurate and consistent multivariate coordinated mapping (Karniadakis et al., 2021; 83 Kashinath et al., 2021; Van Der Westhuizen et al., 2023; Wang et al., 2024). However, 84 the application of machine learning in global mapping of air-sea turbulent heat fluxes 85 remains limited. The only publicly available machine learning-based global air-sea turbulent heat fluxes product, released by the National Oceanic and Atmospheric 86 87 Administration (NOAA) Ocean heat flux CDR (hereafter dubbed OHF), 88 simultaneously modeled SHF and LHF using a Neural Network (NN) technique 89 (Clayson and Brown, 2016). Although it performed well when validated against the 90 observations from the tropical buoys, it failed to capture the regional characteristics, 91 particularly in areas where air-sea turbulent heat exchange is intense (e.g. oceans with 92 latitudes beyond 45° for SHF and subtropical highs for LHF) (Tang et al., 2024). Additionally, it exhibited different pattern of temporal evolution of global annual mean 93 94 and opposite inter-annual trends at both regional and global scales to most widely-used 95 physical model-based products, likely due to unreasonable construction of observation 96 datasets [with data before and after 2007 coming from SeaFlux in-situ datasets and 97 ICOADS (International Comprehensive Ocean-Atmosphere Data Set) datasets, 98 respectively]. Furthermore, the product likely suffers from unphysical estimates of the





99  $\beta$  due to neglecting the interrelations among SHF, LHF and  $\beta$  during the model 100 construction.

101 To improve the estimation of SHF, LHF, and  $\beta$  in a coordinative framework, we 102 recently proposed an innovative Bowen ratio-informed data-driven model by 103 considering their synergistic changes using a Random Forest (RF) technique (Wang et al., 2024). Validation against hourly high-quality eddy covariance (EC) flux 104 105 measurements from 53 historical cruises demonstrated the model's superior 106 performance, achieving high accuracy in estimating SHF, LHF, and  $\beta$ , with results that 107 are physically consistent. This work highlights the feasibility of simultaneously 108 estimating SHF, LHF, and  $\beta$  with high accuracy using machine learning techniques, 109 offering strong potential for global mapping that aligns with physical consistency. 110 However, due to limited availability of EC flux measurements (characterized by sparse spatio-temporal distributions), the application of the model for global mapping remains 111 112 constrained. Buoy-based flux observations provide a viable alternative. Although less 113 reliable than EC-based flux measurements, buoy data offer globally representative flux 114 samples with adequate volume and acceptable accuracy, which have been widely used 115 to evaluate the performance of global products (Bentamy et al., 2017; Tang et al., 2024; 116 Weller et al., 2022; Zhou et al., 2020) and support global modeling (Chen et al., 2020a) 117 and analysis (Song et al., 2024; Yan et al., 2024).

118 The primary objectives of this study are three-folds: (1) to develop an innovative 119 Bowen ratio-constrained model for improving the air-sea SHF, LHF and  $\beta$  estimates 120 (referred to as the BrTHF model hereafter) using the machine learning technique and 121 global buoy-based air-sea turbulent heat fluxes observations; (2) to demonstrate the 122 superiority of the model through an inter-comparison with seven widely used global 123 products and the estimates from the physics-free machine learning-based model; (3) to 124 produce a global daily 0.25° dataset based on the BrTHF model over ice-free oceans 125 covering the period from 1993 to 2017. The flux observations from 197 global 126 distributed buoys, along with multi-source satellite-based and reanalysis-based forcings,





- 127 were collected to construct the models and further produce the global air-sea turbulent
- heat fluxes dataset. The accuracy and spatio-temporal patterns of the SHF, LHF and  $\beta$
- 129 estimates were inter-compared with seven widely used products, including the remote
- 130 sensing-based JOFURO v3, IFREMER v4.1 and SeaFlux v3, as well as reanalysis-
- 131 based ERA5 and MERRA2, hybrid-based OAFlux v3 and machine learning-based
- 132 OHF v2 products.
- 133 **2. Data and Methods**
- 134 The following sub-sections provide an overview of the development of the BrTHF
- 135 product, detailing the construction of air-sea turbulent heat fluxes observation datasets,
- 136 forcing datasets and the BrTHF model, as well as the evaluation strategies used in this
- 137 study, as indicated in Figure 1.



- 139 Figure 1. flowchart of the generation of a global product of air-sea SHF, LHF and  $\beta$  by the
- 140 **BrTHF model**

138

### 141 2.1 Air-sea turbulent heat fluxes observation datasets

To obtain the buoy-derived air-sea turbulent heat fluxes observations, the hourly or sub-hourly oceanic and atmospheric measurements including sea surface temperature ( $T_s$ ), sea surface air temperature ( $T_a$ ), sea surface wind speed (WS) and relative humidity (RH) were firstly collected at 267 buoys covering a variety of ocean





146 basins from 13 organizations or networks, namely 67 buoys from the Tropical 147 Atmosphere Ocean/Triangle Trans-Ocean (TAO/TRITON) Buoy Network in the 148 Pacific, 20 buoys from the Prediction and Research Moored Array (PIRATA) in the 149 Atlantic, 23 buoys from the Research Moored Array for African-Asian-Australian 150 Monsoon Analysis and Prediction (RAMA) in the Indian Ocean, 73 buoys from 151 National Data Buoy Center (NDBC) around the coasts of the United States, 19 buoys 152 from Copernicus Marine In Situ Thematic Centre (TAC) nearby the coasts of Europe, 153 23 buoys from Upper Ocean Processes (UOP) Group around the low-latitude oceans 154 like the Bay of Bengal, 3 buoys from the Ocean Climate Stations Project (OCS) in the mid-latitudes like the Kuroshio Extension, 24 buoys from Korea Meteorological 155 156 Administration (KOREA) nearby the Korean Peninsula, 6 buoys from Ocean 157 Observatories Initiative (OOI) in the high latitude sea area like the Argentine Basin, 2 buoys from Alaska Ocean Observing System (AOOS) in the Arctic Ocean, 1 buoy of 158 159 JKEO nearby Japanese Ocean, 6 buoys from Irish Weather Buoy Network around British waters, and 1 buoy from Icelandic Meteorological Office (IMO) nearby the 160 161 Iceland Sea (Iceland) (Petersen, 2017). For certain buoys lacking RH measurements 162 [e.g. buoys from NDBC (National Data Buoy Center) provided dew point temperature 163 (*DEW*) rather than *RH*], we computed *RH* using *DEW* and  $T_a$  via formula (1).

164 
$$RH = 100 \times \left| \frac{\frac{17.67 \times DEW}{e^{243.5 \times DEW}}}{e^{\frac{17.67 \times DEW}{243.5 \times T_a}}} \right|$$
(1)

165 To ensure the quality of the measurements, we filtered the records based on the 166 quality control recommendations provided by the data providers. Further refinement 167 was also made by removing the questionable values that exceeded three standard 168 deviations  $(3\sigma)$  for each variable at individual buoys.

Once the data was cleaned, daily mean aggregation was applied to the oceanic and atmospheric measurements. Given the varying temporal resolutions of the measurements (e.g. NDBC provided hourly observations before 2005 and 10-min observations thereafter), we only retained the daily mean data when the fraction of the





- 173 valid hourly or sub-hourly observations exceeded 80% on a given day.
- 174 After the above mentioned data preprocessing, the daily buoy-derived air-sea 175 turbulent heat fluxes (SHF and LHF) observations were then calculated using the daily oceanic and atmospheric measurements combined with the version 3.5 of Coupled 176 177 Ocean-Atmosphere Response Experiment (COARE3.5) model (Edson, 2013) (available at https://zenodo.org/record/5110991). Following the air-sea turbulent heat 178 179 fluxes computations, we further made a quality control on the derived SHF and LHF 180 observations to exclude the abnormal records, by filtering the observations based on 181 the range of daily  $\beta$  values determined from seven widely-used flux products. 182 Specifically, we calculated the cumulative distribution of daily  $\beta$  for each product and their ensemble (across all products). The medians of the 1<sup>st</sup> and 99<sup>th</sup> percentiles, 183 approximately -5 and 5, respectively, were selected as the minimum and maximum of 184 valid daily  $\beta$ , as shown in Figure S1. In total, this study compiled 463,585 observations 185 186 of valid daily air-sea turbulent heat flux from 197 buoy stations (Figure 2 and Table S1) 187 in the Arctic Ocean, Pacific Ocean, Atlantic Ocean and Indian Ocean.





Figure 2. Geographic locations of 197 buoy sites from 12 organizations or networks involved in this analysis including TAO/TRITON, PIRATA, RAMA, NDBC, TAC, UOP, OOI, AOOS, KOREA, OCS, JKEO and IMO. The boundaries of global land and open oceans were sourced from the Natural Earth dataset (<u>https://www.naturalearthdata.com/downloads/</u>) and the Global Oceans and Seas dataset (<u>https://www.marineregions.org/sources.php</u>), respectively. Abbreviations MR refers to the Mediterranean Region. It should be noted that the Caspian Sea was not included within the boundaries of the open oceans and is shown in white.





Finally, the quality-controlled observations were collected to train and validate the
BrTHF model. Note that the COARE-based observations at the buoy stations have
already widely applied as a benchmark for global air-sea turbulent heat flux product
development and evaluation (Bentamy et al., 2017; Chen et al., 2020b; Tang et al., 2024;
Weller et al., 2022)
201 2.2 Forcing datasets and state-of-the-art products

### 202 2.2.1 Forcing datasets

203 Forcing variables were carefully selected based on their potential impacts on the 204 variations of the air-sea turbulent heat fluxes (Grist et al., 2016; Kudryavtsev et al., 2014; Myslenkov et al., 2021; Song, 2020, 2021; Yan et al., 2024) to conduct the feature 205 206 selection (see section 2.3.1). These variables include  $T_a$ , sea surface air specific 207 humidity  $(O_a)$ , Mean Sea Level Pressure (SLP), Downward Long Wave Radiation Flux (LW), Downward Short Wave Radiation Flux (SW),  $T_s$ , sea surface specific humidity 208 209  $(Q_s)$ , Absolute Dynamic Topography (ADT), Sea Level Anomaly (SLA), Sea Surface 210 Salinity (SSS), Sea Surface Density (SSD), Ocean Mixed Layer Current Velocity (CS), 211 WS, Significant Wave Height (SWH), Wave period  $(T_p)$ , as well as gradient of 212 temperature (diff<sub>T</sub>) calculated using the  $T_s$  and  $T_a$ , and gradient of humidity (diff<sub>Q</sub>) 213 calculated using the  $Q_s$  and  $Q_a$ .

214 Datasets of these forcing variables were collected from the following sources (Table 1): the daily 0.25° ERA5 meteorology dataset (providing  $T_a$ ,  $Q_a$ , SLP, LW and 215 216 SW) (Hersbach et al., 2020) from the European Centre for Medium-Range Weather Forecasts (ECMWF) Climate Data Store (CDS), the daily 0.25° the Optimum 217 218 Interpolation Sea Surface Temperature (OISST) dataset ( $T_s$  and  $O_s$ ) (Huang et al., 2021), 219 the daily 0.25° Global Ocean Gridded L4 Sea Surface Heights And Derived Variables 220 Reprocessed 1993 Ongoing (SSH) dataset (ADT and SLA), daily 0.125° Multi 221 Observation Global Ocean Sea Surface Salinity and Sea Surface Density (MOGOSD) 222 dataset (SSS and SSD) and 3-hour 0.2° Global Ocean Waves (GOW) Reanalysis dataset 223  $(SWH \text{ and } T_p)$  from the Copernicus Marine Environmental Monitoring Service





224	(CEMES), the daily 0.25° Ocean Surface Current Analysis Real-time (OSCAR) dataset
225	(CS) (Bonjean and Lagerloef, 2002) from the Physical Oceanography Distributed
226	Active Archive Center of the National Aeronautics and Space Administration (NASA)
227	Jet Propulsion Laboratory (JPL), the 6-hour 0.25° Cross-Calibrated Multi-Platform
228	(CCMP) wind vector analysis dataset (WS) from the Remote Sensing Systems (RSS).
229	The MOGOSD and GOW datasets were spatially resampled to a $0.25^\circ$ resolution
230	using mean aggregation, while temporal mean aggregation to daily values was applied
231	to the GOW (originally at 3-hour resolution) and CCMP (6-hour resolution) datasets.
232	Additionally, a daily ERA5 sea-ice mask was applied to the datasets to mitigate the
233	impact of sea ice.

### 234 2.2.2 State-of-the-art products for inter-comparison

Seven widely used air-sea turbulent heat fluxes products, involving remote
sensing-based JOFURO3, IFREMER and SeaFlux, as well as reanalysis-based ERA5
and MERRA2, hybrid-based OAFlux and machine learning-based OHF products were
selected for inter-comparison.

239 The remote sensing-based JOFURO3, IFREMER, and SeaFlux products were 240 developed by the Japanese Ocean Flux Data Sets under the Remote Sensing 241 Observations (J-OFURO) research project, the Institute Français de Recherche pour 242 l'Exploitation de la Mer (IFREMER), and the NASA Global Hydrology Resource 243 Center (GHRC) Distributed Active Archive Center (DAAC), respectively. The 244 reanalysis-based ERA5 and MERRA2 products were developed by the ECMWF and 245 NASA Global Modeling and Assimilation Office (GMAO), respectively. The hybridbased OAFlux and machine learning-based OHF products were developed or published 246 247 by the Woods Hole Oceanographic Institution (WHOI) and NOAA Ocean Surface 248 Bundle (OSB) Climate Data Record (CDR), respectively.

With the exception of the OHF product calculating SHF and LHF simultaneously
using a NN model without a constraint, all other products employed bulk aerodynamic
methods to estimate SHF and LHF. The JOFURO3, IFREMER, and OAFlux products





252 used the COARE3.0 model, while the SeaFlux used the COARE3.5 model. Differently, 253 the ERA5 adopted the bulk aerodynamic method used by the ECMWF, and the 254 MERRA2 used the method by the GEOS. These products provide SHF and LHF estimates at a 0.25° spatial resolution, except for the MERRA2 (0.5°×0.625°) and 255 256 OAFlux (1°). Additionally, most products provide daily SHF and LHF estimates, while 257 only the OHF product provide estimates at a 3-hour interval. For further inter-258 comparison, the daily mean aggregation was applied to the OHF products. More details 259 about the seven products can be found in the review of Tang et al. (2024).





# 260 Table 1 Summary of forcing datasets used in this study

Dataset source	Resolution	Variables	Urls
		Sea surface air temperature $(T_a)$ , sea surface air	
	0 7 50/1 -: 1	specific humidity ( $Q_a$ ), mean sea level pressure	https://cds.climate.copernicus.eu/datasets/derived-era5-single-levels-
ENAJ	0.20 /uany	(SLP), downward long wave radiation flux $(LW)$	daily-statistics?tab=overview
		and downward short wave radiation flux (SW)	
OSCAR	0.25°/daily	Ocean mixed layer current velocity (CS)	https://podaac.jpl.nasa.gov/dataset/OSCAR_L4_OC_FINAL_V2.0
CCMP	0.25°/6-hour	Wind speed (WS)	https://data.remss.com/ccmp/v03.0/daily/
MOCOCD	0 1050/4-1-	Sea surface salinity (SSS) and sea surface	https://data.marine.copernicus.eu/product/MULTIOBS_GLO_PHY
MODOD	0.123 /uany	density (SSD),	S SURFACE MYNRT 015 013/description
CCII	0 7 50/20:10	Absolute dynamic topography (ADT) and sea	https://data.marine.copernicus.eu/product/SEALEVEL GLO PHY
лее	0.20 /uany	level anomaly (SLA)	CLIMATE L4 MY 008 057/description
COW	0 70/2 4000	Significant wave height (SWH) and wave period	https://data.marine.copernicus.eu/product/GLOBAL_MULTIYEAR_
00%		$(T_p)$	WAV 001 032/description
OICCT	0 7 50/20:10	Sea surface temperature $(T_s)$ and sea surface	https://www.ncei.noaa.gov/data/sea-surface-temperature-optimum-
U O O I	0.20 /uany	specific humidity $(\hat{Q}_s)$	interpolation/v2.1/access/avhrr/
OISCT - EP AS	0 750/daily	Gradient of temperature $(diff_T)$ and gradient of	
	0.20 / daily	humidity $(diff_{\hat{Q}})$	

261 262





263	Table 2 Summary of	of the state-of-the-art ai	r-sea turbulent heat	fluxes products used fo	r inter-comparison in this study
	Dataset source	Resolution	Model	Variables	Urls
	JOFURO3	0.25°/daily	COARE3.0		https://www.j-ofuro.com/en/
	IFREMER	0.25°/daily	COARE3.0		<u>ftp://ftp.ifremer.fr/ifremer/cersat/data/heat-flux/ifremer/v4.1/daily</u>
	SeaFlux	0.25°/daily	COARE3.5		https://www.earthdata.nasa.gov/data/catalog/ghrc-daac-seaflux-1
				Latent heat flux	https://developers.google.com/earth-
	MERRA2	$0.5^{\circ}  imes 0.625^{\circ}$ /daily	GEOS	(LHF), sensible	engine/datasets/catalog/NASA GSFC MERRA flx 2?hl=zh-
				heat flux (SHF) and	<u>cn#bands</u>
		n nco/dailer	ECIVITYE	Bowen ratio ( $\beta =$	https://cds.climate.copernicus.eu/datasets/derived-era5-single-levels-
	ENAD	0.20 / uaity		SHF/LHF)	daily-statistics?tab=overview
	OAFlux	1°/daily	COARE3.0		<u>ftp://ftp.whoi.edu/pub/science/oaflux/data_v3</u>
	OHE	0 750/2 hour	Neural Network		https://www.ncei.noaa.gov/products/climate-data-records/ocean-heat-
	OIII	0.2 <i>3</i> /3-11001	model		fluxes
264					





### 265 2.3 Construction of the BrTHF model

### 266 **2.3.1 Feature selection**

267 The study employed a random forest (RF) model to evaluate the importance scores 268 of 17 oceanic and atmospheric forcing variables (with datasets collected in Section 2.2) 269 for target variables (SHF and LHF), aiming to filter out less influential variables. As 270 shown in Table S2, the variable importance assessment revealed that  $diff_T$  and  $diff_O$ 271 showed the highest importance score (71.56% and 49.93%) for SHF and LHF 272 modelling, respectively; additionally, WS exhibited the second highest importance for 273 both SHF (10.19%) and LHF (27.59%) modelling. Building upon the importance 274 evaluation and through careful screening of highly correlated variables, we ultimately 275 selected 11 key environmental features for subsequent air-sea turbulent heat fluxes 276 modelling including SLP, LW, SW, SSS, ADT, CS, WS, SWH, T<sub>p</sub>, diff<sub>Q</sub>, and diff<sub>T</sub>.

### 277 2.3.1 Model construction and optimization

We selected the NN technique to build the BrTHF model due to its strong ability to capture the complex nonlinear relationships between the multiple-inputs and multiple-target variables with high accuracy (Zhou et al., 2024; Fu et al., 2023; Cummins et al., 2023; Cummins et al., 2024). Additionally, the technique enables the seamless integration of physical constraints, improving the reasonableness of the results (Zhou et al., 2024; Zhao et al., 2019; Shang et al., 2023).

In order to estimate the SHF and LHF with high accuracy in a physics-consistency framework, the  $\beta$  (= SHF/LHF) physical constraint was incorporated into the NN model using the customed multiple-objects (SHF, LHF and  $\beta$ ) loss function as follows:

$$287 \qquad Loss = a \times Loss_{SHF} + b \times Loss_{IHF} + c \times Loss_{\beta} \tag{2}$$

*Loss<sub>SHF</sub>*, *Loss<sub>LHF</sub>* and *Loss*<sup> $\beta$ </sup> represent the Mean Squared Error (MSE) of SHF, LHF and  $\beta$ , respectively. They were weighted using the factors of a (SHF), b (LHF) and c ( $\beta$ ) to balance the different magnitudes of loss during optimization. To prevent potential gradient explosion during model training, predicted  $\beta$  [SHF'/LHF', calculated using the predicted SHF (SHF') and LHF (LHF')] values were clipped within the observed range





293 of  $\beta$  (from -5 to 5) during training:

294 
$$CLIP(\frac{SHF'}{LHF'}) = \begin{cases} Min(\frac{SHF'}{LHF'}, 5) & \frac{SHF'}{LHF'} > 0\\ Max(\frac{SHF'}{LHF'}, -5) & \frac{SHF'}{LHF'} < 0 \end{cases}$$
(3)

295 
$$Loss_{\beta} = MSE(\frac{SHF}{LHF}, CLIP(\frac{SHF'}{LHF'}))$$
 (4)

Finally, after optimization, the final weights (a, b and c) for SHF, LHF, and  $\beta$  were set to 5, 1, and 250, respectively. The model was constructed consisting of one input layer, three hidden layers, two BatchNormalization layers, and one output layer using the Python TensorFlow library. The number of neurons in the three hidden layers were 32, 64, and 16, respectively and the activation function of Leaky Rectified linear unit (ReLU) was used throughout the model.

To illustrate the superiority of the BrTHF model in terms of accuracy and physical consistency, another physics-free NN models, trained without integrating the  $\beta$ constraint, were also constructed to predict SHF and LHF separately for further comparison, where  $\beta$  was calculated to be SHF/LHF.

### 306 2.4 Evaluation strategy

307 A spatial 10-fold cross-validation was employed to assess the performances of the 308 BrTHF model for estimating air-sea SHF, LHF and  $\beta$ . Compared to the traditional 10-309 fold cross-validation, which randomly split all samples into ten folds and thus may 310 result in overlapping spatial samples between training and validating datasets, the 311 spatial 10-fold cross-validation were conducted in a relatively independent spatial 312 distribution and can provide a more generalized and convincing evaluation.

313 Specifically, first, all buoy sites were randomly split into ten folds. Then, each fold
314 was in succession selected as the validation dataset and the rest of ten folds was used
315 as the training dataset.

The metrics used to evaluate the performance of the models include: (1) the mean bias error (BIAS); (2) the root mean squared error (RMSE); (3) the correlation coefficient (r):





319 
$$BIAS = \frac{1}{n} \sum_{i=1}^{n} (\hat{y}_i - y_i)$$
(5)

320 
$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} \left( \hat{y}_i - y_i \right)^2}$$
(6)

321 
$$r = \frac{\sum_{i=1}^{n} [(\hat{y}_i - \overline{\hat{y}})(y_i - \overline{y})]}{\sqrt{\sum_{i=1}^{n} (\hat{y}_i - \overline{\hat{y}})^2 \sum_{i=1}^{n} (y_i - \overline{y})^2}}$$
(7)

322 where *n* is the number of samples,  $\hat{y}_i$  and  $y_i$  are the estimated value and reference

- 323 truth,  $\overline{\hat{y}}$  and  $\overline{y}$  are the mean of  $\hat{y}_i$  and  $y_i$ , respectively.
- 324

### 325 3. Results and discussion

### 326 **3.1 Spatial ten-fold cross-validation of the models**

### 327 3.1.1 Overall accuracy

Figures 3, 4 and 5 present the normalized scatter density plots of the estimated daily SHF, LHF and  $\beta$  from the BrTHF and physics-free NN models, as well as the seven air-sea turbulent heat fluxes products against the observations obtained from 197 global distributed buoys by the spatial ten-fold cross-validation strategy.

332 Most models and products showed data distributions closely aligned with the 333 observed SHF, with the majority of samples clustered around the 1:1 line. The BrTHF 334 model slightly overestimated SHF with a BIAS of 0.09 W/m<sup>2</sup>, whereas the physics-free 335 NN models, ERA5 and IFREMER products showed more pronounced overestimations 336 (from 0.42 W/m<sup>2</sup> to 4.05 W/m<sup>2</sup>). In contrast, the rest five products exhibited notable underestimations (from -3.44 W/m<sup>2</sup> to -0.41 W/m<sup>2</sup>). As illustrated in Figure 6, the 337 338 variability of estimated SHF from the BrTHF and the physics-free NN models and 339 ERA5 product closely matched the observed SHF, all with a Standard Deviation (STD) of approximately 16 W/m<sup>2</sup>. Notably, the BrTHF model achieved the lowest RMSE 340  $(6.05 \text{ W/m}^2)$ , outperforming both the physics-free NN models (6.29 W/m<sup>2</sup>) and the 341 seven air-sea turbulent heat flux products (ranging up to 12.34 W/m<sup>2</sup> for OHF). 342 343 Additionally, the BrTHF model combined with the physics-free NN models yielded the 344 highest values of r (0.93), surpassing all seven other products. In summary, the BrTHF





- 345 model showed overall the best performance in estimating SHF among all the models
- and products.





Figure 3. Normalized scatter density plots of estimated SHF from the BrTHF model, the
physics-free NN models and seven air-sea turbulent heat fluxes products against the observed
SHF obtained from 197 global distributed buoys.

For LHF, similar to the results for SHF, the BrTHF model also demonstrated the best agreement with observations, achieving the lowest RMSE (23.67 W/m<sup>2</sup>) and the highest value of r (0.91). Compared to the physics-free NN models and seven products, the BrTHF model reduced RMSE by 2.05 W/m<sup>2</sup> (physics-free NN models) to 12.38 W/m<sup>2</sup> (OHF) and improved r by 0.01 (physics-free NN model) to 0.1 (OHF).





Additionally, the BrTHF model showed a slight overestimation of LHF (BIAS = 0.14  $W/m^2$ ), lower than that of the SeaFlux, MERRA2, and ERA5 products. In contrast, the remaining products (JOFURO3, IFREMER, OAFlux, and OHF), along with the physics-free NN models, underestimated LHF, with the BIAS values ranging from - 10.19  $W/m^2$  (OHF) to -1.61  $W/m^2$  (JOFURO3).



361

362 Figure 4. Same as Figure 3 but for LHF.

The BrTHF model exhibited a significantly different distribution of  $\beta$  compared to the physics-free NN models and the seven products, as shown in Figure 5. The  $\beta$ estimates from the BrTHF model consistently fell within the observed range of -5 to 5, while the physics-free NN model and the seven products occasionally produced





367	estimates outside this range. Specifically, approximately 0.9% of $\beta$ estimates from both
368	the physics-free NN model and the seven products were out of range. The extreme
369	positive and negative $\beta$ estimates were found in the OHF ( $\beta = 14997$ ) and physics-free
370	NN models ( $\beta$ = -25703) products, respectively. The abnormal $\beta$ estimates significantly
371	impacted the accuracy of the physics-free NN models and the seven products as Figure
372	6 indicated. When excluding the abnormal $\beta$ samples from the physics-free NN models
373	and seven products, the RMSEs ranged from 0.17 (physics-free NN models and
374	SeaFlux) and 0.26 (OHF), with values of r ranging from 0.13 (OHF) to 0.46 $$
375	(IFREMER), as shown in Figure 6 and Table S3. However, when all estimates were
376	considered, the performances of these model and products deteriorated sharply, with
377	RMSEs rising from 0.87 (SeaFlux) to 39.21 (physics-free NN models), and values of r
378	dropping from 0.06 (SeaFlux) to 0 (JOFURO3, MERRA2 and OHF). In contrast, the
379	BrTHF model maintained robust outperformance, with the lowest RMSEs of 0.22 and
380	0.15, and higher r values of 0.25 and 0.43, both before and after removing the abnormal
381	$\beta$ samples from the physics-free NN models and the seven products. Notably, the BIAS
382	values remained stable (ranging from -0.04 to 0.04) for all models and products,
383	regardless of whether the abnormal samples were excluded.







384

Figure 5. Same as figure 3 but for β. The samples out of the ranges of observed β (-5 ≤ β ≤ -5)
were colored in blue, orange, green, red, purple, brown, pink and gray for JOFURO3,
IFRMER, SeaFlux, ERA5, MERRA2, OAFlux, OHF products and the physics-free NN models,
respectively.







389

Figure 6. Taylor diagrams of the validation of estimated daily SHF (a), LHF (b),  $\beta$  (c) and  $\beta$  (-391  $5 \le \beta \le 5$ , d) from the BrTHF model, the physics-free NN models and the seven products against 392 the in-situ observations.

393

### 394 3.1.2 Accuracies across oceans

To better understand the accuracy of SHF, LHF and  $\beta$  estimates from the BrTHF and physics-free NN models, as well as the seven products in different oceans, we conducted an additional evaluation by categorizing the observations according to the belonging ocean basins, as shown in Figure 7. The major ocean boundaries, obtained from Marine Regions (https://www.marineregions.org/), were used to define the ocean





- 400 basins, which include the Arctic Ocean, South Pacific Ocean, North Pacific Ocean,
- 401 South Atlantic Ocean, North Atlantic Ocean, and Indian Ocean.
- 402 For SHF, the BrTHF model exhibited overestimations in the South Pacific Ocean, North Atlantic Ocean, and Indian Ocean, while it underestimated SHF in the remaining 403 three ocean basins. The values of BIAS ranged from -4.57 W/m<sup>2</sup> in the Arctic Ocean to 404 0.49 W/m<sup>2</sup> in the North Atlantic Ocean. Furthermore, the BrTHF achieved the lowest 405 RMSEs in most ocean basins, ranging from 3.84 W/m<sup>2</sup> in the South Atlantic Ocean to 406 7.72 W/m<sup>2</sup> in the North Atlantic Ocean, except in the Arctic Ocean where the RMSE of 407 13.59 W/m<sup>2</sup> were higher than those of the ERA5 (12.5 W/m<sup>2</sup>) and MERRA2 (13.46 408 409 W/m<sup>2</sup>) products, as shown in Figure 7(b). Correlation analysis also demonstrated the 410 robust performance of the BrTHF model in estimating SHF, with values of r exceeding 411 0.89 in most ocean basins, except those ocean basins in the South Hemisphere (ranging from 0.71 to 0.79) where the values of r for all models and products reduced. 412

413 For LHF, the values of BIAS of the BrTHF model ranged from -4.15 W/m<sup>2</sup> in the Arctic Ocean to 1.19 W/m<sup>2</sup> in the North Pacific Ocean. In comparison, the BrTHF 414 415 model showed more pronounced underestimations in the Arctic Ocean and Indian 416 Ocean. Additionally, the BrTHF model outperformed the physics-free NN models and 417 the seven products across most ocean basins, achieving the lowest RMSEs (ranging 418 from 17.06 W/m<sup>2</sup> in the Arctic Ocean to 28.20 W/m<sup>2</sup> in the North Atlantic Ocean) and 419 the highest values of r (ranging from 0.83 in the Indian Ocean to 0.94 in the North 420 Atlantic Ocean) except for the Arctic Ocean where the value of r was 0.01 less than the physics-free NN models and the RMSE were 2.45 W/m<sup>2</sup>, 3.25 W/m<sup>2</sup> and 1.84 W/m<sup>2</sup> 421 higher than the ERA5 and MERRA2 products and the physics-free NN models, 422 423 respectively.

The BrTHF model consistently performed better in estimating  $\beta$  across most ocean basins, both before and after removing the abnormal  $\beta$  samples that deviated from the observed range (-5  $\leq \beta \leq$  5). In contrast, the physics-free NN models and the seven products did not perform as well. Specifically, the BrTHF model exhibited the lowest





- 428 RMSEs in almost all ocean basins except in the South Atlantic Ocean after removing  $\beta$
- 429 outliers. Moreover, in terms of correlation analysis, the BrTHF model achieved higher
- 430 values of r in most ocean basins before and after the removal of abnormal  $\beta$  samples,
- 431 among all models and products.





Figure 7. Heatmaps of BIAS, RMSE and r metrics for the validation of estimated daily SHF (a - c), LHF (b - e),  $\beta$  (f - i) and  $\beta$  (-5  $\leq \beta \leq$  5, j - l) from the BrTHF model, the physics-free NN models and the seven products against the in-situ observations across different ocean basins.





### 437 **3.2** Temporal variations in SHF, LHF and $\beta$

After spatial ten-fold cross-validation, we produced the daily  $0.25^{\circ}$  global air-sea turbulent heat fluxes products from 1993 to 2017 using a combination of the BrTHF model and forcing datasets, and further made a comparison of the temporal variation (in this section), spatial distribution (in Section 3.3) and annual trend (in Section 3.4) of SHF, LHF and  $\beta$  estimates from the BrTHF product and those with the seven stateof-the-art global products. The selected period (from 1993 to 2017) was determined by the overlapping availability of input forcing datasets.

445 Figure 8 illustrates the monthly area-weighted global means of SHF, LHF and  $\beta$ 446 from 1993 to 2017 for the BrTHF product and seven state-of-the-art products. The 447 BrTHF product exhibited similar bimodal patterns for SHF, LHF and  $\beta$  as the seven products, with peaks in December-January and May-June-July-August. However, the 448 449 peak in May-June-July-August was less pronounced for SHF and  $\beta$  compared to that 450 for LHF. The monthly area-weighted global means of SHF and  $\beta$  from the BrTHF 451 product were higher than those of most products, except for the MERRA2 product in 452 January, February, March, April, July, August and September, and the IFREMER 453 product in all months. For LHF, the BrTHF showed lower values than the ERA5 and 454 MERRA2 products across all months. Notably, the patterns of SHF and  $\beta$  from the OHF 455 product, with the highest peak occurring in August and smoother intra-annual cycles, 456 differed from those of the corresponding BrTHF product and the other six products 457 developed using the bulk aerodynamic methods.







458

## 459 Figure 8. Intra-annual cycles of area-weighted global monthly mean of SHF (a), LHF (b) and 460 $\beta$ (c) from the eight products from 1993 to 2017.

461 Figure 9 presents the temporal evolution of the area-weighted annual global mean of SHF, LHF and  $\beta$  from 1993 to 2017 for the eight products for the ice-free oceans. 462 The global mean annual SHF of the BrTHF product was 12.7 W/m<sup>2</sup>, which was close 463 to those of SeaFlux (11.6 W/m<sup>2</sup>), OAFlux (10.6 W/m<sup>2</sup>), MERRA2 (13 W/m<sup>2</sup>) and 464 465 ERA5 (12.4 W/m<sup>2</sup>), whereas significantly lower than that of IFREMER (18.8 W/m<sup>2</sup>) and higher than those of JOFURO3 (7.5 W/m<sup>2</sup>) and OHF (5.6 W/m<sup>2</sup>). Meanwhile, the 466 BrTHF product exhibited significant largest growth of SHF with the trend of 0.04 467 468 W/(m<sup>2</sup>·year) among all eight products, and showed similar temporal evolution as 469 SeaFlux, MERRA2, ERA5 and OAFlux during the period from 1993 to 2017. As for LHF, the BrTHF exhibited a larger global mean annual value of 106.2 W/m<sup>2</sup>, which 470 471 was close to those of the ERA5(107.3 W/m<sup>2</sup>) and MERRA2 (108.3 W/m<sup>2</sup>), and it was 472 significantly higher than the rest five products. Moreover, the growth of the BrTHF LHF was significant with a trend of 0.33 W/( $m^2$ ·year), which was lower than the 473





474 IFREMER but higher than the OAFlux, MERRA2, OHF, ERA5, JOFURO3 and SeaFlux, ranging from -0.14 W/(m<sup>2</sup>·year) to 0.4 W/(m<sup>2</sup>·year). Note that only the 475 476 OAFlux product showed negative trend of LHF from 1993 to 2017. For  $\beta$ , the BrTHF showed a similar temporal pattern to that of SHF, and most products concentrated 477 within the narrow range of 0.11 to 0.12 for the annual values. The magnitude of annual 478 479  $\beta$  of the BrTHF was about 0.11, which was close to the OAFlux, SeaFlux, MERRA2 480 and ERA5, but significantly lower than the IFREMER and higher than the JOFURO3 481 and OHF. Moreover, in contrast to the significant increasing trends of LHF and SHF, 482 negative of trends of  $\beta$  were shown for most products. However, the BrTHF product 483 exhibited a weak positive trend.



484

Figure 9. Inter-annual evolution of area-weighted global mean SHF (a - b), LHF (c - d) and  $\beta$ (e - f) from 1993 to 2017. The trends were calculated based on the Sen's slope method. The \* in the sub-figures (b, d and f) represent the trend passed the Mann-Kendall significant test (p <0.05).

489





### 490 **3.3 Inter-comparison of the spatial pattern**

We selected three representative products including the (reanalysis-based) ERA5, (remote sensing-based) SeaFlux, and (the only publicly available machine learningbased) OHF products to evaluate the BrTHF product's ability in simulating global airsea turbulent heat fluxes (SHF, LHF, and  $\beta$ ) from 1993 to 2017. These products were chosen because they demonstrated relatively high accuracy within their respective categories (as shown in Section 3.1) and shared the same 0.25° spatial resolution with the BrTHF product.

498 Figure 10 presents the spatial distribution of multi-year mean of SHF from the 499 SeaFlux, ERA5, BrTHF, and OHF products, along with their cross-comparisons. 500 Overall, the BrTHF product exhibited strong consistency with ERA5 and SeaFlux 501 products, with values of r exceeding 0.88, which was significantly higher than the 502 consistency between SeaFlux and OHF (r = 0.33) and between ERA5 and OHF (r =503 0.37). Spatially, the BrTHF, SeaFlux and ERA5 products all showed higher SHF (over 50 W/m<sup>2</sup>) in the Western Boundary Currents (WBCs, e.g. Kuroshio, Gulf Stream, Brazil 504 505 Current and Agulhas Current) regions, whereas OHF product yielded much lower SHF (~25 W/m<sup>2</sup>). Additionally, the former three products captured pronounced SHF 506 507 gradients in the Southern Ocean, features that were absent in OHF product. SHF 508 differences between BrTHF and SeaFlux/ERA5 remained within  $\pm 10$  W/m<sup>2</sup> in most 509 oceans. The BrTHF product exhibited slightly higher SHF values than SeaFlux in the 510 Northern Hemisphere, whereas in the Southern Hemisphere-particularly over the 511 Southern Ocean-the BrTHF showed relatively lower SHF. Compared to the ERA5 product, the BrTHF product yielded lower SHF in the equatorial zone, subtropical high-512 513 pressure regions and the Southern Ocean, but higher SHF in other areas, particularly in 514 the North Pacific and the southern Indian Ocean.









516 Figure 10. Inter-comparison of the spatial distributions of multi-year means of SHF among

517 the SeaFlux, ERA5, OHF and BrTHF products from 1993 to 2017.

518 For LHF, the BrTHF and the selected three products exhibited more close spatial 519 distribution patterns, with the values of r exceeding 0.98, compared to the results for the SHF, as shown in Figure 11. The higher LHF (over 150 W/m<sup>2</sup>) primarily occurred 520 around the regions of WBCs and the sub-tropic highs, while lower LHF (below 50 521 522 W/m<sup>2</sup>) appeared in the Eastern Equatorial Pacific and Atlantic Warm Tongue and the 523 oceans with latitudes higher than 45°. The spatial distribution of LHF in the BrTHF 524 product generally agreed better with that of the ERA5 product, though the BrTHF 525 showed significantly lower LHF in sub-tropic highs. Additionally, the BrTHF exhibited 526 relatively lower LHF than the ERA5 over the Southern Ocean and the central North 527 Atlantic. Compared to the SeaFlux, the BrTHF yielded slightly higher LHF in most 528 oceans except the Southern Ocean and equatorial zones.









### 530 Figure 11. Same as Figure 10 but for LHF.

531 For  $\beta$ , the BrTHF product demonstrated strong spatial correlation with the ERA5 532 and SeaFlux in multi-year mean distributions, with values of r exceeding 0.81. In 533 contrast, the OHF showed markedly a different spatial pattern of  $\beta$ , exhibiting negative 534 correlations when compared to the rest of three products. Spatially, the BrTHF product's 535  $\beta$  distribution aligned more closely with the SeaFlux, both displaying higher  $\beta$  (up to 1) 536 in high-latitude oceans particularly in the Northern Hemisphere and the similar 537 wavelike textures of  $\beta$  over the Southern Ocean's Antarctic Circumpolar Current zone. 538 The differences between the BrTHF and OHF products were more evident. Specifically, 539 the BrTHF product showed overall overestimation of  $\beta$  in the oceans where latitudes 540 were larger than 45° compared to the OHF product.







542 Figure 12. Same as Figure 10 but for  $\beta$ .

543

541

### 544 3.4 Spatial pattern of trends in SHF, LHF and $\beta$ from the BrTHF product

545 Figure 13 illustrates the spatial distribution of inter-annual trends of SHF, LHF and  $\beta$  in the BrTHF product from 1993 to 2017. The SHF showed increasing trends across 546 547 71.4% of the oceans, with statistically significant increases in 26.2% of regions. In 548 contrast, decreasing trends were observed in 28.6% of the oceans, with only 3% 549 showing significant reductions. Overall, the trends of zonal annual averages of SHF 550 remained stable between the 60°N to 45°S, with significant increases occurring 551 southward and decreases northward. Specifically, moderate increases (~0.2 W/(m<sup>2</sup> 552 year)) dominated between 45°N and 45°S, while more pronounced increases (>0.8 553  $W/(m^2 \text{ year}))$  were observed in high-latitude oceans, including the Kara Sea, Gulf 554 Stream, Baffin Bay, Brazil Current, Sea of Okhotsk, and Sea of Japan. Notable decreases (< -0.8 W/(m<sup>2</sup> year)) were concentrated in the Barents Sea and the central 555 556 North Atlantic.

# The LHF exhibited markedly different characteristics of the spatial distribution, with 87.5% of oceans showing increasing trends (38.9% were significant), versus 12.5% decreasing (0.7% were significant). In contrast to those of the SHF, the trends of zonal





- annual averages for LHF weakened poleward from the oceans of Equator. The
  substantial increases (>0.6 W/m<sup>2</sup>/year) occurred in the oceans between 45°N to 45°S,
  particularly in the Gulf Stream, Brazil Current, and Agulhas Current systems, while
  notable decreases (lower than -0.3 W/m<sup>2</sup>/year) were observed in the central North
  Atlantic and Kuroshio extension regions.
- For  $\beta$ , approximately 53% of the oceans showed increasing trends, with 12.2% of these being statistically significant. Conversely, about 47% of the oceans showed decreasing trends, with 9.8% being significant. Most oceans between 45°N to 45°S exhibited near-zero trends, while significant trends were concentrated in the highlatitude oceans. Notable increases were found in Baffin Bay, Kara Sea, and the Southern Ocean, while decreases were observed in the Barents Sea and the Southern Ocean near South America.



572

573 Figure 13. Spatial maps of inter-annual trends for SHF (a), LHF (c), and  $\beta$  (e) from the BrTHF 574 product for the period 1993 to 2017. The trends were calculated using the Sen's slope method. 575 Dotted areas indicate oceans where the p-value of the Mann-Kendall significance test is less 576 than 0.05. Panels (b), (d) and (f) represent the inter-annual trends of zonal annual averages 577 for SHF, LHF and  $\beta$ , respectively.



### 578 **3.5 Discussion**

579 Advancing our understanding of the air-sea interaction and achieving the global 580 closure of the ocean surface energy budget require accurate global-scale simulations of 581 air-sea turbulent heat fluxes (Yu, 2019). Existing global air-sea turbulent heat fluxes 582 products, primarily generated using the semi-empirical bulk aerodynamic methods and 583 data-driven machine learning approach, are often weak in accuracy and physical 584 rationality, arising from uncertainties in environmental forcings and inappropriate 585 parameterizations (Brodeau et al., 2017; Jiang et al., 2024a; Wang et al., 2024). To 586 improve the simulation of the global air-sea turbulent heat fluxes, this study presents the BrTHF product, generated using a Bowen ratio-constrained NN technique with a 587 588 customed multiple-objective loss function, as well as observations from 197 globally 589 distributed buoys along with multi-source remote sensing and reanalysis forcings.

590 The primary advantage of the BrTHF product is the absence of outliers in the 591 estimation of  $\beta$ . Unlike the approach of our previous study (Wang et al., 2024), which 592 simultaneously predicted SHF, LHF and  $\beta$  in the constructed RF model, this study 593 employed an NN model constrained by the Bowen ratio to jointly estimate SHF and 594 LHF. The new approach avoided the issue of selection of  $\beta$  derived from either the 595 calculated  $\beta \left[\beta_{cal}\right]$  equals predicted SHF (SHF<sub>pre</sub>) divided by predicted LHF (LHF<sub>pre</sub>)] or 596 the predicted  $\beta$  ( $\beta_{pre}$ ), as reported by Wang et al. (2024). Furthermore, the customed loss 597 function in our new approach provides a flexible approach to adjust the weights of SHF, 598 LHF, and  $\beta$ , allowing the model to balance attention among these variables. As a result, 599 the accuracy of SHF, LHF, and  $\beta$  from our newly developed BrTHF model 600 outperformed that of the mainstream air-sea turbulent heat fluxes products and the 601 physics-free NN models on both global and regional scales. In contrast, the accuracy of 602 SHF and LHF in the model constructed by Wang et al. (2024) was somewhat marginally 603 lower than that of the physics-free RF model.

604The machine learning-based OHF product demonstrated significantly poorer605performance in estimating SHF and LHF, with higher RMSEs and lower values of r, as





606 shown in Figure 6, compared to the remote sensing-, reanalysis-, and hybrid-based 607 products developed using the bulk aerodynamic methods. This finding contrasted with 608 the results of Tang et al. (2024), who reported the superior performance of the OHF 609 product. The discrepancy could primarily be attributed to the different spatial 610 representativeness of the observation datasets used by Tang et al. (2024), which were primarily collected from the buoys between 30°N and 30°S. Moreover, as shown in 611 612 Figure 7, the accuracy of the OHF product degraded notably in high-latitude ocean 613 basins, particularly in the North Atlantic Ocean. This accuracy degradation may be due 614 to the limitation of the observation datasets used to train the model of the OHF product, where different sources of datasets were integrated, i.e. the SeaFlux in-situ dataset 615 616 (before 2007) and the ICOADS in-situ dataset (after 2007). Specially, the ICOADS in-617 situ datasets, commonly used for developing products at monthly or lower frequency scales (Berry and Kent, 2011; Gulev et al., 2013), suffered from sparse distribution and 618 619 insufficient volume for developing the original 3-hour OHF product. Besides, the model 620 of the OHF product was trained by randomly splitting all observations into training, 621 validation, and test sets, which likely resulted in data dependencies across these sets, 622 weakening the model's transferability. These problems together contributed to the 623 poorer performance of the OHF product, including worse accuracy, overall negative 624 spatial trends in high-latitude oceans such as the Southern Ocean, as Tang et al. (2024) 625 reported, and an overall underestimation of the multi-year mean, especially in the 626 Western Boundary Currents (WBCs) where the air-sea exchange is intense.

The BrTHF product also has some limitations. First, due to the lack of an explicitly defined reasonable range for daily  $\beta$ , the constraint of  $\beta$  used in this study was derived from the daily  $\beta$  global distribution in the seven widely used global products. Although the results demonstrated significant improvements in the accuracy and physical consistency of SHF, LHF, and  $\beta$  estimates from the BrTHF model compared to those from the physics-free NN models and the seven products, there remains room for improvement once a more reasonable range for daily  $\beta$  is established. Secondly, the





634 estimated SHF and LHF values exhibited a narrower distribution compared to the 635 observations. This issue possibly stems from the uncertainty of the BrTHF model that 636 was constructed from the uneven distribution of SHF and LHF in the observation 637 datasets, which contain a low proportion of extreme samples, especially negative LHF 638 values. Moreover, due to the insufficient observations, validation in high-latitude 639 oceans, especially in the Southern Ocean, was limited. To address these problems, more 640 experiments are highly recommended to collect observations covering more regions of 641 oceans with better spatial and temporal representativeness, which could further enhance 642 the product.

643 The BrTHF model demonstrated the feasibility and potential of jointly estimating 644 multiple interrelated air-sea variables through a machine learning model that 645 incorporates appropriate physical constraints to account for their interrelations. In the future, the predicted variables in the BrTHF model could be expanded to include 646 647 surface radiation, heat storage, and precipitation over the ocean, by integrating the 648 physical mechanisms of energy and water exchange. This would allow for the 649 collaborative optimization of estimates across all components of the air-sea energy and 650 water budgets, potentially contributing to achieving global closure of the air-sea energy 651 and water budgets.

652

### 653 4. Data and code availability

654 The daily 0.25° BrTHF product, consisting of SHF and LHF estimates from 1993 to 2017, can be freely accessed from the National Tibetan Plateau Data Center (TPDC) 655 [https://doi.org/10.11888/Atmos.tpdc.302578, Tang and Wang (2025)]. The code for 656 657 developing the product can be found on the GitHub platform 658 (https://github.com/zhezhe1996/BrTHF).

659

### 660 5. Summary and Conclusion

661 In this study, we generated a daily 0.25° air-sea turbulent heat fluxes product for

34





the period 1993 to 2017 using our developed BrTHF model and multi-source remote sensing and reanalysis data. A comprehensive validation was performed against observations from 197 buoys and inter-comparisons were made with seven representative gridded products. The key findings are as follows:

666 The BrTHF model demonstrated superior accuracy in estimating SHF, LHF and  $\beta$ 667 compared to the physics-free NN models and the seven widely used air-sea turbulent 668 heat products (including the JOFURO3, IFREMER, SeaFlux, ERA5, MERRA2, 669 OAFlux and OHF products). Through the spatial ten-fold cross-validation against the observations from the 197 buoys, the BrTHF model achieved RMSEs of 6.05 W/m<sup>2</sup> for 670 671 SHF, 23.67 W/m<sup>2</sup> for LHF and 0.22 for  $\beta$ , and showed values of r of 0.93, 0.91, and 672 0.25 for SHF, LHF, and  $\beta$ , respectively. Additionally, The BrTHF model performed 673 better in evaluations across six major ocean basins, with lower RMSEs and higher values of r, in comparison to the physics-free NN models and the seven products. 674 675 Notably, the BrTHF model significantly improved the rationality of  $\beta$  estimates, successfully eliminating the outliers observed in both the physics-free NN models and 676 the seven products. Furthermore, the global distributions for SHF, LHF, and  $\beta$  from the 677 678 BrTHF product closely matched those of the physically-based ERA5 and SeaFlux 679 products. The global mean annual estimates of SHF, LHF, and  $\beta$  from the BrTHF 680 product from 1993 to 2017 were 12.7 W/m<sup>2</sup>, 106.2 W/m<sup>2</sup> and 0.11, respectively, all 681 within the ranges of the seven products. The BrTHF product exhibited similar intra-682 annual cycles for SHF, LHF and  $\beta$ , with bimodal patterns featuring lower and higher 683 peaks in May-June-July-August and December-January, respectively, which was consistent with the results of the seven state-of-the-art products. Additionally, the 684 685 BrTHF product exhibited significant increasing trends for global SHF and LHF, with rates of 0.04 W/(m<sup>2</sup> year) and 0.33 W/(m<sup>2</sup> year), respectively, which were consistent to 686 687 most of the seven products. In contrast, the BrTHF product displayed weak growth in 688  $\beta$ , with a trend approaching 0, which were opposite to the results of the seven products 689 except for the MERRA2 product. The increasing (significant increasing) trends





- 690 dominated the oceans, with areas of 71.4% (26.2%) for SHF, 87.5% (38.9%) for LHF,
- 691 53% (12.2%) for  $\beta$  in the BrTHF product.

The BrTHF product shows significant advantages in the accuracy and rationality of estimates for key parameters (SHF, LHF, and  $\beta$ ) related to air-sea interaction and the global energy and water budgets compared to the existing products. It holds great potential for quantifying the global air-sea energy and water budgets, enhancing our understanding of the air-sea interaction, and projecting climate change under global warming.

### 698 Author contribution

YW and RT conceived the study and designed the experimental framework. YW
 performed the experiment and prepared the initial manuscript draft. All authors
 contributed to manuscript revision, and approved the final version of the manuscript.

### 702 **Competing interests**

The contact author has declared that none of the authors has any competing interests.

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