

A New-Generation Internal Tide Model Based on 30 Years of Satellite Sea Surface Height Measurements: Multiwave Decomposition and Isolated Beams

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Abstract. An internal tide model ZHAO30yr is developed using 30 years of satellite altimetry sea surface height (SSH) measurements from 1993 to 2022 by a recently improved mapping technique that consists of two rounds of plane wave analysis with a spatial bandpass filter in between. Prerequisite wavelengths are calculated using climatological annual-mean hydrographic profiles in the World Ocean Atlas 2018. ZHAO30yr only extracts the 30-year phase-locked internal tide component, lacking the incoherent component caused by the time-varying ocean environment. The model contains 12 internal tide constituents: 8 mode-1 constituents (M_2 , S_2 , N_2 , K_2 , K_1 , O_1 , P_1 , and Q_1) and 4 mode-2 constituents (M_2 , S_2 , K_1 , and O_1). Model errors are estimated to be lower than 1 mm in the SSH amplitude on a global average, thanks to the long data record and improved mapping technique. The model is evaluated by making internal tide correction to independent altimetry data in 2023. Ten constituents (but for K_2 and Q_1) can reduce variance on a global average. K_2 and Q_1 can only cause variance reductions in their source regions. The model decomposes the multiconstituent multimodal multidirectional internal tide field into a series of simple plane waves at each grid point. The decomposition reveals unprecedented features previously masked by multiwave interference. The model divides each internal tide constituent into components by propagation direction. The directionally-decomposed components show numerous long-range internal tidal beams associated with notable topographic features. The semidiurnal internal tidal beams off the Amazon shelf and the diurnal internal tidal beams in the Arabian Sea are examined in detail. ZHAO30yr is available at <http://doi.org/10.6084/m9.figshare.28078523> (Zhao, 2024b). Model errors are available at <https://doi.org/10.6084/m9.figshare.28559978.v3> (Zhao, 2025).

1 Introduction

Internal tides (internal gravity waves at tidal frequencies) are inherent wave motions in the interior of the stratified ocean (Wunsch, 1975; Munk and Wunsch, 1998; Garrett and Kunze, 2007). Internal tides are mainly generated by barotropic tidal currents flowing over variable topography (Egbert and Ray, 2000; Smith and Young, 2002; Nycander, 2005). They propagate over hundreds to thousands of km and redistribute the converted tidal energy in the open ocean (Ray and Mitchum, 1996; Alford, 2003; Zhao, 2014; MacKinnon et al., 2017). Internal tides gradually lose their coherence (phase locking) with the barotropic tidal forcing in long-range propagation through the time-varying ocean. Fortunately, a fraction of internal tides remain coherent and

thus detectable by multiyear time series from field moorings, acoustics thermometry, and satellite altimetry (Ray and Mitchum, 1996; Alford, 2003; Dushaw, 2022). In recent years, internal tides have drawn great research interest, because they play an important role in various ocean processes including tracer transport, acoustic transmission, coral bleaching, primary productivity, and ocean mixing (Jayne and St. Laurent, 2001; Colosi and Munk, 2006; Tuerena et al., 2019; Whalen et al., 2020; Zhang et al., 2021; Dushaw, 2022; Jacobsen et al., 2023; Guan et al., 2024). In particular, internal tides can be used for monitoring global ocean changes, in that their speed changes in long-range propagation contain important information on ocean stratification (Zhao, 2016). Internal tides may be unwanted noise in some researches and thus should be accurately corrected (Morrow et al., 2019; Yadidya et al., 2024). In the past decade, a few empirical internal tide models have been constructed from satellite altimetry (Ray and Zaron, 2016; Zhao et al., 2016; Zaron, 2019; Zhao, 2023b; Zaron and Elipot, 2024). On the other hand, internal tide models have been developed by numerical simulations driven by atmosphere forcing and tidal potential (Simmons et al., 2004; Müller et al., 2012; Shriver et al., 2012; Buijsman et al., 2017; Arbic et al., 2018; Li and von Storch, 2020; Arbic, 2022). Internal tide models can also be developed using semi-analytical methods (Nycander, 2005; Pollmann and Nycander, 2023; Geoffroy et al., 2025). In this paper, I will present a new internal tide model developed using 30 years of satellite altimetry sea surface height (SSH) measurements from 1993 to 2022.

Satellite altimetry observes internal tides via their small SSH fluctuations and thus provides a unique tool for mapping internal tides on a global scale. However, their weak SSH signals are usually overwhelmed by leaked mesoscale signals (mesoscale contamination), because the internal tide field is spatially and temporally under-sampled by satellite altimetry. Previous studies mainly focused on the large first baroclinic modes of M_2 , S_2 , K_1 , and O_1 constituents (Carrere et al., 2021). Previous internal tide models usually contain considerable errors, but none provide error estimates. The oceanographic community needs accurate and complete internal tide models in various researches such as quantifying coherent and incoherent internal tides, internal tide-induced ocean mixing, and internal tide-eddy interactions. These questions require a better knowledge of the global internal tide field. Previous advances are due mainly to the accumulation of multiyear multimission altimetry data, because the longer data record may lead to lower errors. Some recent altimetry missions (phases) are operated along nonrepeat tracks (Zhao, 2022a). For example, CryoSat-2 has a long repeat period of 369 days and samples the ocean along 10668 ground tracks (Wingham et al., 2006). Haiyang-2A has 386 ground tracks in its exact-repeat phase and 4630 ground tracks in its geodetic phase. The nonrepeat ground tracks greatly improve spatial resolution, because the denser ground tracks allow us to map internal tides in smaller fitting windows (Zhao, 2022a).

I have been improving my mapping technique over the past decade to construct better and better internal tide models (Zhao, 2021, 2022a, b, 2023b). My core technique is plane wave analysis that extracts waves in different horizontal directions. My mapping technique has been adapted to nonrepeat altimetry missions. Previous point-wise harmonic analysis cannot extract internal tides from nonrepeat altimetry missions, because the SSH time series at any given point is too short to extract reliable internal tides. The point-wise harmonic analysis employed in Zhao et al. (2016) has been replaced with plane wave analysis, and thus my improved mapping procedure calls plane wave analysis twice. The along-track one-dimensional bandpass filter in Zhao et al. (2016) has been replaced with spatial two-dimensional bandpass filter to extract internal tides having large angles with ground tracks. Thus, my new mapping technique consists of two rounds of plane wave analysis with a spatial

bandpass filter in between (Zhao, 2022a, b). It maps the internal tide field in three rounds of temporal and spatial filtering,
60 taking advantage of preknown tidal periods and wavelengths of the target internal tides.

This paper reports a new internal tide model developed by applying my improved mapping technique to 30 years of satellite altimetry data from 1993 to 2022. The new internal tide model is labeled ZHAO30yr. The model decomposes the internal tide field and thus reveals numerous long-range internal tidal beams. Note that it is important to resolve the multiwave interference pattern to correctly interpret in situ and satellite observations (Rainville et al., 2010). However, all previous internal tide models
65 give the multiwave summed internal tide fields and do not resolve internal tidal beams (Carrere et al., 2021). As shown in this paper, the decomposed internal tidal beams contain key information on their generation, propagation, and dissipation.

ZHAO30yr has the following outstanding features:

1. The model provides model errors that are estimated by background internal tides (Zhao, 2023b). The combination of long data record and improved mapping technique reduces model errors down to lower than 1 mm on a global average;
70 therefore, I can extract the much weaker minor and mode-2 internal tide constituents.
2. The model contains 12 internal tide constituents: eight mode-1 constituents (M_2 , S_2 , N_2 , K_2 , K_1 , O_1 , P_1 , and Q_1) and four mode-2 constituents (M_2 , S_2 , K_1 , and O_1). It contains more constituents than any previous empirical internal tide model mentioned in Carrere et al. (2021, Table 1).
3. The model resolves the 12 internal tide constituents each by 5-wave decomposition. The global multiconstituent mul-
75 timodal multidirectional internal tidal field is thus decomposed into 60 simple plane waves at each grid point. The decomposition reveals many new features that were previously masked by multiwave interference.
4. The model contains directionally decomposed components, which reveal numerous well-defined long-range internal tidal beams associated with notable topographic features. The beams are characterized by larger amplitudes, linear-increasing phases, and across-beam co-phase lines.

80 The remainder of this paper is arranged as follows. Section 2 briefly describes the satellite altimetry data and ocean stratification data used in this study. Section 3 gives a detailed description of my mapping procedure and key mapping parameters. Section 4 estimates model errors and evaluates the model using independent altimetry data. Section 5 examines the decomposed components and shows numerous internal tidal beams. Section 6 examines in detail the internal tidal beams off the Amazon shelf and in the Arabian Sea. Section 7 is a summary. Section 8 contains model limitations and perspectives.

85 2 Data

2.1 Satellite altimetry data

The internal tide model is developed using 30 years of satellite altimetry SSH measurements from 1993 to 2022 (Figure 1, red box). The data are pre-processed and distributed by the Copernicus Marine Service (<https://doi.org/10.48670/moi-00146>). The

SSH measurements are made by 15 nadir altimetry missions. The merged data record is about 120 years long. The multisatellite altimetry data have higher spatial resolution, because the SSH measurements are along both exact-repeat and nonrepeat tracks (Zhao, 2022a, b). The data have been pre-processed for standard geophysical corrections including atmospheric effects, surface wave bias, geophysical effects, barotropic tide, pole tide, solid Earth tide and loading tide (Taburet et al., 2019). The mean sea surface model used in this satellite altimetry product is CNES-CLS15 (Pujol et al., 2018). The SSH measurements from seven nadir altimetry missions in 2023 are reserved for model evaluation (Figure 1, blue box).

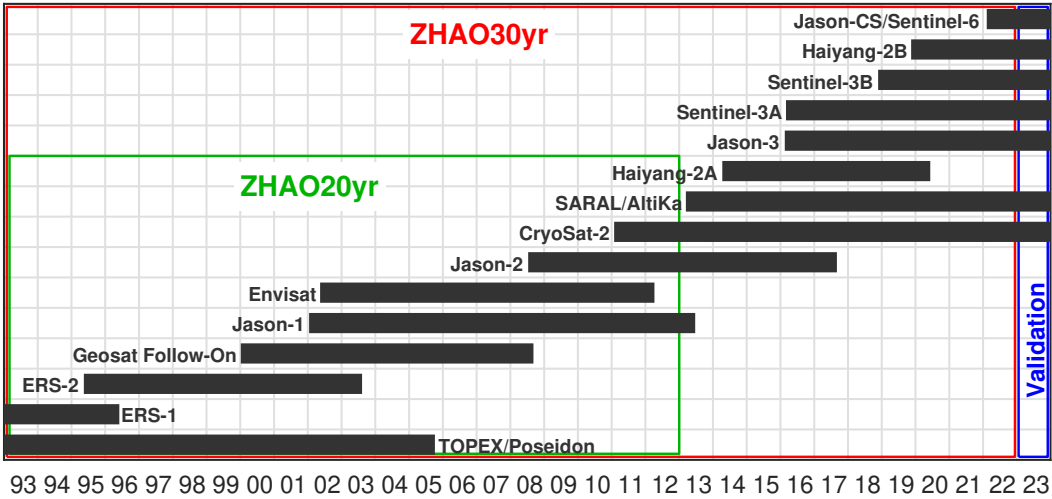


Figure 1. Satellite altimetry data. ZHAO20yr and ZHAO30yr are developed using 20 (1993–2012) and 30 (1993–2022) years of altimetry data, respectively. Altimetry data in 2023 are reserved for model evaluation.

The SSH signals of mesoscale eddies are about one order of magnitude greater than the internal tide signals. Directly mapping internal tides without mesoscale correction would lead to large model errors (Ray and Zaron, 2016; Zhao et al., 2016). Mesoscale correction was brought up by Ray and Byrne (2010) and has been employed in a number of studies (Ray and Zaron, 2016; Zaron, 2019; Zhao, 2022b). In this study, prior mesoscale correction is made using the two-dimensional (2D) gridded SSH fields distributed by the Copernicus Marine Service (<https://doi.org/10.48670/moi-00148>). The fields are gridded daily in time and 0.25° by 0.25° in the horizontal. Prior to mesoscale correction, the gridded SSH fields are 2D low-pass filtered to remove leaked internal tide signals (Ray and Zaron, 2016; Zaron, 2017). Cutoff wavelengths of 200 km (300 km) are used for data sets prepared for mapping semidiurnal (diurnal) internal tides. The mesoscale signals are then interpolated and removed from the along-track SSH data (Ray and Byrne, 2010; Ray and Zaron, 2016; Zaron, 2019; Zhao, 2022b). Note that mesoscale correction is affected by the chosen cutoff parameters (Zaron and Ray, 2018). Mesoscale correction is an indispensable step to suppress mesoscale contamination, although it cannot perfectly remove mesoscale signals.

2.2 Internal tide wavelengths

My mapping technique requires tidal periods and wavelengths of the target internal tides. The periods (frequencies) of internal tides are astronomical constants that have been well documented in classic textbooks (e.g., Pugh and Woodworth, 2014) and software packages (e.g., Egbert and Erofeeva, 2002; Pawlowicz et al., 2002). Table 1 gives the tidal periods of eight principal constituents studied in this paper (M_2 , S_2 , K_1 , O_1 , N_2 , K_2 , P_1 , and Q_1). There are two pairs of internal tide constituents that are separated by 2 cycles per year (cpy). One pair is K_1 (23.9345 hours) and P_1 (24.0659 hours). The other pair is S_2 (12 hours) and K_2 (11.9672 hours). For the barotropic tide, at least a 6-month hourly data record is needed to separate each pair. In this study, I show that 30 years of altimetry data with irregular sampling rates can separate both constituent pairs.

The internal tide wavelengths are calculated using the climatological annual-mean hydrographic profiles in the World Ocean Atlas 2018 (WOA18) provided by the NOAA National Centers for Environmental Information (<https://www.nodc.noaa.gov/OC5/woa18/>). The WOA18 hydrography is at a spatial grid of 0.25° by 0.25° . For a given ocean depth and stratification profile, the vertical structures and eigenvalue speeds of discrete baroclinic modes are obtained by solving the Sturm-Liouville orthogonal problem (Gill, 1982; Kelly, 2016)

$$\frac{d^2\Phi(z)}{dz^2} + \frac{N^2(z)}{c_n^2}\Phi(z) = 0, \quad (1)$$

subject to free-surface (not rigid-lid surface) and rigid-bottom boundary conditions, where $N(z)$ is buoyancy frequency profile, $\Phi(z)$ and c_n are eigenvector and eigenvalue, and the subscript n is modal number, respectively. With Earth's rotation, wavelength λ_n can be calculated from the eigenvalue speed c_n following $\lambda_n = c_n / \sqrt{\omega^2 - f^2}$, where ω and f ($\equiv 2\Omega \sin(\text{latitude})$), where Ω is Earth's rotation rate) are the tidal and inertial frequencies, respectively. The resulting global wavelengths for the semidiurnal and diurnal internal tide constituents are shown in Figures S1 and S2 (Supplementary Materials), respectively. It is well known that wavelengths are a function of location, in particular, latitude. Table 1 gives their global mean wavelengths (within $\pm 60^\circ$ for semidiurnal constituents and $\pm 26.5^\circ$ for diurnal constituents). For the eight mode-1 constituents, the mean wavelengths range from 129.5 km for S_2 to 404.5 km for Q_1 . The mode-2 K_1 and O_1 internal tides have mean wavelengths of 163.8 and 191.2 km, respectively, longer than mode-1 semidiurnal constituents. The mode-2 M_2 and S_2 constituents have wavelengths shorter than 80 km. Mode-1 K_1 and P_1 have close wavelengths (294.1 km and 294.3 km); therefore, it is challenging to separate these two constituents. This study shows that one can extract reasonable K_1 and P_1 internal tides using 30 years of altimetry data.

3 Methods

My recently improved mapping procedure consists of two rounds of plane wave analysis with a spatial bandpass filter in between (Zhao, 2022a, b). An example of the 3-step mapping procedure can be found in Zhao (2022a, Figure 3). In the first step, one target internal tide constituent is mapped by plane wave analysis. At each grid point, five internal tidal waves of arbitrary propagation directions are determined (Section 3.1). The vector sum of these five waves gives the internal tide solution. This step yields a global internal tide field at a regular latitude-longitude grid from the sparse satellite along-track

Table 1. Properties and Empirical Mapping Parameters of the 12 Internal Tide Constituents.

Constituent	Period (hour)	Wavelength ^a (km)	Window Size (step 1)	Bandpass Width ^b (step 2)	Window Size (step 3)	Final Grid
mode-1 M ₂	12.4206	137.3	120 km	[0.75, 1.50]	120 km	0.05°
mode-1 S ₂	12	129.5	120 km	[0.80, 1.25]	120 km	0.05°
mode-1 K ₁	23.9345	294.1	120 km	[0.75, 1.50]	160 km	0.05°
mode-1 O ₁	25.8193	345.6	120 km	[0.75, 1.50]	160 km	0.05°
mode-2 M ₂	12.4206	71.9	120 km	[0.75, 1.50]	80 km	0.05°
mode-2 S ₂	12	67.9	120 km	[0.80, 1.25]	80 km	0.05°
mode-2 K ₁	23.9345	163.8	120 km	[0.75, 1.25]	120 km	0.05°
mode-2 O ₁	25.8193	191.2	120 km	[0.75, 1.25]	120 km	0.05°
mode-1 N ₂	12.6583	142.1	160 km	[0.80, 1.25]	120 km	0.05°
mode-1 K ₂	11.9672	127.9	160 km	[0.80, 1.25]	120 km	0.05°
mode-1 P ₁	24.0659	294.3	160 km	[0.75, 1.50]	160 km	0.05°
mode-1 Q ₁	26.8584	404.5	160 km	[0.75, 1.50]	160 km	0.05°

^a global mean wavelength within $\pm 60^\circ$ (semidiurnal) and $\pm 26.5^\circ$ (diurnal)

^b bandpass width multiplying local wavenumber $K(\text{lon}, \text{lat})$ yields bandpass cut-off wavenumbers

SSH data. In the second step, the regularly gridded internal tide field is cleaned by spatial bandpass filtering (Section 3.2). The target internal tide field is converted to the 2D wavenumber spectrum by Fourier transform and the spectrum is truncated by bandpass width times the local wave number (Zhao, 2022b). Empirical bandpass widths are given in Table 1. In the third step, plane wave analysis is called again to decompose the filtered internal tide field into five internal waves at each grid point. The second-round plane wave analysis is the same as the first-round plane wave analysis, but that the input is the filtered internal tide field in the second step. In the end, the resulting five waves are saved with their respective amplitudes, phases and directions. The 5-wave decomposition makes it possible to separate internal tides in different propagation directions.

3.1 Plane wave analysis

My core technique for mapping internal tides from satellite altimetry data is plane wave analysis developed in a series of previous studies (Zhao and Alford, 2009; Zhao, 2014; Zhao et al., 2016; Zhao, 2022a). Plane wave analysis evolves from the two-dimensional plane-wave fit method (Ray and Cartwright, 2001), but plane wave analysis extracts multiple waves in different propagation directions and thus resolves multiwave interference (Zhao and Alford, 2009). Plane wave analysis determines internal tides using SSH measurements in a square fitting window. At each grid point, the internal tide solution is mapped using along-track altimetry data in a fitting window centered at the grid point. Each fitting window thus contains a large number of independent SSH data. One target internal tidal wave $\eta(A, \phi, \theta)$ has three parameters to be determined: amplitude A , phase ϕ , and propagation direction θ . There are multiple waves of arbitrary propagation directions at one site;

therefore, 5 target internal tidal waves are fitted following

$$155 \quad \eta(A, \phi, \theta; x, y, t) = \sum_{m=1}^5 A_m f(t) \cos\left(\frac{2\pi}{T} t + \phi_m + u(t) - \frac{2\pi}{\lambda} x \cos \theta_m - \frac{2\pi}{\lambda} y \sin \theta_m\right), \quad (2)$$

where x and y are the east and north Cartesian coordinates, t is time, T and λ are the period and wavelength of the target wave, and $f(t)$ and $u(t)$ are nodal factor and phase for the 18.6-year cycle, respectively. The lunar nodal cycle is taken into account (Pugh and Woodworth, 2014), because the altimetry data are longer than 18.6 years. An iterative algorithm has been developed to extract five internal tidal waves in different propagation directions. Examples can be found in Zhao (2014, Figure 3) and
160 Zhao et al. (2016, Figure 2). In each step, the amplitude A , phase ϕ , and propagation direction θ of one target internal tidal wave are determined using SSH data in one given fitting window by least-squares fit. To do that, the amplitude and phase of one plane wave are determined in each compass direction (angular increment is 1°). When the resultant amplitudes are plotted as a function of direction in polar coordinates, an internal tidal wave appears to be a lobe. The amplitude and direction of the target wave are thus determined from the largest lobe. After that, the signal of the determined wave is predicted and removed
165 from the original SSH data. This step is repeated five times to determine five target internal tidal waves. In the end, each wave is refitted with other four waves temporally removed to reduce the wave-wave interference. The five internal tidal waves are usually sorted with decreasing amplitudes, and their vector sum gives the internal tide solution at the grid point.

3.2 Spatial bandpass filtering

Using the spatially regular internal tide field obtained by plane wave analysis, the internal tide field can be converted to a 2D
170 wavenumber spectrum by Fourier transform in overlapping 850 by 850 km windows. I have tested different spatial windows and found that the filtering is insensitive to the window size. The 2D wavenumber spectrum shows that the variance is mainly around the theoretical wavenumber. The variance falling outside the theoretical wavenumber range is considered as noise. Thus, the 2D wavenumber spectrum is truncated and converted back to the internal tide field by inverse Fourier transform. The width of the bandpass filter (e.g., cutoff wave numbers) is empirically determined (Table 1). They reflect the spectral peaks of
175 the target internal tide constituent determined by the length of the data record. The bandpass width is affected by the fitting window employed in plane wave analysis and noise level. To reduce ringing effect of artificial wiggles occurs in the boundary layer, I throw away the filtered values in the outer 100-km boundary layer and only keep values in the inner region. An example of the spatial 2D bandpass filter can be found in Figure 4 of Zhao et al. (2019).

3.3 Special issues

180 There are some issues in the model development that require special attention. First, Sun-synchronous altimetry missions, including ERS-1/2, Envisat, and Haiyang-2A/2B, have an aliasing issue with the S_2 tide. Previous studies usually map S_2 internal tides excluding Sun-synchronous missions (Zhao, 2018; Zaron, 2019). It is a surprise that Ubelmann et al. (2022) can map S_2 internal tides including data from Sun-synchronous missions. In this study, mode-1 and mode-2 S_2 internal tides are mapped using all altimetry missions including Sun-synchronous missions (Figure 1, red box). The result shows that my new

185 S_2 internal tide model has a higher spatial resolution and lower model errors. It significantly improves over my previous S_2 internal tide model (Section 4.3). There are three likely reasons for why Sun-synchronous missions do not ruin the mapping of S_2 internal tides. (1) My mapping procedure extracts internal tides not only by their frequencies in time but also by their wavelengths in space. Measurements by Sun-synchronous missions still provide useful spatial information on S_2 internal tides. (2) The 30-year-long data record itself can significantly reduce model errors. (3) A large fraction of the data is from non-Sun-
190 synchronous missions, which greatly reduces model errors. Additionally, the nontidal signals caused by solar radiance have longer spatial scales and can be reduced by spatial bandpass filtering.

Second, care is needed to separate two pairs of internal tide constituents. The first pair contains mode-1 K_1 and P_1 with tidal periods of 23.9345 and 24.0659 hours, respectively. The second pair contains mode-1 S_2 and K_2 with tidal periods of 12 and 11.9672 hours, respectively. To separate K_1 and P_1 , mode-1 K_1 internal tides are firstly constructed. Then P_1 internal tides are
195 mapped using the temporally K_1 -corrected altimetry data (e.g., predict and subtract K_1 internal tides from the original data). In the end, mode-1 and mode-2 K_1 internal tides are re-mapped using the P_1 -corrected altimetry data. Likewise, S_2 and K_2 can be separated following the same procedure. The results show that this method can suppress cross-talk and better separate the two constituent pairs (Sections 4).

Third, the larger mode-1 constituents may affect the smaller mode-2 constituents. Both mode-1 and mode-2 constituents are
200 mapped for M_2 , S_2 , K_1 , and O_1 . For each constituent, modes 1 and 2 have the same tidal period, but the mode-1 wavelengths are about twice the mode-2 wavelengths (Table 1). For each case, the mode-1 constituent may affect the mode-2 constituent, but the mode-2 constituent does not affect the mode-1 constituent. Assuming the mode-1 and mode-2 internal tide amplitudes are 15 and 5 mm, respectively, and they leak 10% of their amplitude to the other. One can see that mode 2 leaks to mode 1 by 0.5 mm ($5 \text{ mm} \times 10\%$), which is only 3.3% of the mode-1 amplitude. However, mode 1 leaks to mode 2 by 1.5 mm ($15 \text{ mm} \times 10\%$), which is 30% of the mode-2 amplitude. In this study, the mode-1 constituent is firstly mapped and removed from
205 the original data. Then the mode-2 constituent is mapped using the corrected data. Comparisons show that this measure is indispensable to extract reliable mode-2 internal tide constituents.

3.4 Mapping parameters

I extract 12 internal tide constituents from the 30 years of satellite altimetry data one by one following the same 3-step mapping
210 procedure. They are eight mode-1 constituents (M_2 , S_2 , N_2 , K_2 , K_1 , O_1 , P_1 , and Q_1) and four mode-2 constituents (M_2 , S_2 , K_1 , and O_1). Table 1 lists the 12 internal tide constituents and their key empirical mapping parameters. In this study, semidiurnal internal tide constituents are mapped from 60° S to 60° N and diurnal constituents from 30° S to 30° N . In the first round of plane wave analysis, a fitting window of 120 km is used for major constituents (M_2 , S_2 , K_1 , and O_1) and 160 km for minor constituents (N_2 , K_2 , P_1 , and Q_1). In the second round of plane wave analysis, a fitting window of 160 km is used for
215 diurnal constituents, 120 km for mode-1 semidiurnal constituents, and 80 km for mode-2 M_2 and S_2 constituents. In the spatial bandpass filtering, $[0.75, 1.50]$ is used for diurnal constituents and M_2 constituents, and $[0.80, 1.25]$ for other semidiurnal constituents. All constituents are finally interpolated onto a spatial grid of 0.05° by 0.05° . These mapping parameters are empirically chosen after testing several reasonable choices. My previous studies show that these mapping parameters will not

affect the results much on a global scale (Zhao, 2022a, b); however, these parameters can be optimized region by region and constituent by constituent. Figure ?? shows the resulting 12 internal tide constituents. Internal tides with amplitudes lower than 1 mm are shown in light blue. The regions with large model errors due to mesoscale contamination are indicated by black contours. The results show that mode-1 M_2 and K_1 internal tides have the largest amplitudes greater than 25 mm, while mode-1 K_2 and Q_1 internal tides have the lowest amplitudes lower than 3 mm.

3.5 Multiwave decomposition

The global internal tide field is a superposition of multiconstituent multimodal multidirectional internal waves. The multiwave superposition leads to complicated spatial interference and makes it difficult to detect individual internal tidal waves and track their generation, propagation, and dissipation. In the new model, the internal tide field is decomposed into a series of simple plane waves. In frequency, eight principal internal tide constituents are extracted (M_2 , S_2 , N_2 , K_2 , K_1 , O_1 , P_1 , and Q_1). In the vertical direction, two lowest baroclinic modes are extracted for the four major constituents (M_2 , S_2 , K_1 and O_1). In the horizontal direction, each internal tide constituent is decomposed into 5 plane waves with empirically determined directions at each grid point. All together, 60 simple plane waves are determined at each grid point. The 12 internal tide constituents and their 5 wave components are shown in Figures S4–S15 (Supplementary Materials).

For each constituent, the 5-wave summed field shows obvious interference features such as half-wavelength fluctuations in amplitude and phase. In contrast, the 5-wave resolved components are not affected much by multiwave interference. Therefore, the decomposed results reveal a lot of new features that were previously masked by multiwave interference. In particular, the first wave components (panels (b) in Figures S4–S15) show the largest waves at each grid point. They have relatively larger and smoother amplitudes, so that individual long-range internal tidal beams can be clearly identified. Around the Hawaiian Ridge, there are outgoing internal tidal beams in all 12 internal tide constituents. Because the Hawaiian Ridge is generally in west-east direction, the internal tide radiation is dominantly southward and northward. Around the south-north aligned Izu–Bonin–Mariana Arc, there exist westward and eastward internal tidal beams. In the Madagascar–Mascarene region, there are outgoing internal tidal beams in all directions. However, internal tidal beams shown in Figures S4–S15 may mix internal tidal waves from different generation sites. In this study, I show that isolated internal tidal beams should be examined using the directionally decomposed components (Section 5).

4 Errors and Evaluation

4.1 Model errors

Model errors (Zhao, 2025) are estimated using background internal tides following Zhao (2023a, b). Background internal tides are extracted from the same altimetry data following the same procedure but using tidal periods slightly different from the eight principal constituents. In other words, model errors are indicated by internal tide signals where internal tides do not exist. In principle, model errors are determined by the given altimetry data and the mapping technique used to extract internal

250 tides. Background internal tides do not vary much over the narrow semidiurnal or diurnal frequency bands (Zhao, 2023b). This study estimates errors in semidiurnal internal tides using 12.3373 hours (M_2 minus 5 minutes) and in diurnal internal tides using 23.8511 hours (K_1 minus 5 minutes). Both mode-1 and mode-2 internal tide errors are estimated for the semidiurnal and diurnal constituents. The resulting model errors are shown in Figure 2. In regions of extremely high mesoscale eddies, the semidiurnal errors are dominantly larger than 1 mm due to mesoscale contamination (mesoscale correction in Section 2 is not enough). These regions include the Kuroshio extension region, the Gulf Stream, the East Australian Current, the Agulhas Current, the Brazil Current, the Leeuwin Current, the loop current in the Gulf of Mexico, and the Antarctic Circumpolar Current. These regions are highlighted by black contours following Zhao et al. (2016). Fortunately, in most of the global ocean, model errors are very low (Figure 2, blue patches). On a global average, the model errors in all constituents are lower than 1 mm. The low model errors allow us to map the much weaker mode-2 constituents and minor constituents.

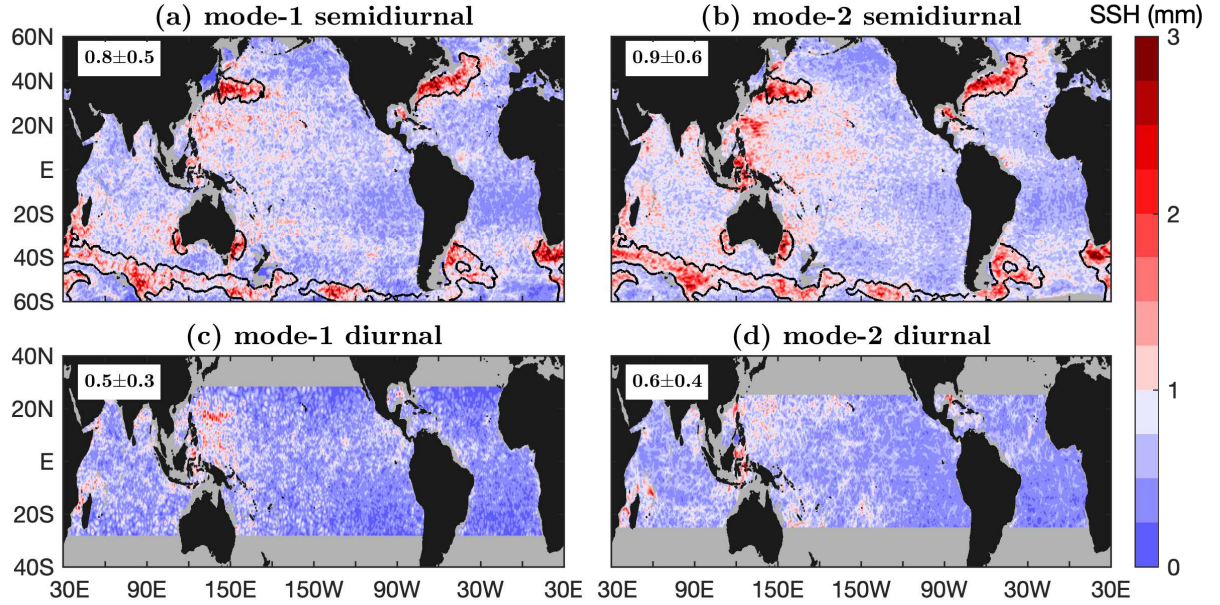


Figure 2. Model errors. For each constituent, the global mean and one standard deviation are given in the upper left corner. Black contours indicate regions of large model errors due to mesoscale contamination.

260 4.2 Model evaluation

The new internal tide model is evaluated using independent nadir-looking altimetry data in 2023 (Figure 1, blue box). Once the harmonic constants (amplitude and phase of each constituent) in the model are determined, one can predict internal tides $a(x, y, t)$ following

$$a(x, y, t) = \sum_{n=1}^{12} A_n(x, y) f_n(t) \cos\left[\frac{2\pi}{T_n} t + \phi_n(x, y) + u_n(t)\right], \quad (3)$$

265 where (x, y) indicate location, t is time, T_n is the tidal period, $f_n(t)$ and $u_n(t)$ are the nodal factor and phase of the 18.6-year cycle, $A_n(x, y)$ and $\phi_n(x, y)$ are the amplitude and phase of one internal tide constituent, and the subscript n indicates the serial number of the 12 constituents, respectively. One can predict internal tides for any individual constituent or combination of constituents. Note that Equation (3) only predicts the SSH displacements of internal tides. To predict their subsurface properties, one should convert the SSH displacements to subsurface properties following their baroclinic modal structures
 270 (Kelly, 2016; Zhao et al., 2016).

For each SSH measurement $\eta(x, y, t)$ in the independent data with known location (x, y) and time t , the internal tide signal can be predicted following Equation (3) and subtracted from the original data. The variance reduction $\sigma^2(x, y, t)$ is the difference in variance computed before and after the internal tide correction following

$$\sigma^2(x, y, t) = \eta^2(x, y, t) - [\eta(x, y, t) - a(x, y, t)]^2. \quad (4)$$

275 All SSH measurements in the independent altimetry data are corrected following Equation (4). The resulting variance reductions are then binned into 1° by 1° boxes. Variance reductions for the 12 internal tide constituents are computed respectively following the same procedure. Special measures are needed to take care of the cross-talk between constituents (Section 3.3). To validate the mode-1 P_1 constituent, one should first predict and remove the mode-1 and mode-2 K_1 constituents, and vice versa. The same measure is taken in the evaluation of the S_2 – K_2 pair. In addition, to validate each of the four mode-2 constituents
 280 (M_2 , S_2 , K_1 , and O_1), one need to first predict and correct the corresponding mode-1 constituent.

The global maps of variance reductions explained by the 12 constituents are shown in Figure 3. The predicted real internal tides reduce variance by σ_{sig}^2 but model errors increase variance by σ_{err}^2 . When internal tides are larger than model errors ($\sigma_{sig}^2 > \sigma_{err}^2$), positive variance reductions are obtained. Otherwise, negative variance reductions are obtained. The results show that all the constituents can cause regional positive variance reductions, because they can overcome model errors in these
 285 regions. However, these constituents also cause negative variance reductions in some regions, where the weak internal tides are lower than model errors. Figure 3 shows that negative variance reduction occurs in regions with weak internal tides, such as the equatorial and southern Pacific Ocean. Their global area-weighted mean variance reductions are 17.97 (mode-1 M_2), 2.26 (mode-2 M_2), 2.70 (mode-1 S_2), 0.52 (mode-2 S_2), 0.40 (mode-1 N_2), -0.26 (mode-1 K_2), 4.30 (mode-1 K_1), 0.39 (mode-2 K_1), 2.29 (mode-1 O_1), 0.13 (mode-2 O_1), 0.03 (mode-1 P_1), and -0.002 mm^2 (mode-1 Q_1), respectively. Ten constituents
 290 (but for K_2 and Q_1) cause overall positive values, because they can overcome model errors. The four minor constituents are overall weak, but they are relatively strong in the western Pacific Ocean (the Indonesian Seas, the South China Sea and the Philippine Sea). Their area-weighted mean variance reductions in the region ranging 105° – 160° E, 10° S– 30° N (Figure 3, green boxes) are 1.52 (N_2), 0.47 (K_2), 1.57 (P_1), and 0.61 (Q_1) mm^2 , respectively. The results suggest that the minor internal tide constituents are only reliable in the western Pacific Ocean.

295 4.3 Comparison of ZHAO20yr and ZHAO30yr

In this section, I show that ZHAO30yr greatly improves over ZHAO20yr, an old model developed in Zhao et al. (2016) and presented in Carrere et al. (2021). ZHAO20yr was constructed using 20 years of altimetry data from 1993–2012 by the obsolete

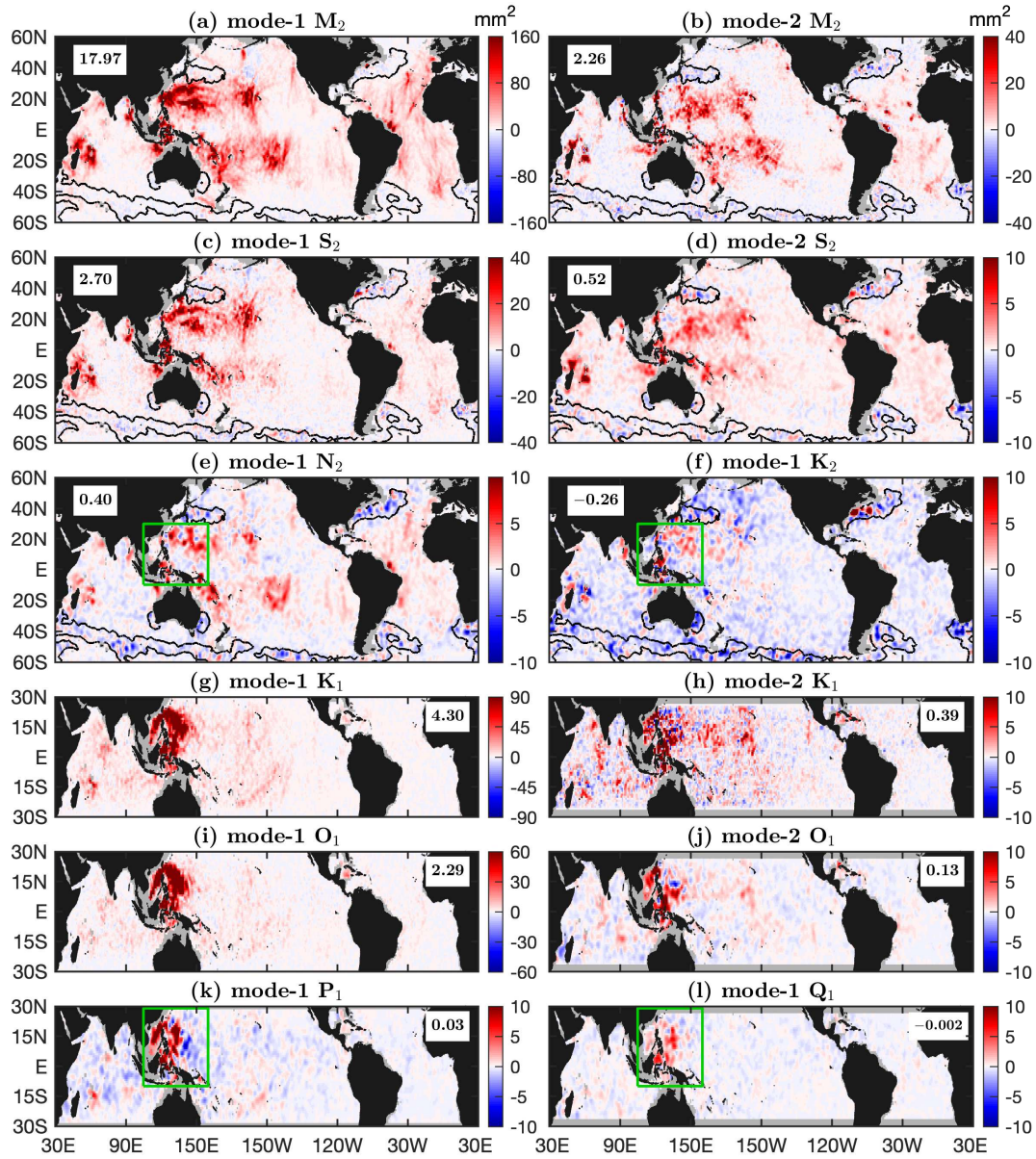


Figure 3. Model evaluation. Shown are variance reductions obtained in making internal tide correction to independent altimetry data in 2023. Black contours indicate regions of large model errors. Global area-weighted mean variance reductions (unit: mm^2) are given in the upper left (a-f) or right (g-l) corners. Green boxes indicate regions where minor constituents have strong signals.

mapping procedure (Zhao et al., 2016). ZHAO20yr contains only 4 mode-1 constituents: M_2 , S_2 , K_1 and O_1 . Both models are evaluated using the altimetry data in 2023 following the same procedure. The resulting global variance reduction maps (not shown) are similar to Figures 3. It is straightforward to calculate the global area-weighted mean variance reductions caused

by the two models (Figure S16). It shows that ZHAO30yr reduces more variance than ZHAO20yr for all 4 constituents. The improvement can be quantified by the change rate of variance reduction following $(\sigma_{30yr}^2 - \sigma_{20yr}^2) / \sigma_{20yr}^2 \times 100\%$. They are 32% (M_2), 80% (S_2), 45% (K_1) and 36% (O_1), respectively, suggesting that ZHAO30yr significantly improves over my old model. The improvement is mainly because ZHAO30yr is constructed using a longer data record and an improved mapping
305 technique.

A comparison of the mode-1 S_2 internal tides in ZHAO20yr and ZHAO30yr is shown in Figure S17. One can see that ZHAO30yr has a higher spatial resolution and lower errors. The low model errors in ZHAO30yr are evidenced by the weak signals in the regions of large model errors. The improvement is because they are constructed using different altimetry data records. ZHAO20yr uses 20 years of altimetry data from 1993 to 2012 excluding Sun-synchronous missions. The data record
310 is only about 40 years long. ZHAO30yr uses all satellite altimetry data from 1993 to 2022 including the Sun-synchronous missions (Figure 1). The data record is about 120 years long, about 3 times larger. Due to their different data densities, the S_2 constituent is mapped using fitting windows of 120 km and 250 km, respectively. As a result, ZHAO30yr has a much higher spatial resolution and better resolve internal tidal beams.

5 Decomposed Components and Internal Tidal Beams

315 In this section, I present the 12 internal tide constituents, each of which has been divided into two components by propagation direction. The decomposed components reveal numerous well-defined long-range internal tidal beams. A picture is worth a thousand words. An interested reader may study the decomposed internal tide components for more features.

5.1 Mode-1 and mode-2 M_2 constituents

Figure 4 shows the mode-1 M_2 constituent and its northward (0° – 180°) and southward (180° – 360°) components. In this
320 figure, bottom topographic features are indicated by the 3000-m isobath contours (green lines). The 5-wave summed M_2 internal tide field (Figure 4a) shows significant small-scale spatial variations caused by multiwave interference. Internal tides with amplitudes lower than 1 mm (model errors) are shown in light blue. Figure 4a shows that mode-1 M_2 internal tides are dominantly greater than model errors and barely affected by model errors. Therefore, previous satellite investigations of internal tides mainly focused on the mode-1 M_2 constituent. Figure 4a shows that strong mode-1 M_2 internal tides occur
325 around the Hawaiian Ridge, around the French Polynesian Ridge, in the western Pacific Ocean, in the Madagascar–Mascarene region, and in the Indonesian Seas. These regions have long been recognized in previous studies by satellite altimetry (Ray and Zaron, 2016; Zhao et al., 2016; Zaron, 2019), numerical models (Simmons et al., 2004; Li et al., 2015; Arbic et al., 2018), semi-analytical models (Nycander, 2005; Falahat et al., 2014; de Lavergne et al., 2019), and recently observed by drifter measurements (Zaron and Elipot, 2024).

330 I divide the mode-1 M_2 constituent into northward and southward components by propagation direction. The northward and southward components contain the largest waves at each grid point with propagation directions ranging 0° – 180° and 180° – 360° , respectively. Such a division can separate long-range internal tidal beams in different directions. Note the eastward

(-90° – 90°) and westward (90° – 270°) decomposition can better resolve semidiurnal internal tidal beams in regions such as the western Pacific Ocean. In the decomposed components (Figures 4b, c), internal tides with amplitudes lower than $2/3$ mm are shown in light blue. The colormap adjustment is to highlight internal tidal beams. The northward and southward components show numerous well-defined long-range internal tidal beams, which are featured by larger amplitudes, linear-increasing phases, and across-beam co-phase lines (Section 6). The results are consistent with previous satellite observations using short data records (Zhao and Alford, 2009; Zhao, 2014; Zhao et al., 2016), because mode-1 M_2 internal tides are less affected by model errors.

All mode-1 M_2 beams are associated with notable topographic features. In the Pacific Ocean, mode-1 M_2 beams radiate from the Hawaiian Ridge, the Line Islands Ridge, the French Polynesian Ridge, the Izu–Bonin–Mariana Arc, the Luzon Strait, the Amukta Pass (Alaska), the Mendocino Ridge, the Macquarie Ridge, and the Eastern Pacific Rise. In the Indian Ocean, mode-1 M_2 beams are from the Mascarene Plateau, the Ninety East Ridge, the Andaman Islands chain, and the Indian western shelf. In the Atlantic Ocean, mode-1 M_2 beams are from the Mid-Atlantic Ridge, the Amazon shelf, the Vitória-Trindade Ridge, the Walvis Ridge, the Great Meteor Seamount, and the Cape Verde. In addition, there are many short-range mode-1 M_2 beams from the narrow straits in the Indonesian Seas, the Coral Sea, and the Caribbean Sea. As an example, Section 6.1 shows mode-1 M_2 beams off the Amazon shelf.

Figure 5 shows the mode-2 M_2 constituent and its northward (0° – 180°) and southward (180° – 360°) components. The mode-2 M_2 constituent is relatively weak; however, its SSH amplitudes may be up to 15 mm, larger than minor constituents N_2 and K_2 . Mode-2 M_2 internal tides are mainly associated with rough bottom topography, because they are also generated in the tide-topography interaction. Mode-2 M_2 internal tides mainly occur at low latitudes, which is likely determined by the latitudinal structure of ocean stratification. Note that mode-2 M_2 internal tides tend to become more incoherent and undetectable, because they are easily affected by the time-varying ocean environment. The mode-2 M_2 constituent is divided into northward and southward components following the same method. The northward and southward internal tides are to the north and south of notable topographic features, respectively (Figures 5b, c), suggesting that they are well extracted and separated. The decomposed components show numerous well-defined mode-2 M_2 beams. Section 6.1 examines the mode-2 M_2 beams off the Amazon shelf.

In the Pacific Ocean, the following remarkable generation sources have been recognized: the Hawaii region in the North Pacific, seamounts, island chains and ridges in the western Pacific Ocean, the western South Pacific including the Coral Sea, the French Polynesian Ridge in the South Pacific, the Eastern Pacific Rise, the Alaskan shelf, and the Indonesian Seas. The Indian ocean has the following remarkable sources: the Madagascar–Mascarene region, the Indian western shelf, the Bay of Bengal, the Andaman Sea, and the Australian Northwest Coast. In the Atlantic Ocean, mode-2 M_2 beams are associated with the Mid-Atlantic Ridge, the Amazon shelf, the Walvis Ridge, and several scattered seamounts. In Figure 5, some mode-2 M_2 beams are highlighted using blue circles. Note that ZHAO30yr presents a better mode-2 M_2 field than Zhao (2018), due to the long data record and improved mapping technique (Sections 2 and 3).

The satellite observed mode-1 and mode-2 M_2 beams have the following different features. (1) Mode-2 M_2 beams are shorter than mode-1 M_2 beams. Mode-2 M_2 internal tides can travel over hundreds of km, in contrast to thousands of km

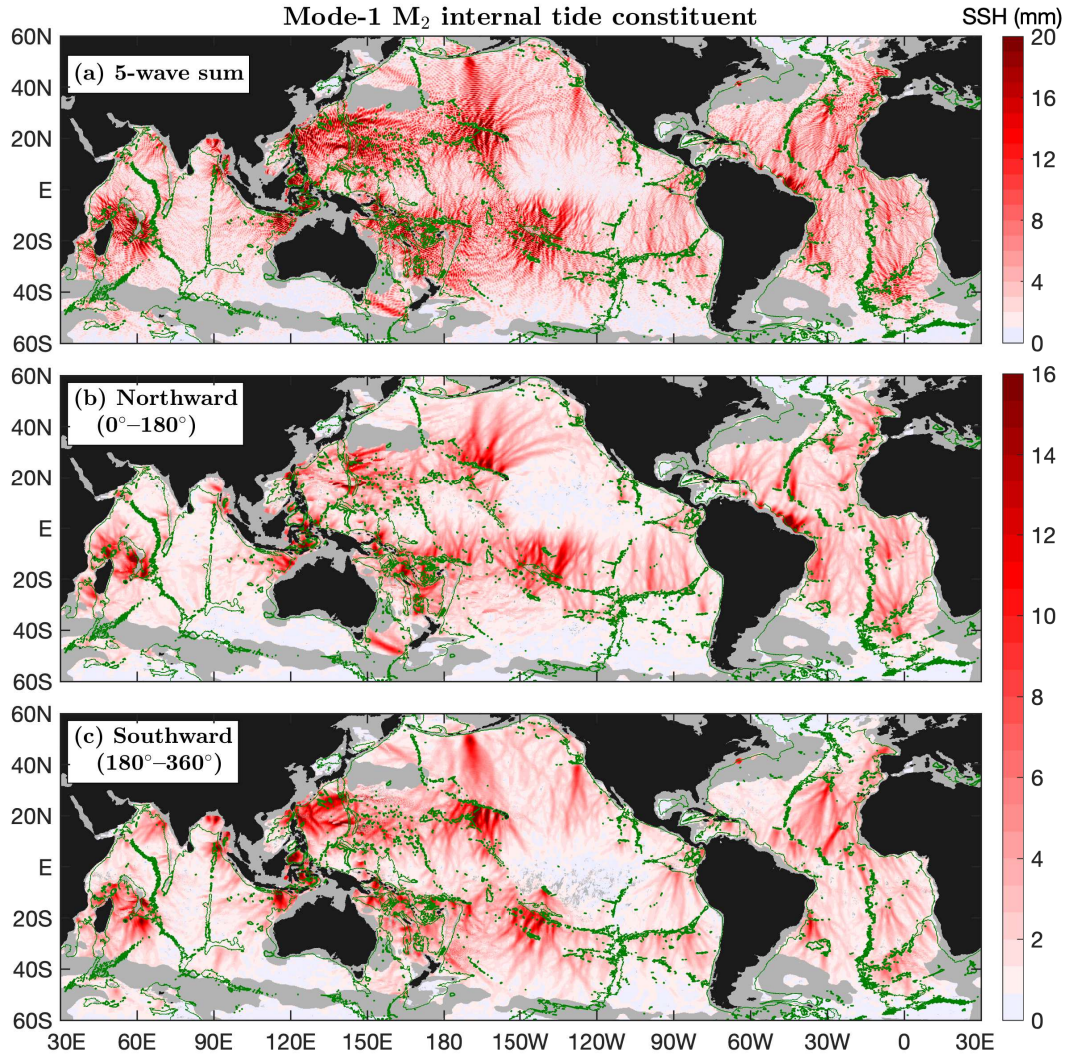


Figure 4. Mode-1 M_2 internal tide constituent. (a) The 5-wave sum. (b) Northward component. (c) Southward component. Internal tides in regions of large model errors or shallower than 1000 m in depth are shown in gray. Green contours indicate the 3000-m isobath. Numerous well-defined long-range internal tidal beams are associated with notable topographic features.

for mode-1 M_2 internal tides. It is partly because mode-2 waves become more incoherent than mode-1 waves after leaving their generation sources (Rainville and Pinkel, 2006). (2) Mode-2 M_2 beams are narrower than mode-1 M_2 beams. That is why the altimetry data along nonrepeat tracks are important in mapping mode-2 internal tides. (3) There are more mode-2 M_2 beams than mode-1 M_2 beams, likely because mode-2 M_2 beams can be induced by small-scale topographic features such as isolated seamounts (Llewellyn Smith and Young, 2002; Zhao, 2018; Geoffroy et al., 2024). Because mode-2 M_2 beams are narrower and shorter, one can locate their sources over topographic features. For example, some isolated mode-2 beams are

unambiguously associated with known topographic features (Figure 5, blue circles). The mode-1 and mode-2 M_2 beams shown in Figures 4 and 5 contain a lot of important information. A detailed examination of the M_2 internal tides region by region or beam by beam can deepen the understanding of their generation, propagation, and dissipation.

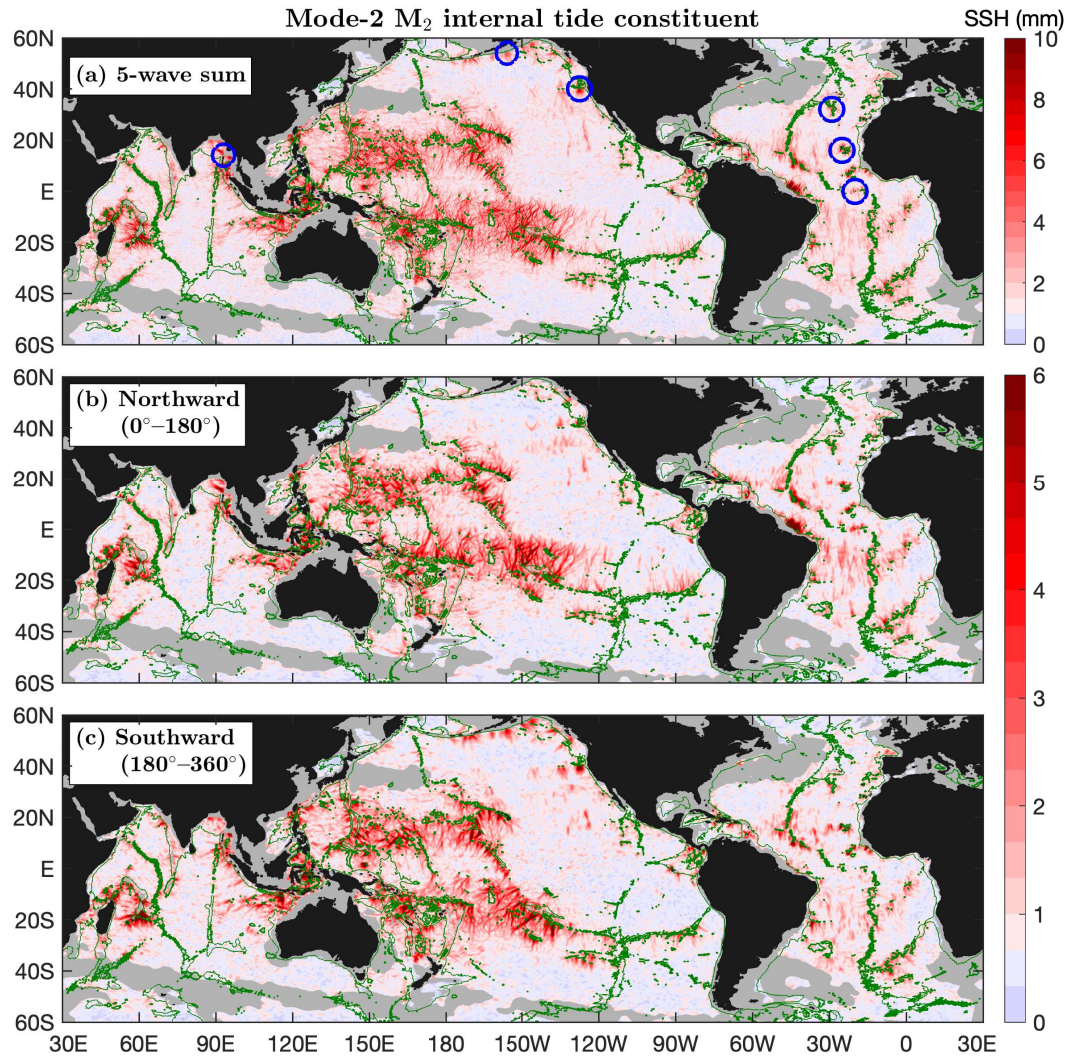


Figure 5. As in Figure 4 but for the mode-2 M_2 internal tide constituent. Well-defined long-range internal tidal beams are associated with notable topographic features. Blue circles mark some isolated beams. Mode-2 M_2 beams are narrower and shorter than mode-1 M_2 beams.

5.2 Mode-1 and mode-2 S_2 constituents

Figure 6 shows the mode-1 S_2 constituent and its northward (0°–180°) and southward (180°–360°) components. Similar to the mode-1 M_2 constituent, the decomposed components (Figures 6b, c) reveal numerous long-range mode-1 S_2 internal tidal

380 beams. It shows that the northward mode-1 S_2 beams from the Hawaiian Ridge reaching the Alaskan shelf and the southward mode-1 S_2 beams from Amukta Pass (Alaska) reaching the Hawaiian Ridge. These long-range mode-1 S_2 beams have been observed in Zhao (2017). Additionally, mode-1 S_2 beams are observed to radiate from notable topographic features such as the Mendocino Ridge, the French Polynesian Ridge, the Izu–Bonin–Mariana Arc, the Australian Northwest shelf, the Lombok Strait, the Andaman Islands chain, and the Mascarene Plateau. In the Atlantic Ocean, mode-1 S_2 beams radiate from the
 385 Amazon shelf, the Vitória-Trindade Ridge, the Walvis Ridge, and isolated seamounts along the Mid-Atlantic Ridge. Compared to Zhao (2017), however, ZHAO30yr can better resolve mode-1 S_2 beams, due to its higher spatial resolution and lower noise level.

In general, the mode-1 M_2 and S_2 constituents show similar internal tidal beams. For example, one notable topographic feature (e.g., the Hawaiian Ridge) usually generate both M_2 and S_2 internal tidal beams. But they have the following different
 390 features. (1) Mode-1 S_2 beams are usually narrower and shorter than corresponding mode-1 M_2 beams, likely because the S_2 barotropic and internal tides are weak and easily masked by model errors. (2) Mode-1 S_2 internal tides in the southern Pacific Ocean (e.g., the French Polynesian Ridge, the Tasman Sea, and the Coral Sea) are weaker, which is caused by the weaker S_2 barotropic tide in this region (Zhao, 2017).

Figure 7 shows the mode-2 S_2 constituent and its northward (0° – 180°) and southward (180° – 360°) components. The mode-
 395 2 S_2 constituent is much weaker. Its amplitudes are usually lower than 4 mm. Therefore, in most of the global ocean, mode-2 S_2 internal tides are overwhelmed by model errors. Fortunately, mode-2 S_2 internal tides are strong enough to overcome model errors in their source regions such as the Hawaiian Ridge, the western Pacific Ocean, the Indonesian Sea, the Coral Sea, the Madagascar–Mascarene region, and the Amazon shelf. Note that the 2–3-mm mode-2 S_2 internal tides are real signals, because they can cause positive variance reductions in making internal tide correction to independent altimetry data (Figure
 400 3d). Likewise, the decomposed components (Figures 7b, c) show numerous well-defined mode-2 S_2 beams associated with topographic features. For example, one mode-2 S_2 beam radiates from the Andaman islands chain (Figure 7b, blue circle). Mode-2 S_2 beams can be clearly seen off the Amazon shelf (Section 6.1). In conclusion, the mode-1 and mode-2 S_2 constituents are weak; however, my multiwave decomposition can resolve well-defined internal tidal beams.

5.3 Mode-1 N_2 constituent

405 Figure 8 shows the mode-1 N_2 constituent and its northward (0° – 180°) and southward (180° – 360°) components. The mode-1 N_2 constituent has amplitudes as large as 6 mm and can overcome model errors in most of the global ocean. Mode-1 N_2 beams can be seen in the 5-wave summed field (Figure 8a), but they are smeared by multiwave interference. The decomposed components (Figures 8b, c) reveal well-defined long-range mode-1 N_2 beams. For example, one can observe both northward and southward N_2 beams radiating from the Hawaiian Ridge, the French Polynesian Ridge, and the Macquarie Ridge. In an
 410 earlier work, Zhao (2023b) mapped the mode-1 N_2 constituent using 27 years of altimetry data (1993–2019) by the same mapping technique used in this study. A comparison shows that the two models are almost same, because 90% of the two data records are the same (27-year vs 30-year). Zhao (2023b) gave a detailed description of the mode-1 N_2 constituent and compared with the mode-1 M_2 constituent. It was reported that mode-1 N_2 internal tides can travel from the Hawaiian Ridge

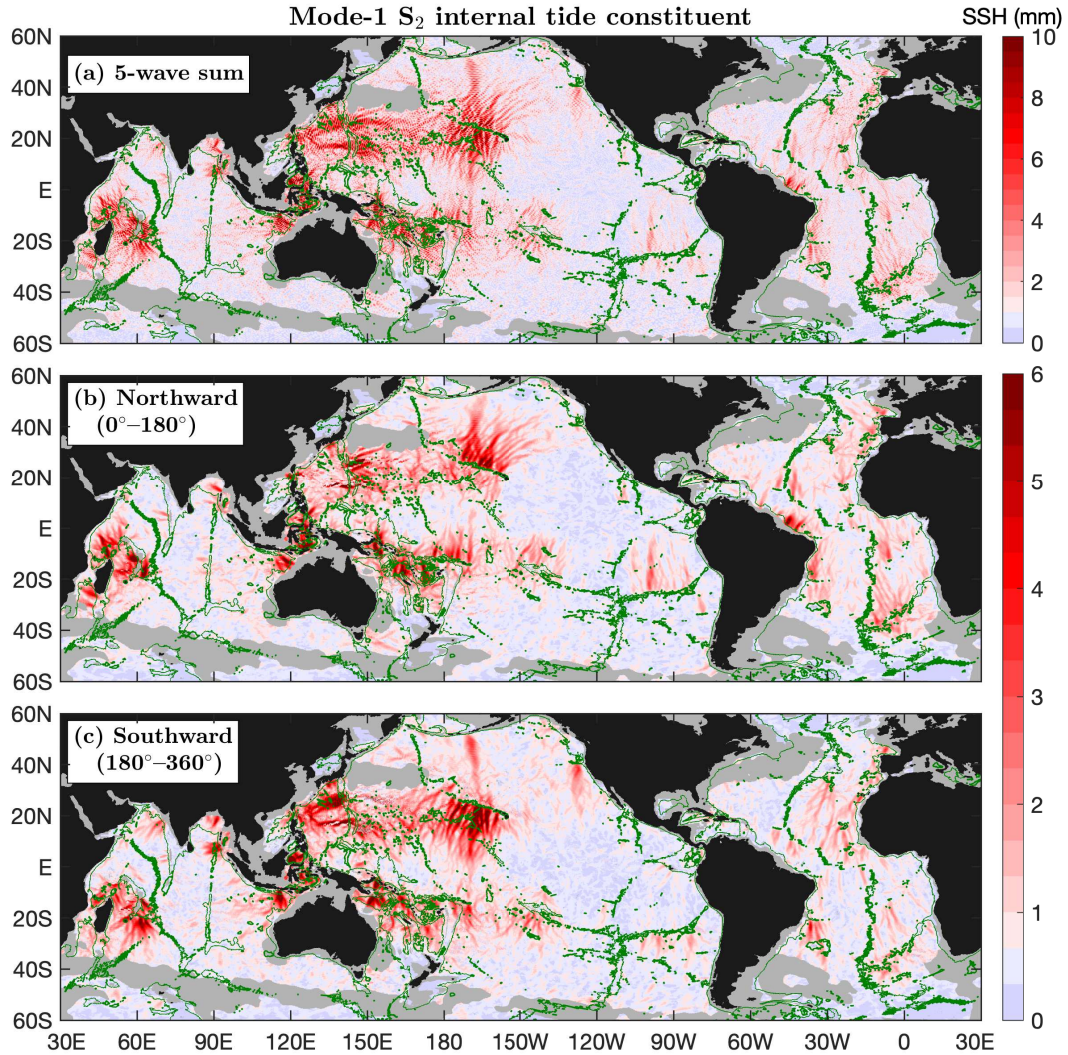


Figure 6. As in Figure 4 but for the mode-1 S_2 internal tide constituent.

to the Alaska and that the southward beams from the Mendocino Ridge can travel over 2000 km. Zhao (2023b) showed that
 415 mode-1 M_2 and N_2 internal tides have similar spatial patterns and that the N_2 amplitudes are about 1/5 of the M_2 amplitudes.
 To avoid repetition, an interested reader is referred to Zhao (2023b) for a detailed description of the mode-1 N_2 constituent.

5.4 Mode-1 K_2 constituent

Figure 9 shows the mode-1 K_2 constituent and its northward (0°–180°) and southward (180°–360°) components. The weak
 420 mode-1 K_2 constituent usually has amplitudes lower than 4 mm; therefore, it is masked by model errors in most of the global
 ocean. However, the mode-1 K_2 constituent can overcome model errors in its source regions such as the Hawaiian Ridge, the

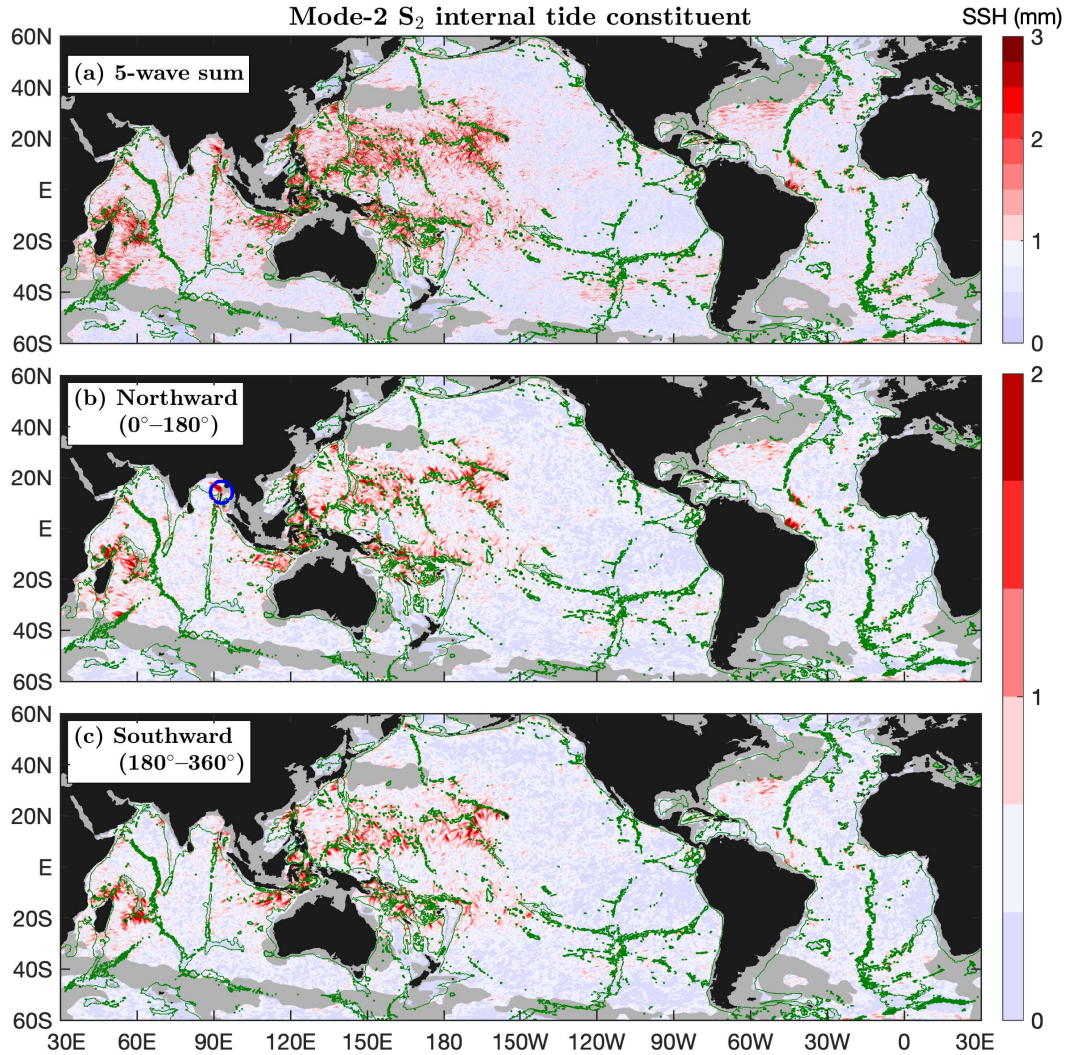


Figure 7. As in Figure 5 but for the mode-2 S_2 internal tide constituent. The blue circle marks an isolated beam in the Bay of Bengal.

Indonesian Seas, and the western Pacific Ocean, where positive variance reduction is obtained in making internal tide correction to independent altimetry data. The decomposed components show numerous well-defined mode-1 K_2 beams. For example, one can see southward and northward beams from the Hawaiian Ridge. Note that mode-1 K_2 beams from the Hawaiian Ridge can be tracked over 1000 km before disappearance. In addition, mode-1 K_2 beams radiate from the Mascarene Plateau, the Luzon Strait, the Mendocino Ridge, the Lombok Strait, the Vitória-Trindade Ridge, and the Amazon shelf (Section 6.1).

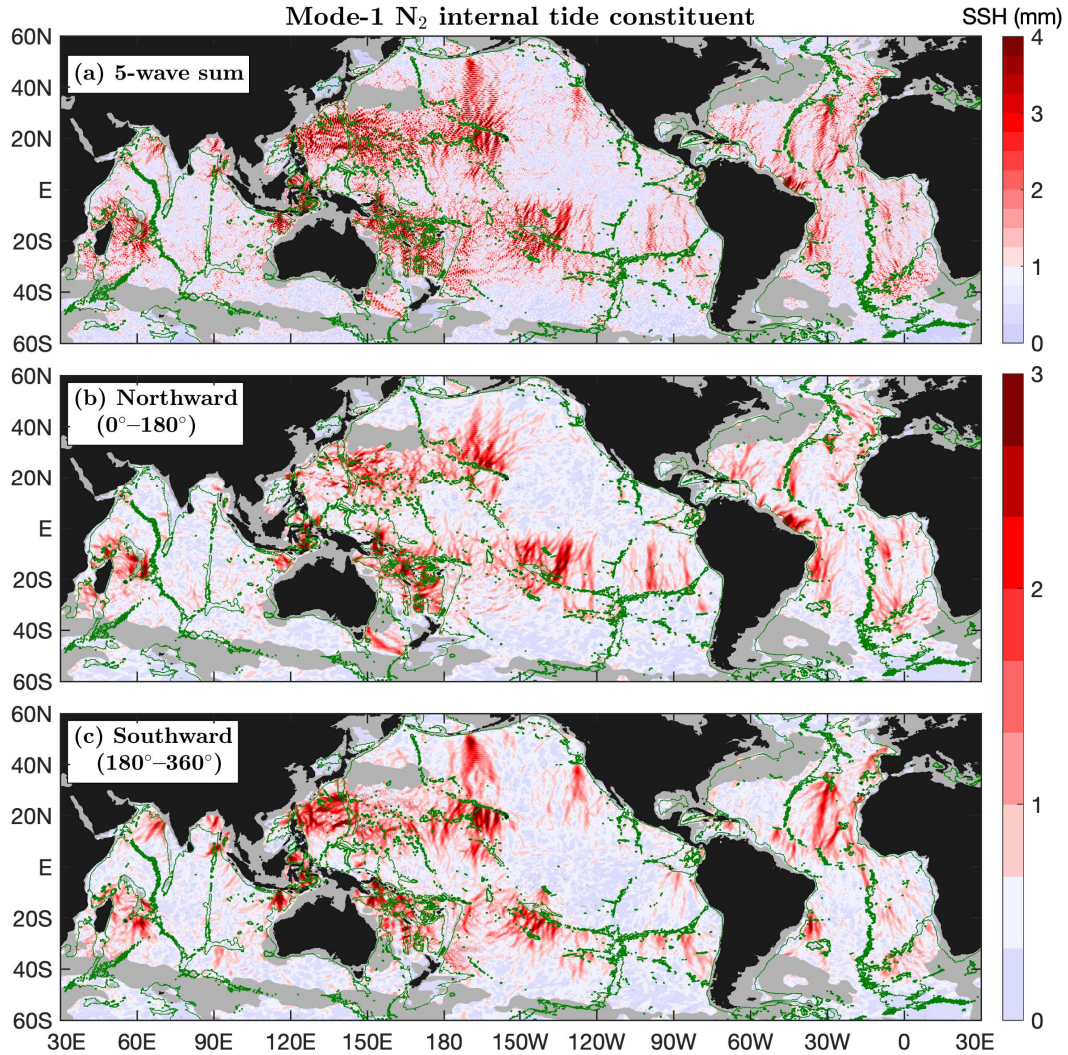


Figure 8. As in Figure 4 but for the mode-1 N_2 internal tide constituent.

5.5 Mode-1 and mode-2 K_1 constituents

Figure 10 shows the mode-1 K_1 constituent and its eastward (-90° – 90°) and westward (90° – 270°) components. In this study, all diurnal internal tide constituents are divided into eastward and westward components, because such a division can better resolve internal tidal beams in most of the global ocean. The eastward and westward components contain the largest wave at each grid point with propagation direction ranging -90° – 90° and 90° – 270° , respectively. All diurnal internal tide constituents are limited within about $\pm 30^\circ$, poleward of which there are no propagating diurnal internal tides. The 3000-m isobath contours are overlain to show topographic features. The most remarkable feature of the mode-1 K_1 constituent and other diurnal con-

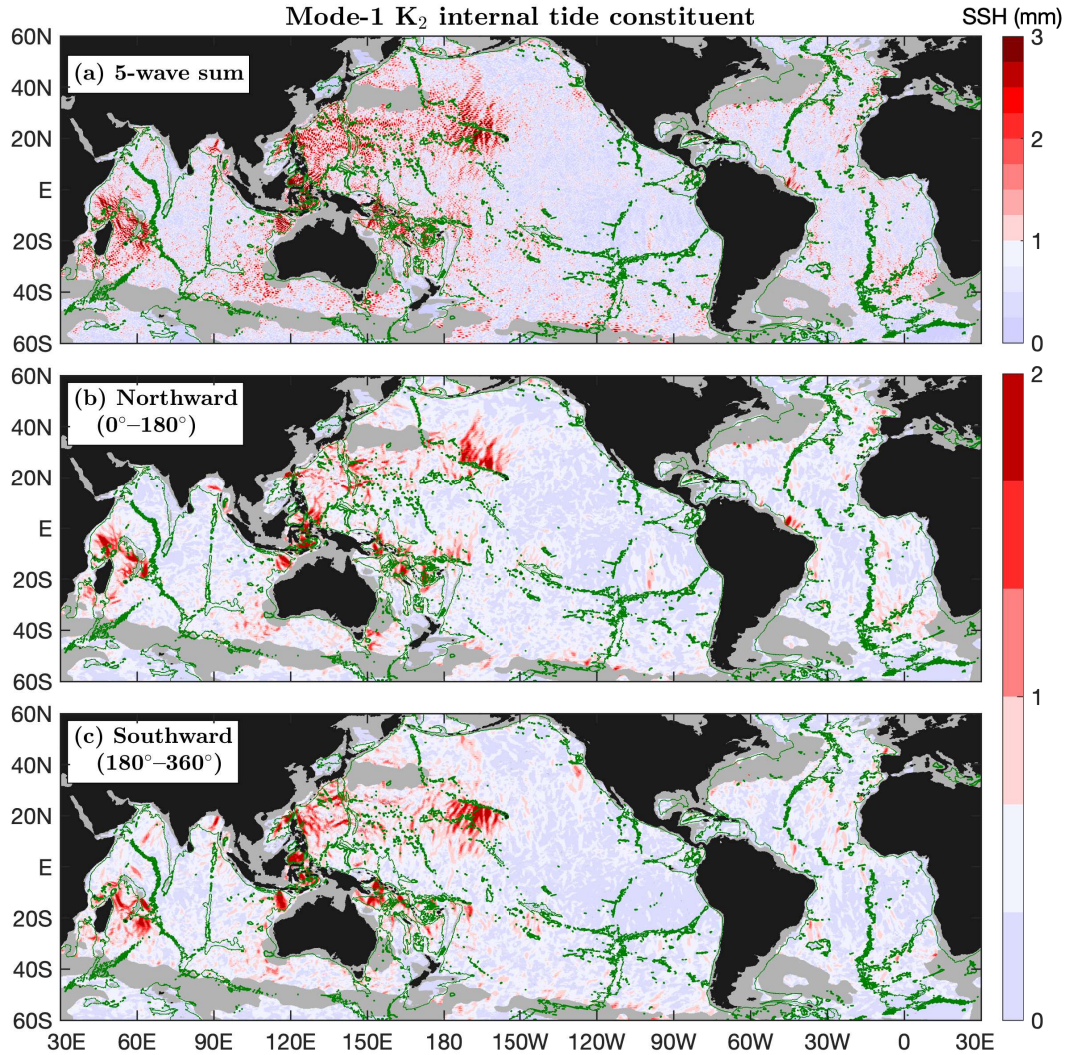


Figure 9. As in Figure 4 but for the mode-1 K_2 internal tide constituent.

stituents is their geographic distribution: All diurnal constituents are strong in the Indian and western Pacific Oceans, and weak in the Atlantic and eastern Pacific Oceans. This feature stems from the geographic inhomogeneity of the diurnal barotropic tide
 435 (Egbert and Ray, 2003). It has long been known that diurnal barotropic tide is weak in the Atlantic Ocean.

The Luzon Strait is the strongest source of mode-1 K_1 internal tides and radiates mode-1 K_1 beams eastward into the western Pacific Ocean and westward into the South China Sea. In their long-range propagation, both beams refract toward the equator due to the beta effect (Zhao, 2014). The Tonga–Kermadec Ridge radiates another long-range mode-1 K_1 beam that propagates northeastward over 3000 km and refracts toward the equator for the same reason (Figure 10b). The decomposed components
 440 (Figures 10b, c) show numerous well-defined long-range mode-1 K_1 beams. In the Indian Ocean, mode-1 K_1 beams radiate

Islands chain, and the Mascarene Plateau. In the Pacific Ocean, mode-2 K_1 beams are from the Luzon Strait, the Indonesian Seas, the Hawaiian Ridge, the Line Islands Ridge, the French Polynesian Ridge, and the eastern Pacific Rise. In the Atlantic Ocean, the mode-2 K_1 internal tides are very weak.

455 The mode-1 and mode-2 K_1 constituents have different spatial patterns (Figures 10 and 11). Mode-2 K_1 beams are shorter and narrower than mode-1 K_1 beams. The short and narrow mode-2 K_1 beams allow us to locate their generation sites. As an example, there are two isolated mode-2 K_1 beams in the eastern Pacific Ocean (Figure 11, blue circles). They originate at two notable seamounts and propagate northward over 1000 km. In contrast, there are no other large diurnal mode-2 beams in the vast eastern Pacific Ocean. This feature raises the question of what special topographic and tidal conditions combined
 460 induce these isolated beams. Answering this question may improve the understanding of the generation of internal tides and their variation with global ocean changes.

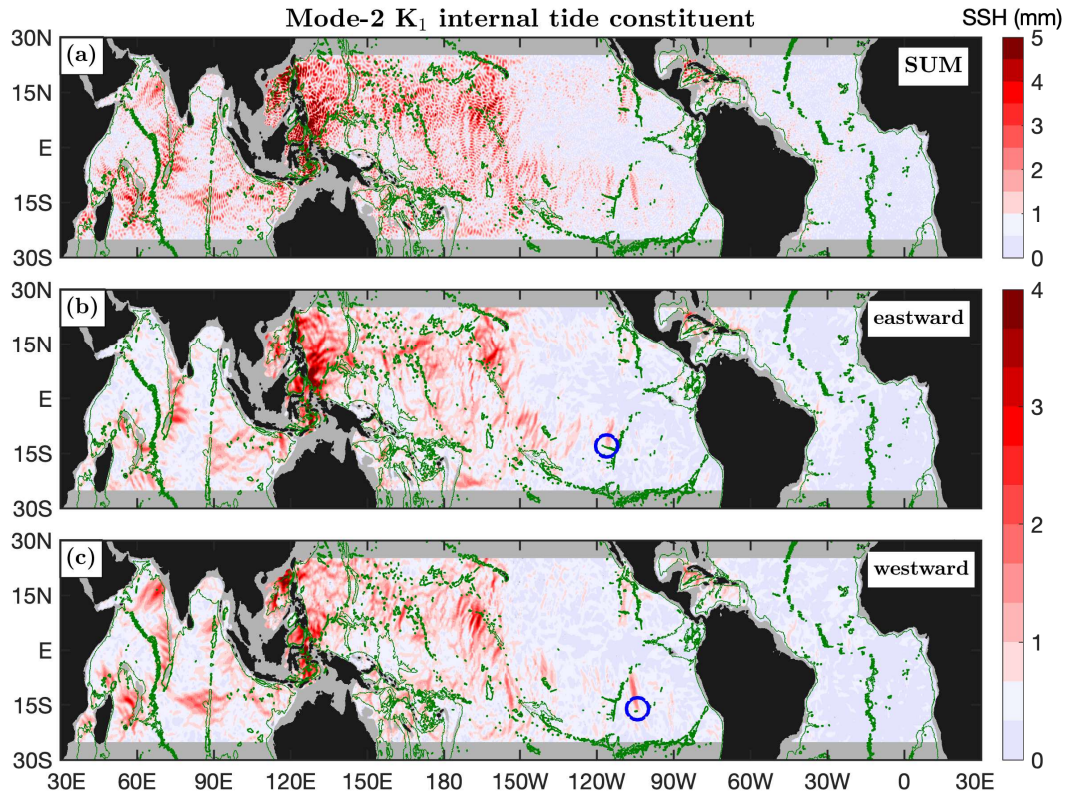


Figure 11. As in Figure 10 but for the mode-2 K_1 internal tide constituent. Blue circles mark two isolated beams in the eastern Pacific Ocean.

5.6 Mode-1 and mode-2 O_1 constituents

Figure 12 shows the mode-1 O_1 constituent and its eastward (-90° – 90°) and westward (90° – 270°) components. The mode-1 O_1 and K_1 constituents have similar spatial patterns (Figures 10 and 12; correlation coefficient is 0.79), but the K_1 constituent

465 is about 50% stronger in amplitude. The decomposed components (Figures 12b, c) reveal numerous well-defined long-range mode-1 O_1 beams. The Luzon Strait generates the strongest mode-1 O_1 internal tides, which propagate eastward into the western Pacific Ocean and westward into the South China Sea. Like mode-1 K_1 beams, the two long-range beams refract in propagation due to the beta effect. The Tonga–Kermadec Ridge radiates a strong northeastward mode-1 O_1 beam, which travels over 2000 km and refracts in propagation. Another similar feature with mode-1 K_1 is that mode-1 O_1 internal tides are weak in the Atlantic Ocean and eastern Pacific Ocean, and strong in the Indian and western Pacific Oceans. In the Indian Ocean, mode-1 O_1 beams are from the Indian western shelf, the Chagos–Laccadive Ridge, the Mascarene Plateau, and the Ninety East Ridge. Although the O_1 amplitudes are low, well-defined mode-1 O_1 beams are observed from the Amazon shelf, the Vitória-Trindade Ridge, and the Sierra Leone Rise in the Atlantic Ocean (Figure 12, blue circles).

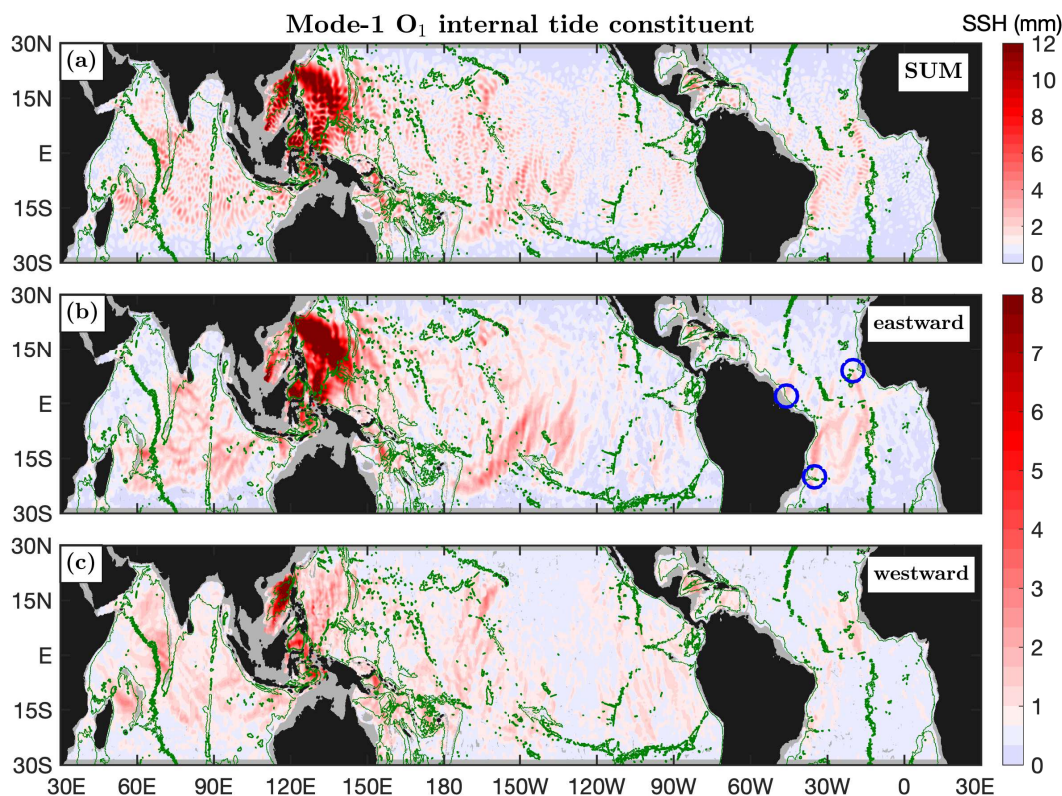


Figure 12. As in Figure 10 but for the mode-1 O_1 internal tide constituent. Blue circles mark isolated mode-1 O_1 beams.

Figure 13 shows the mode-2 O_1 constituent and its eastward (-90° – 90°) and westward (90° – 270°) components. The mode-2 O_1 and K_1 constituents have some degree of similarity, with a correlation coefficient of 0.56. The mode-2 O_1 amplitudes are up to 5 mm around the Luzon Strait. Like other diurnal constituents, the mode-2 O_1 constituent is strong in the Indian and western Pacific Oceans. Strong mode-2 O_1 internal tides occur in the Indonesian Seas and around the Luzon Strait. Mode-2 O_1 beams are also from the Line Islands Ridge and the Izu–Bonin–Mariana Arc. In the eastern Pacific Ocean, there are two

singular mode-2 O_1 beams (Figure 13, blue circles), overlapping with the two mode-2 K_1 beams (Figure 11, blue circles). In the Indian Ocean, mode-2 O_1 beams are from the Indian western shelf, the Chagos–Laccadive Ridge, the Mascarene Plateau, and the Ninety East Ridge (Section 6.2). In the Atlantic Ocean, there is one outstanding beam propagating northward along the Brazilian shelf. In summary, the mode-1 and mode-2 O_1 constituents are similar to the mode-1 and mode-2 K_1 constituents, respectively, but the K_1 constituents are about 50% larger than the O_1 constituents.

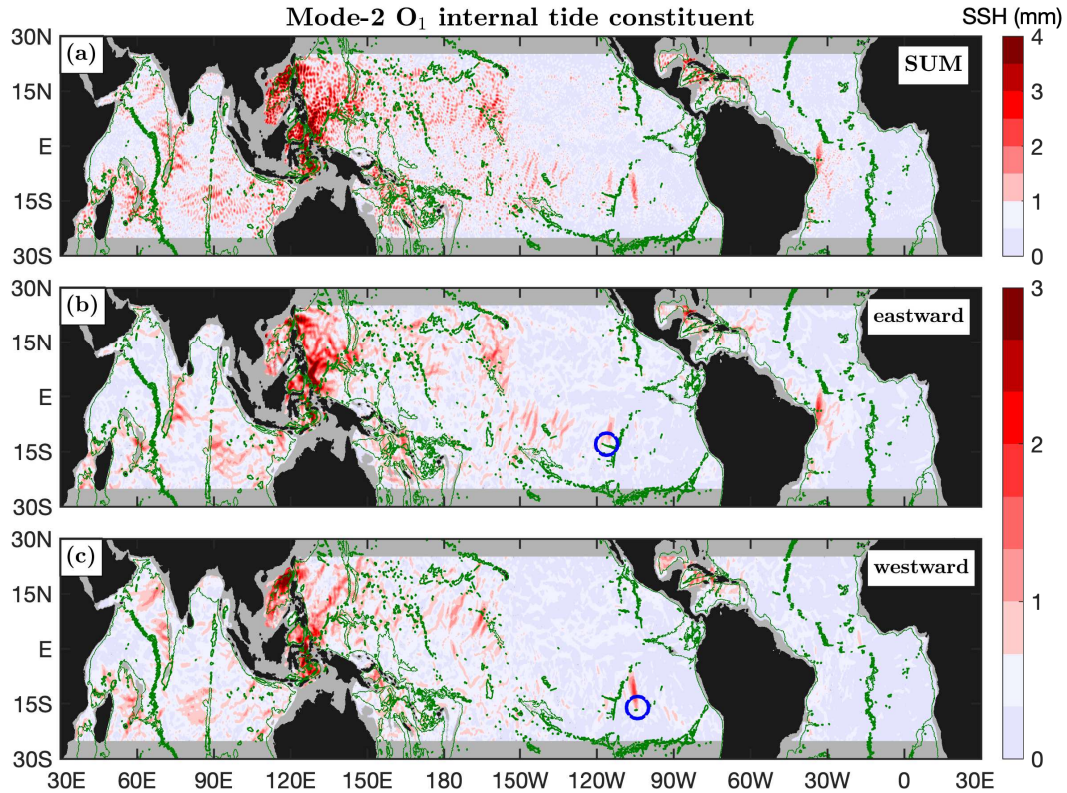


Figure 13. As in Figure 11 but for the mode-2 O_1 internal tide constituent. Blue circles mark two isolated beams in the eastern Pacific Ocean.

5.7 Mode-1 P_1 constituent

Figure 14 shows the mode-1 P_1 constituent and its eastward (-90° – 90°) and westward (90° – 270°) components. The mode-1 P_1 amplitudes can be up to 5 mm. The Luzon Strait is the strongest generation source and radiate mode-1 P_1 beams eastward into the western Pacific Ocean and westward into the South China Sea. The Tango–Kermadec Ridge is another strong generation source and radiates one P_1 beam northeastward. Additionally, mode-1 P_1 beams are observed from the French Polynesian Ridge and the Hawaiian Ridge. In the Indian Ocean, eastward and westward beams radiate from the Ninety East Ridge. The mode-1 P_1 and K_1 constituents have similar spatial patterns and their amplitudes have a scaling factor of about 1/3. Note that

K_1 and P_1 are different by 2 cpy in frequency and their superposition forms a semiannual cycle, which should be accounted in the study of their seasonal variations.

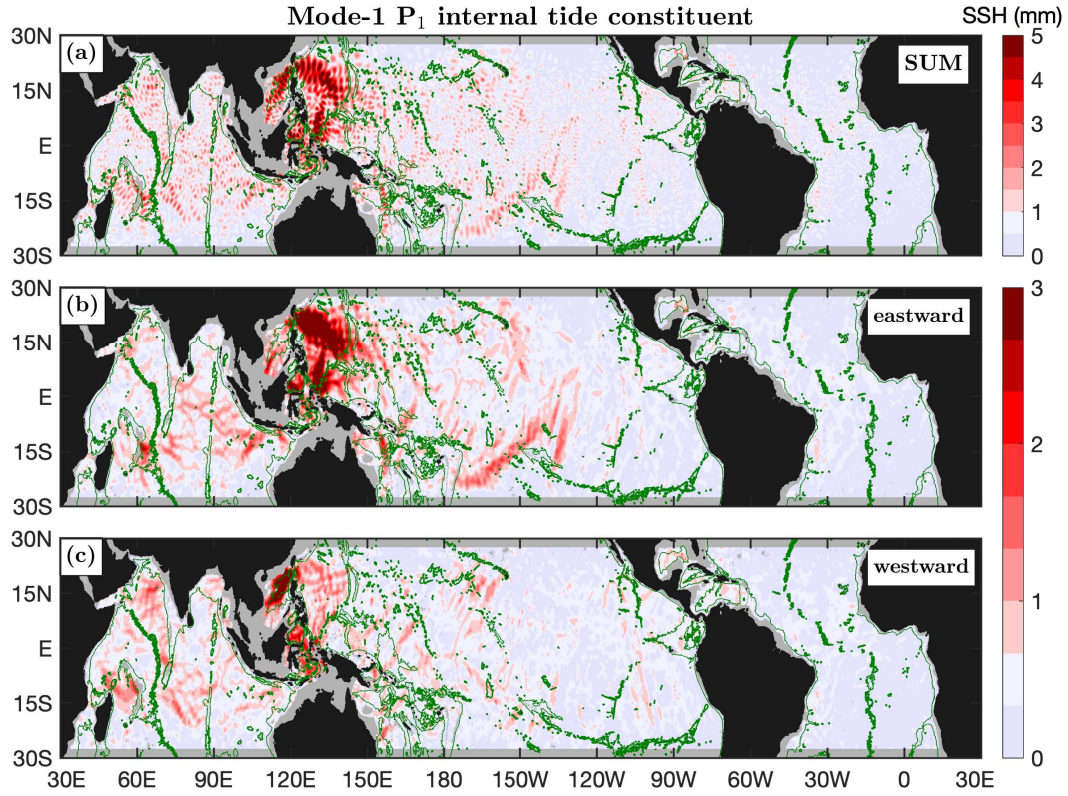


Figure 14. As in Figure 10 but for the mode-1 P_1 internal tide constituent.

5.8 Mode-1 Q_1 constituent

Figure 15 shows the mode-1 Q_1 constituent and its eastward (-90° – 90°) and westward (90° – 270°) components. The mode-1 Q_1 constituent is very weak and its amplitudes are usually lower than 3 mm. The mode-1 Q_1 constituent is overwhelmed by model errors in most of the global ocean. Like other diurnal constituents, the Luzon Strait is the dominant generation source of mode-1 Q_1 beams. The Luzon Strait radiates mode-1 Q_1 beams eastward into the western Pacific and westward into the South China Sea. One can see strong Q_1 internal tides in the Indonesian Seas as well. This feature is consistent with earlier model evaluation (Section 4) that Q_1 can cause variance reduction in the Indonesian Sea and around the Luzon Strait (Figure 3).

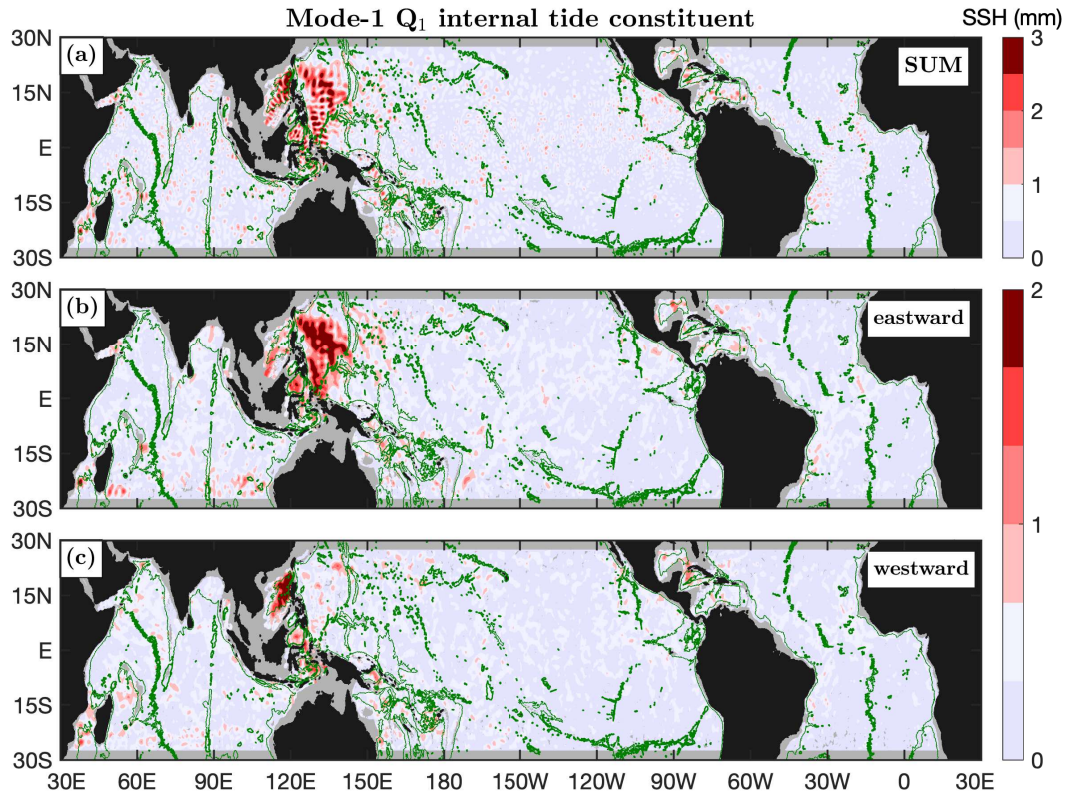


Figure 15. As in Figure 10 but for the mode-1 Q_1 internal tide constituent.

6 Regional Examples

The decomposed components show numerous long-range internal tidal beams, which contain important information on their generation and propagation. To better extract the information, one should study them region by region and beam by beam. This section showcases two examples: the semidiurnal beams off the Amazon shelf and the diurnal beams in the Arabian Sea.

6.1 Semidiurnal internal tidal beams off the Amazon shelf

The Amazon shelf (60° W–35° W, 5° S–20° N) is chosen as an example because of its strong internal tides and frequent occurrence of internal solitary waves (Magalhaes et al., 2016; Barbot et al., 2021; Egbert and Erofeeva, 2021; Tchilibou et al., 2022; de Macedo et al., 2023; Assene et al., 2024). However, previous studies mainly focused on the dominant M_2 internal tides. Here I show internal tidal beams for 6 semidiurnal constituents including mode-1 M_2 , S_2 , N_2 , and K_2 and mode-2 M_2 and S_2 . Figure 16 shows the six internal tide constituents in the region. Each constituent is divided into northeastward and southwestward components. The northeastward component contains the largest waves at each grid point with propagation direction ranging -45° – 135° , and the southwestward component contains the largest waves ranging 135° – 315° (Figure S18).

The six constituents are shown using the same colormap but different ranges, because their amplitudes may vary by an order of magnitude. For all constituents, internal tides with low amplitudes are shown in light blue. The 0° co-phase lines are plotted to highlight internal tidal beams.

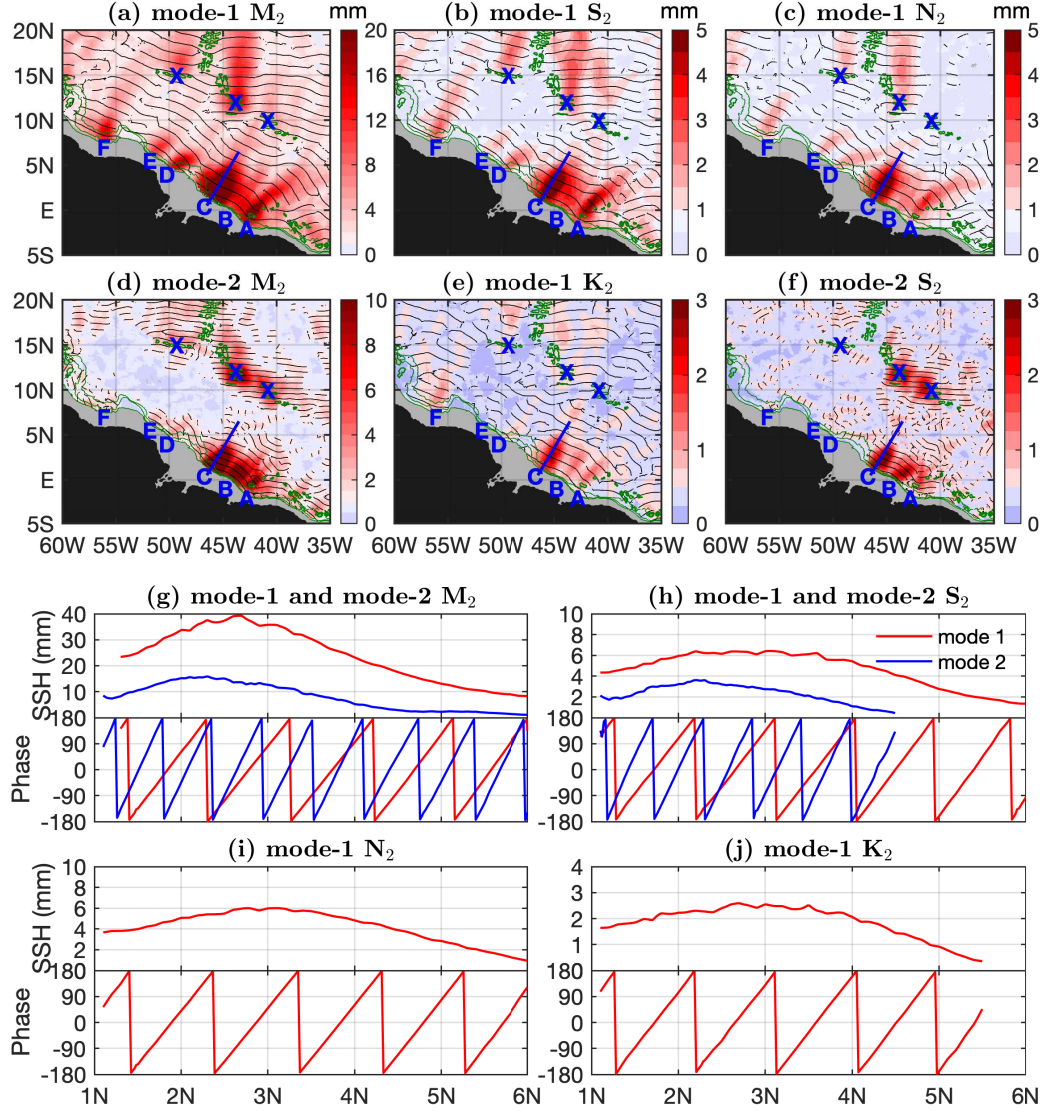


Figure 16. Northeastward semidiurnal internal tidal beams off the Amazon shelf. (a)-(f) Northeastward internal tide components (-45° – 135°). Black lines indicate the 0° co-phase charts. Green contours indicate the 1000-, 2000-, and 3000-m isobaths. Each constituent has up to 6 isolated beams off the Amazon shelf (labeled A–F). Blue lines highlight the strongest beams generated at the mouth of the Amazon River. Beams generated at the Mid-Atlantic Ridge are marked. (g)-(j) Along-beam amplitudes and phases.

515 Compared to the multiwave summed products, the decomposed products present a much clearer view of the isolated internal tidal beams off the Amazon shelf. The four mode-1 constituents (M_2 , S_2 , N_2 , and K_2) have similar spatial patterns. Among them, M_2 , S_2 , and N_2 show 6 isolated internal tidal beams propagating northeastward from the Amazon shelf. They are labeled A–F (Figure 16). The K_2 constituent shows only 5 beams A–D and F. Its beam E is missing, most likely because the much weaker K_2 (lower than 2 mm) is affected by model errors. The co-phase lines are parallel to one another and across the
520 internal tidal beams. For these constituents, the strongest beams (blue lines) radiate from the mouth of the Amazon River. The along-beam amplitudes and phases are shown in Figures 16g–j. One can see that their amplitudes are smooth and their phases increase linearly with propagation. These features suggest that these beams are successfully extracted. Otherwise, they would show standing-wave features (half-wavelength fluctuations). Along the strongest beams, their amplitudes range from 40 mm for M_2 to 3 mm for K_2 . The strongest M_2 beam can be tracked for about 700 km from the Amazon shelf to the
525 Mid-Atlantic Ridge. For comparison, the S_2 , N_2 , and K_2 beams disappear sooner, likely because their lower amplitudes are masked by the still large model errors. In addition, my satellite observations also reveal internal tidal beams generated over the Mid-Atlantic Ridge (Figure 16, ‘X’). Maximum SSH amplitudes along all beams do not appear on the Amazon shelf, but about one wavelength away from their source. It is likely an artificial feature caused by the large spatial windows used in plane wave fitting and Fourier bandpass filtering. It is also likely because the distances are needed for the internal tidal rays bounce
530 to the sea surface for the first time (Merrifield and Holloway, 2002; Carter et al., 2008).

Our satellite observations are generally consistent with previous numerical simulations, which mainly focused on M_2 internal tides. Isolated M_2 internal tidal beams are observed by Tchilibou et al. (2022, Figure 7) and Assene et al. (2024, Figure 2). For example, Tchilibou et al. (2022) identified 6 strong internal tidal beams off the Amazon shelf. Their generation sites are consistent with satellite observations. One exception is that they suggest the strong beam (Figure 16a, beam C) is composed of
535 two beams. Previous studies found that the strong beams overlap with internal solitary waves very well, in that internal solitary waves are generated by nonlinear internal tides. Tchilibou et al. (2022) showed the temporal variation of internal tides in two contrasting time periods September–November and March–June. Likewise, M_2 internal tide maps have been constructed using four seasonal subsets (Zhao, 2021) and decadal maps (Zhao, 2023a). It is interesting to compare the satellite observations, numerical models, semi-analytical, and in situ measurements in future research (Pollmann and Nycander, 2023; Assene et al.,
540 2024; Zaron and Elipot, 2024; Geoffroy et al., 2025). The 6 beams are spatially collocated for the four constituents, suggesting that they are generated by the same topographic features. Their superposition will lead to the temporal variability of semidiurnal internal tides (strong beats and weak beats).

Our decomposed products also reveal mode-2 M_2 and S_2 internal tidal beams (Figures 16d, f). Both constituents show three beams A–C. There are no outstanding mode-2 beams at E–G. Figures 16g and 16h show the along-beam amplitudes and
545 phases for mode-2 M_2 and S_2 (blue lines). It shows that the mode-2 M_2 amplitudes may be up to 15 mm, and the mode-2 S_2 amplitudes are up to 4 mm. Similarly, the mode-2 beams have large and smooth amplitudes and their phases increase linearly with propagation. The mode-2 M_2 constituent is larger than mode-1 S_2 and N_2 constituents; therefore, the missing beams D–F are not likely because of its weak signals. Rather, it is likely that the local specific topography favors the generation of mode-1 constituents, but not mode-2 constituents.

The westward diurnal internal tidal beams in the Arabian Sea are examined next. In this region, the dominant M_2 internal tides have been well documented in previous studies (Kaur et al., 2024; Ma et al., 2021; Subeesh and Unnikrishnan, 2016; Subeesh et al., 2021; Zhao, 2021). Figure 17 shows the lowest two modes of the diurnal O_1 and K_1 constituents. Each constituent is divided into eastward and westward component. The eastward component contains the largest waves at each grid point ranging
 555 -90° – 90° (Figure S19), and the westward component contains the largest waves ranging 90° – 270° . Overlain are the 0° and 180° co-phase lines. The intervals between two neighboring co-phase lines are half one wavelength. Topographic features are indicated by the 1000-, 2000-, and 3000-m isobaths. My new model reveals isolated long-range internal tidal beams for both O_1 and K_1 .

Figure 17 shows that diurnal internal tides have two outstanding generation sites. One set of beams originate at the Indian
 560 western shelf along 15° – 20° N. The beams propagate toward 210° for about 2000 km long from the Indian coast to the Carlsberg Ridge. It takes about 6 (10) repeat diurnal tidal cycles for mode-1 (mode-2) K_1 and O_1 internal tides to travel cross the distance. Another set of beams radiate from the Chagos–Laccadive Ridge (along 73° E) and travel over 1000 km before disappearance. The mode-2 beams from the Chagos–Laccadive Ridge appear to be composed of several isolated narrow beams (blue circles). Note that the two generation sites also generate strong M_2 internal tides (Subeesh et al., 2021; Ma et al., 2021).
 565 For comparison, the diurnal internal tidal beams are wider than semidiurnal beams. The southwestward mode-2 beams from the Indian western shelf are about 500 km wide.

Figures 17e and 17f show along-beam amplitudes and phases for the first two modes of the K_1 and O_1 constituents. Their smooth amplitudes and linear-increasing phases suggest that the beams have been successfully separated. The diurnal internal tidal beams have small amplitudes, ranging from 4 mm for mode-1 K_1 to 1 mm for mode-2 O_1 internal tides. This feature
 570 again suggests that my new internal tide model has low model errors. However, the even weaker P_1 and Q_1 constituents (lower than 1 mm) do not show well-defined internal tidal beams (Figures 14 and 15). The regional maps reveal isolated beams and generation sites. Such an examination can be conducted constituent by constituent and region by region.

7 Summary

In this work, I have mapped global internal tides by applying my recently improved mapping technique to 30 years of satellite
 575 altimetry data from 1993 to 2022 (Figure 1). My mapping technique consists of two rounds of plane wave analysis with a spatial bandpass filter in between (Zhao, 2022a, b). The data record is 120 satellite years long, including all the nadir altimetry data made by 15 altimetry mission. My main findings and conclusions are summarized as follows:

1. I have constructed a new internal tide model that contains 12 internal tide constituents (Figure S3): 8 mode-1 constituents (M_2 , S_2 , N_2 , K_2 , K_1 , O_1 , P_1 , and Q_1) and 4 mode-2 constituents (M_2 , S_2 , K_1 , and O_1). The combination of long data
 580 record and improved mapping technique significantly suppresses model errors down to lower than 1 mm on a global average (Figure 2), which makes it possible to map weak mode-2 and minor internal tide constituents.

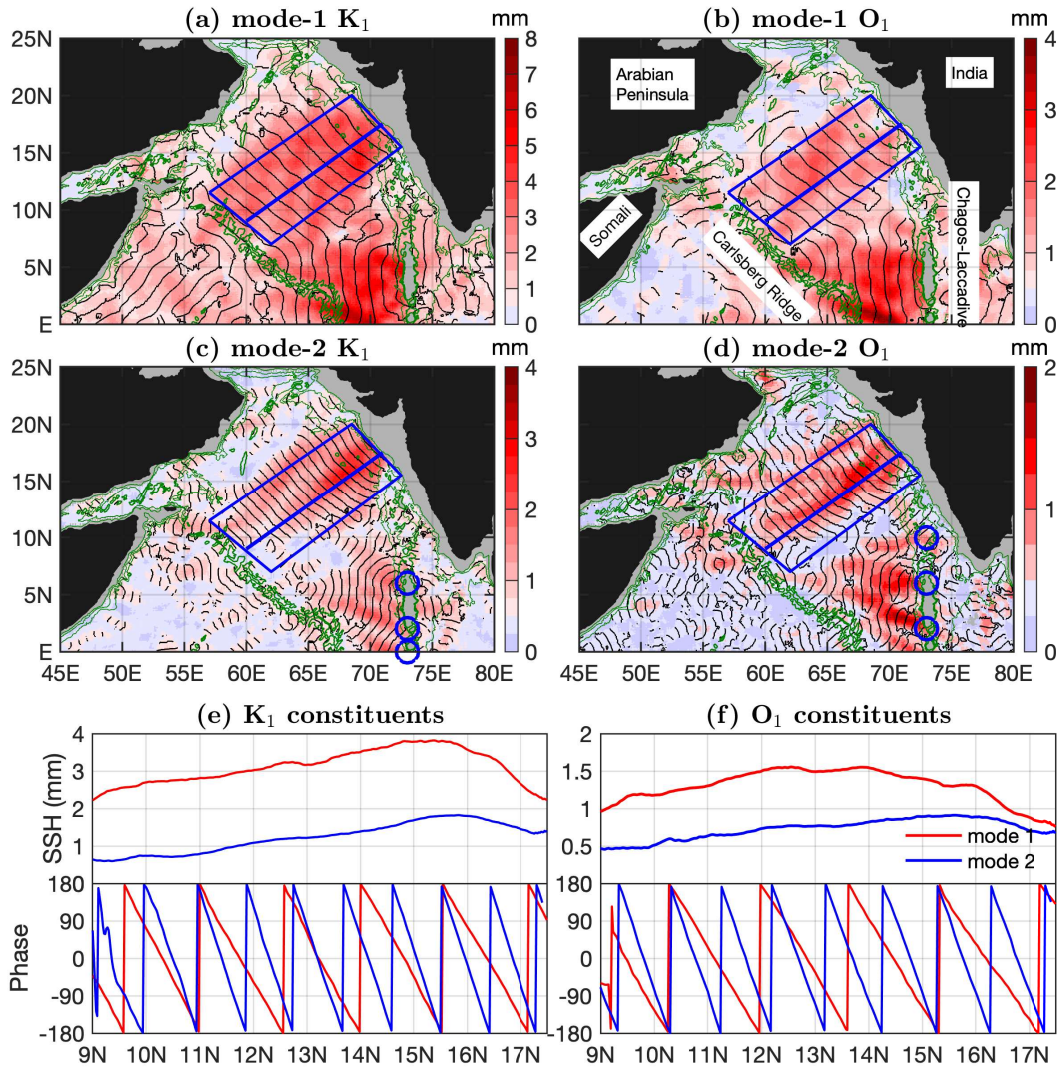


Figure 17. Westward diurnal internal tidal beams in the Arabian Sea. (a)-(d) Westward internal tide components (90° – 270°). Black lines indicate the 0° and 180° co-phase charts. Internal tides with amplitudes lower than 0.5 mm are shown in light blue. Green contours indicate the 1000-, 2000-, and 3000-m isobaths. Blue circles mark some isolated mode-2 beams at the Chagos–Laccadive Ridge. (e, f) Along-beam amplitudes (averaged across the beam) and phases (along the central line).

- I have decomposed the multiconstituent multimodal multidirectional internal tide field into a series of simple plane waves. In frequency, eight principal constituents are extracted. In the vertical direction, two lowest baroclinic modes are extracted for the four major constituents. In the horizontal direction, each internal tide constituent is decomposed into 5 plane waves in different directions. All together, the internal tide field is decomposed into 60 plane waves at each grid point (Figures S4–S15). The multiwave decomposition reveals a new view of the global internal tide field.

3. I have validated the new internal tide model using independent altimetry data in 2023 (Figure 3). On a global average, ten constituents (but for K_2 and Q_1) can cause positive variance reductions, because these constituents are sufficiently strong to overcome model errors. The weak K_2 and Q_1 constituents can overcome model errors near their sources in the western Pacific Ocean.
4. I have shown that ZHAO30yr performs much better than ZHAO20yr (Figures S16 and S17), a model developed using 20 years of altimetry data by an obsolete mapping technique (Zhao et al., 2016). The improvement is mainly because ZHAO30yr is developed using a longer data record and an improved mapping technique.
5. I have observed numerous isolated internal tidal beams for all 12 internal tide constituents. Their decomposed components reveal well-defined long-range internal tidal beams (Figures 4–15). These beams are associated with notable topographic features. For all constituents, mode-2 beams are shorter and narrower than corresponding mode-1 beams. One can acquire important information on their generation, propagation, and dissipation by tracking these long-range internal tidal beams.
6. I have studied the semidiurnal internal tidal beams off the Amazon shelf (Figure 16). For mode-1 constituents (M_2 , S_2 , N_2 , and K_2), six isolated beams propagating northeastward off the Amazon shelf have been recognized. Along the strongest beams from the mouth of the Amazon River, their amplitudes range from 40 mm for M_2 to 3 mm for K_2 . For mode-2 M_2 and S_2 constituents, there are three isolated beams off the Amazon shelf.
7. I have studied the diurnal internal tidal beams in the Arabian Sea (Figure 17). For both mode-1 and mode-2 O_1 and K_1 constituents, westward beams radiate from the Indian western shelf and the Chagos–Laccadive Ridge. Their along-beam amplitudes range from 4 mm for mode-1 K_1 to 1 mm for mode-2 O_1 . Isolated mode-2 O_1 and K_1 beams are from the Chagos–Laccadive Ridge.

8 Limitations and Perspectives

ZHAO30yr has its limitations stemming from (1) the complex nature of the global internal tide field and (2) the spatially and temporally under-sampling by satellite altimetry. Would the internal tide field be sufficiently sampled in time and space, mapping internal tides is not a problem anymore. I notice three major limitations in the model. First, ZHAO30yr only extracts the 30-year phase-locked internal tides, missing the incoherent component caused by the time-varying ocean environment. There exist some mitigation methods. Incoherent internal tides can be mapped from the de-correlation of covariance (Zaron, 2015; Buijsman et al., 2017; Geoffroy and Nycander, 2022). The seasonal, inter-annual, and decadal variations of internal tides can be mapped using subsetted satellite altimetry data (Zhao, 2021, 2022a, 2023a). Second, ZHAO30yr is constructed using empirical mapping parameters (Table 1). These parameters are tested and chosen for mapping internal tides on a global scale; however, they are not necessarily the best choices in one given region. Regional internal tide models can be further improved by optimizing these mapping parameters. Third, ZHAO30yr still has large model errors. ZHAO30yr has significantly reduced

model errors to lower than 1 mm; however, the model errors are still large for the minor and mode-2 internal tide constituents. In most of the global ocean, the minor and mode-2 constituents in ZHAO30yr are just slightly larger than model errors. Future
620 efforts are needed to further reduce model errors to obtain reliable high-mode internal tides.

The advances in mapping internal tides by satellite altimetry are attributed to the multiyear multimission accumulation of satellite altimetry data. All empirical internal tide models are limited by the spatially and temporally low sampling rates of the conventional nadir-looking altimetry. Since December 2022, the new Surface Water and Ocean Topography (SWOT) mission has been measuring SSH along a 120-km swath using the Ka-band Radar Interferometer (KaRIn) technique (Fu et al., 2024).
625 The SWOT SSH measurements have instrumental errors about one order of magnitude lower than the conventional radar technique. Recent studies have demonstrated that SWOT greatly improves our capability of mapping internal tides (Zhao, 2024a; Tchilibou et al., 2025). However, SWOT has a repeat cycle of about 21 days. In each cycle, SWOT samples one given position from once at low latitudes to ~ 20 times at high latitudes (Morrow et al., 2019). The low temporal sampling rate is still an issue for high-frequency internal tides. SWOT thus poses new challenges as well as offers a great opportunity for mapping
630 internal tides by satellite altimetry.

9 Data availability

The internal tide model ZHAO30yr is available at <http://doi.org/10.6084/m9.figshare.28078523.v1> (Zhao, 2024b). Model errors are available at <https://doi.org/10.6084/m9.figshare.28559978.v3> (Zhao, 2025).

Author contributions. The model was developed and the paper was written by the sole author.

635 *Competing interests.* The author has declared that there are no competing interests.

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