



- 1 Global ocean surface heat fluxes revisited: A new dataset
- 2 from maximum entropy production framework with heat

# 3 storage and Bowen ratio optimizations

- 4 Yong Yang<sup>1</sup>, Huaiwei Sun<sup>1,2,3,4\*</sup>, Jingfeng Wang<sup>5</sup>, Wenxin Zhang<sup>6</sup>, Gang Zhao<sup>7</sup>, Weiguang
- 5 Wang<sup>8</sup>, Lei Cheng<sup>9</sup>, Lu Chen<sup>1</sup>, Hui Qin<sup>1</sup>, Zhanzhang Cai<sup>6</sup>
- <sup>1</sup>School of Civil and Hydraulic Engineering, Huazhong University of Science and Technology, Wuhan
   430074, China
- 8 <sup>2</sup>Hubei Key Laboratory of Digital River Basin Science and Technology, Huazhong University of Science and
- 9 Technology, Wuhan 430074, China
- 10 <sup>3</sup>Institute of Water Resources and Hydropower, Huazhong University of Science and Technology, Wuhan
- 11 430074, China
- 12 <sup>4</sup>College of Water Conservancy & Architectural Engineering, Shihezi University
- 13 <sup>5.</sup> School of Civil and Environmental Engineering, Georgia Institute of Technology, Atlanta 30318, USA
- <sup>6.</sup> Department of Physical Geography and Ecosystem Science, Lund University, Sweden
- 15 <sup>7.</sup> Key Laboratory of Water Cycle and Related Land Surface Processes, Institute of Geographic Sciences and
- 16 Natural Resources Research, Chinese Academy of Sciences, Beijing, China
- 17 <sup>8.</sup> College of Hydrology and Water Resources, Hohai University, Nanjing 210098, China
- <sup>9</sup> State Key Laboratory of Water Resources and Hydropower Engineering Science, Wuhan University,
- 19 Wuhan, China
- 20 Correspondence to: Huaiwei Sun (hsun@hust.edu.cn) and Wenxin Zhang (wenxin.zhang@nateko.lu.se)

21 Abstract. Ocean evaporation (latent heat flux, LE) plays a crucial role in global precipitation patterns, water 22 cycle dynamics, and energy exchange processes. However, current bulk methods for quantifying ocean 23 evaporation are subject to significant uncertainties. The Maximum Entropy Production (MEP) theory offers 24 a novel approach for estimating surface heat fluxes, but its effectiveness over ocean surfaces has not been 25 validated. This study integrates heat storage effects and four empirical Bowen ratio formulas into the MEP 26 theory to improve ocean LE estimation. We employed multi-source data from 129 globally distributed buoy 27 stations and seven auxiliary turbulent flux datasets for validation and comparison. We first evaluated the 28 MEP method using observed data from buoy stations, identifying the optimal Bowen ratio formula to enhance 29 the model. Results indicate that accounting for heat storage and adjusting the Bowen ratio significantly 30 improve heat flux accuracy, with R<sup>2</sup>=0.99 and a root mean squared error (RMSE) of 4.7 W·m<sup>-2</sup> compared to 31 observations. Subsequently, we conducted a thorough evaluation of seven global turbulent flux datasets to 32 identify the most accurate input variables (e.g., heat storage, net radiation, surface temperature) for applying 33 the MEP method on a global ocean scale. The enhanced MEP method provided new estimates of the annual





34 average LE at 93 W·m<sup>-2</sup> and sensible heat at 12 W·m<sup>-2</sup> for the period 1988 to 2017. Validation against 35 observations from 129 buoy stations demonstrated that the MEP-derived latent heat dataset achieved the highest accuracy, with a mean error (ME) of 1.3 W m<sup>2</sup>, an RMSE of 15.9 W m<sup>2</sup>, and a Kling-Gupta 36 37 Efficiency (KGE) of 0.89, outperforming four major long-term global heat flux datasets, including J-38 OFURO3, ERA5, MERRA2, and OAFlux. Additionally, we examined the long-term spatiotemporal 39 variability of global ocean evaporation, identifying a significant increasing trend from 1988 to 2010 at a rate 40 of 3.58 mm/yr, followed by a decline at a rate of -2.18 mm/yr from 2010 to 2017. The current dataset provides 41 a new benchmark for the ocean surface energy budget and is expected to be valuable for research on global 42 ocean warming, sea surface-atmosphere energy exchange, the water cycle and climate change. The monthly 43 MEP 1988-2017 heat flux dataset for is publicly available at 44 https://doi.org/10.6084/m9.figshare.26861767.v2 (Yang et al., 2024, last access: 28 August 2024).

#### 45 1. Introduction

46 The ocean system plays a pivotal role in regulating the global climate by receiving and redistributing 47 heat and freshwater, thereby influencing Earth's energy balance and the dynamics of the water cycle (Li et 48 al., 2023; Von Schuckmann et al., 2023; Marti et al., 2022; Johnson et al., 2020). A key component of this 49 regulation is ocean evaporation (latent heat), which accounts for approximately 86% of atmospheric water vapor and is the primary driver of the global hydrological cycle (Yu, 2011). As climate change warms the 50 51 ocean, evaporation rates are anticipated to rise, potentially intensifying the global hydrological cycle 52 (Masson-Delmotte et al., 2021). This intensification could alter precipitation patterns, affecting regional 53 water availability and freshwater ecosystems (Konapala et al., 2020; Roderick et al., 2014). Therefore, precise 54 estimation of ocean evaporation is critical to understand and quantify the global energy and water budget 55 (Iwasaki et al., 2014).

56 Current methods for calculating surface latent heat (LE) and sensible heat flux (H) employ bulk transfer 57 formulations that necessitate extensive parameterization inputs, including temperature gradients, humidity 58 gradients, wind speed, and transfer coefficients (Fairall et al., 1996; Andreas et al., 2008). Despite their 59 widespread application, these bulk methods encounter significant limitations primarily due to challenges in 60 accurately parameterizing and empirically deriving coefficients (Zeng et al., 1998; Robertson et al., 2020). 61 These methods heavily depend on assumptions regarding atmospheric stability and boundary layer dynamics, 62 which may not consistently apply across diverse and complex environmental conditions (Fairall et al., 2003; 63 Andreas et al., 2013). Furthermore, uncertainties in estimating turbulent transfer coefficients can lead to





64 substantial errors in the estimation of latent heat flux. The high demands for parameterization and challenges 65 in data acquisition contribute to considerable uncertainties when implementing bulk methods for calculations. 66 While numerous energy balance-based algorithms have been developed to estimate global terrestrial 67 evapotranspiration (Wang et al., 2012; Yang et al., 2023), similar efforts to apply these algorithms for 68 estimating ocean surface heat flux remain unexplored. Therefore, proposing an innovative method for 69 estimating ocean surface heat flux based on rational surface energy allocation could yield significant 70 theoretical and practical implications. This approach may serve as an additional reference source for existing 71 bulk methods and their derived datasets, offering a new methodological perspective for quantifying the 72 uncertainty of ocean heat flux estimation. Ultimately, this could facilitate more accurate ocean flux estimation 73 and enhance research on ocean energy allocation patterns.

74 The Maximum Entropy Production (MEP) model, an energy-balance-based approach, has recently 75 emerged as a novel method for simulating surface heat fluxes. Developed from Bayesian probability theory 76 and information theory, it prioritizes the most probable partitioning of radiation fluxes (Wang & Bras, 2011). 77 The MEP model has been rigorously validated across diverse surface types and varying degrees of surface 78 wetness (Wang et al., 2014; Huang et al., 2017; Yang et al., 2022; Sun et al., 2022; Sun et al., 2023). Notably, 79 the MEP model requires fewer input variables-net radiation, surface temperature, and specific humidity-80 yet provides accurate estimates of latent heat, sensible heat, and ground heat fluxes simultaneously. Unlike 81 bulk methods (Fairall et al., 2003), which rely on wind speed, temperature gradient, and humidity gradient, 82 the MEP model satisfies the energy balance constraint without these dependencies. This characteristic 83 enhances its applicability and robustness across diverse environmental conditions. However, the previous 84 application of the MEP model over ocean surfaces has revealed significant limitations, including notable 85 underestimations of latent heat and overestimations of sensible heat flux (Huang et al., 2017). The global 86 multi-year averaged LE estimated by the MEP model indicates a value around 58 W m<sup>-2</sup>, much lower than 87 the range of 92~109 W·m<sup>-2</sup> reported by other remote sensing or reanalysis-based products. Conversely, MEP 88 estimates an averaged H of approximately 28 W·m<sup>-2</sup>, which is significantly higher compared to values ranging from 6 to 18 W·m<sup>-2</sup> found in other products. These discrepancies highlight substantial uncertainties 89 90 in applying the MEP model to oceanic energy partitioning, highlighting the urgent need for further refinement 91 and rigorous validation efforts.





92	The Bowen ratio $(B_o)$ , defined as the ratio of sensible heat to latent heat flux $(B_o = H/LE)$ , is crucial for
93	understanding the energy partitioning process (Hicks & Hess, 1977). In the context of the energy balance-
94	based MEP model, the significant overestimation of $B_o$ suggests that focusing on this ratio can enhance our
95	understanding of energy partitioning dynamics (Andreas et al., 1996). Studies have highlighted that the actual
96	Bowen ratio over ocean surfaces ( $B_{oa}$ ) often diverges from the equilibrium Bowen ratio ( $B_o^*$ ) observed under
97	ideal conditions where the air is saturated with water vapor. The $B_{oa}$ may deviate significantly from $B_o^*$ under
98	non-equilibrium conditions, which are typical in most environments (Jo et al., 2002; Andreas et al., 2013),
99	posing challenges in establishing a robust relationship between $B_{oa}$ and $B_{o}^{*}$ (Liu & Yang, 2021). Therefore,
100	developing an accurate $B_o^* \sim B_{oa}$ relationship is crucial for refining the energy partitioning process in the
101	MEP model. The advancement of buoy observation networks has provided compelling evidence for
102	validating ocean heat fluxes and has become crucial in assessing their associated uncertainties (Bourras, 2006;
103	Smith et al., 2011; Bentamy et al., 2017; Liang et al., 2022; Tang et al., 2023). This study utilizes the energy
104	balance-based MEP method to estimate ocean evaporation, introducing a novel approach to redistributing
105	surface energy budgets and offering a streamlined parameterization scheme distinct from conventional bulk
106	methods used for estimating ocean heat fluxes. In contrast to existing approaches that using reanalysis-based
107	schemes (e.g., NCEP, ECMWF, and GEOS) and their associated parameterizations (Tang et al., 2024) to
108	estimate LE, this study employs satellite observations to directly estimate ocean heat fluxes, thereby
109	minimizing error propagation associated with the model structures and assimilation schemes.

The primary objectives of this study are as follows: (1) to develop and validate the MEP approach for estimating ocean heat fluxes using observations from 129 stations; (2) to investigate the impact of heat storage on ocean energy allocation and the influence of the Bowen ratio on energy partitioning for heat flux estimations; (3) to produce a MEP-derived ocean heat fluxes product (spatial resolution: 0.25°; temporal coverage: 1988-2017) and present its spatiotemporal patterns.

## 115 **2. Methods**

## 116 2.1 Components of ocean surface energy balance

117 The global ocean energy balance equation is as follows (Meehl, 1984; Wang et al., 2021):

$$R_n = LE + H + G \tag{1}$$





119	$R_n = R_{ns} + R_{nl} = R_s^{\downarrow} - R_s^{\uparrow} + R_l^{\downarrow} - R_l^{\uparrow} $ <sup>(2)</sup>
120	where $R_n$ , $R_{ns}$ , $R_{nl}$ are net radiation, net shortwave radiation (the difference of incoming radiation $R_s^{\downarrow}$
121	and reflected solar radiation $R_s^{\uparrow}$ ), and net longwave radiation (the difference of incoming longwave radiation
122	$R_l^{\downarrow}$ and outgoing longwave radiation $R_l^{\uparrow}$ ), H is sensible heat, LE is latent heat, and G is the heat flow
123	through the surface. Unlike terrestrial surfaces, the energy balance equation for the ocean surface accounts
124	for distinct energy exchange processes, including the impact of seawater mixing and dynamics on energy
125	transfer. For the ocean surface, the flux term G has two components,
126	$G = G_t + G_v \tag{3}$
127	where $G_t$ is the change in the ocean heat content ( $\Delta OHC$ , or heat storage), and $G_v$ is the lateral heat
128	transported by ocean currents and other processes. The $G_t$ can be quantified as the vertical integration of
129	temperature profile in a column of depth (Meehl ,1984, Li et al., 2023). Both the heat storage and the ocean
130	heat transport $G_{\nu}$ are difficult to quantify, which requires large masses of hydrographic variables and
131	performing integrations at different depths. Since the previous study overlooked the calculation of
132	evaporation on a global scale (Wang et al., 2021), leading to the G flux being equal to heat storage. For the
133	convenience in description, this study will consider the concept of G flux as equivalent to heat storage.
134	

#### 135 2.2 The Maximum Entropy Production theory

#### 136 2.2.1 The original MEP model

The MEP model simulate ocean surface heat fluxes using inputs variables of net radiation  $(R_n)$ , surface skin 137 temperature  $(T_s)$ , and surface specific humidity  $(q_s)$  under the constraint of the surface energy balance. The 138 latent heat, sensible heat, and surface thermal energy flux (Q) are calculated as, 139

140 
$$[1+B(\sigma) + \frac{B(\sigma)}{\sigma} \frac{I_s}{I_0} |H|^{-\frac{1}{6}}]H = R_n$$
(4)

141 
$$E = B(\sigma)H \tag{5}$$

$$Q = R_{nl} - E - H \tag{6}$$





$$B(\sigma) = 6(\sqrt{1 + \frac{11}{36}\sigma} - 1), \quad \sigma = \frac{\lambda^2}{c_p R_v} \frac{q_s}{T_s^2}$$
(7)

$$I_{0} = \rho_{a}c_{p}\sqrt{C_{1}kz}\left(C_{2}\frac{kzg}{\rho_{a}c_{p}T_{r}}\right)^{\frac{1}{6}}$$
(8)

145 where  $B(\sigma)$  is the reciprocal Bowen ratio,  $\sigma$  is a dimensionless parameter that characterizes the phase change at the ocean surface,  $\lambda$  (J·kg<sup>-1</sup>) is the latent heat of vaporization of liquid surface,  $C_n$  (10<sup>3</sup> J·kg<sup>-1</sup>·K<sup>-1</sup>) 146 is the specific heat of air under constant pressure, and  $R_{\nu}$  (461 J·kg<sup>-1</sup>·K<sup>-1</sup>) is the gas constant of water vapor. 147 148  $I_0$  is the "apparent thermal inertia" of air and describes the turbulent transport process of the boundary layer 149 based on the Monin-Obukhov similarity theory (MOST) (Wang and Bras, 2010).  $I_s$  is the thermal inertia of the ocean surface (J·m<sup>-2</sup>·K<sup>-1</sup>·s<sup>-1/2</sup>), and can be parametrized as  $I_s = \sqrt{\rho c \lambda}$  (with density  $\rho$ , the specific 150 heat c) represents the physical property of surface ( $I_s = 1.56 \times 10^3 \, \text{J} \cdot \text{m}^{-2} \cdot \text{K}^{-1} \cdot \text{s}^{-1/2}$  for water surface and 151  $1.92 \times 10^3$  J·m<sup>-2</sup>·K<sup>-1</sup>·s<sup>-1/2</sup> for ice surface). 152 153 Over the sea ice surface, assumed to be saturated, the specific humidity  $q_s$  can be derived as a function 154 of surface temperature  $T_s$  using the Clausius-Clapeyron equation. (El Sharif et al., 2019; Shaman & Kohn, 155 2009).

156 
$$q_s = \varepsilon \frac{e_s(T_s)}{P} = \varepsilon \frac{e_0}{P} \exp[\frac{\lambda_s}{R_v}(\frac{1}{T_0} - \frac{1}{T_s})]$$
(9)

where  $\varepsilon$  (= 0.622) represents the ratio of the molecular weight of water vapor to that of dry air,  $e_s(T_s)$ denotes the saturation vapor pressure at temperature Ts,  $e_0$  is the saturation vapor pressure at the reference temperature  $T_0$  (273.15 K), and P is the atmospheric pressure (mb).

## 160 2.2.2 Specific improvements on the MEP model

161 Equations (4) ~ (9) presented above represent the original formulas of the MEP model. According to the

- 162 MEP theory, the net solar radiation  $(R_{ns})$  entering the water surface medium is absorbed by the water body,
- 163 with the allocable radiation flux denoted as  $R_{nl} = E + H + Q$  (Eq.6). Consequently, the expression for

144





164 ocean heat uptake (heat storage) is derived as  $G = R_n - E - H = R_{ns} + Q$ . While this theory has received 165 preliminary validation in shallower water bodies, such as lake surfaces (Wang et al., 2014), its applicability 166 on deeper water bodies with larger heat storage capacities in ocean surfaces requires further evaluation. This 167 study introduces two key hypotheses: (1) The substantial heat storage capacity of the ocean can exert a 168 significant influence on seasonal latent and sensible fluxes, potentially introducing bias to the MEP equations, 169 (2) The notable underestimation of latent heat flux and overestimation of sensible heat flux by the MEP 170 model point to a significant deviation from the Bowen's ratio formula, necessitating a reasonable correction. 171 To address this, the study proposes two approaches for enhancing the MEP formulas: (1) Considering the 172 impact of heat storage in the MEP's energy balance equation, and (2) Adjusting the theoretical equilibrium 173 Bowen ratio within the MEP model. This can be specifically represented as follows:

174 
$$[1 + \frac{1}{B_o^*}]H = R_n - G$$
 (10)

175 
$$B_o^* = \frac{1}{B(\sigma)}$$
(11)

$$B_{oa} = a \times B_o^* + b \tag{12}$$

where  $B_o^*$  is the equilibrium Bowen ratio, which denotes the theoretical ratio of sensible heat flux to latent heat flux when the surface and the atmosphere are in equilibrium regarding water vapor. Correspondingly, the corresponding evaporation at this condition is known as equilibrium evaporation (defined as the water vapor evaporating from a saturated surface into a saturated atmosphere). To accurately predict actual evaporation, a reliable functional relationship needs to be established to predict  $B_{oa}$  from  $B_o^*$ . Empirical studies have introduced coefficients to correlate  $B_o^*$  to  $B_{oa}$  under diverse environmental circumstances; for instance, the Priestley–Taylor coefficient is expressed as (Priestley & Taylor, 1972).

184 
$$B_{oa} = 0.79 \times B_{o}^{*} - 0.21 = \frac{0.79 - 0.21 \times B(\sigma)}{B(\sigma)}$$
(13)

Further studies have led to the emergence of more updated empirical coefficients. Hicks and Hess (1977) estimated the actual Bowen ratio as  $B_{oa} = 0.63 \times B_o^* - 0.15$  by aligning it with direct observations of the fluxes. Yang & Roderick (2019) deduced an empirical coefficient of 0.24 and formulated it as





 $B_{oa} = 0.24 \times B_o^*$  through fitting Bowen ratio and surface temperature data across the global ocean surface. 188 189 Furthermore, Liu & Yang (2021) derived a new equation as  $B_{oa} = 0.37 \times B_o^* - 0.05$  based on the 190 atmospheric boundary layer model. Given their favorable spatial applicability and representativeness, this 191 study opted to utilize these four  $B_{oa} \sim B_o^*$  formulas to refine the MEP model and assess their suitability. The 192 revised reciprocal actual Bowen ratio is represented as,

193  

$$\begin{cases}
B(\sigma)_{a1} = \frac{1}{B_{oa}} = \frac{B(\sigma)}{0.79 - 0.21 \times B(\sigma)} \\
B(\sigma)_{a2} = \frac{1}{B_{oa}} = \frac{B(\sigma)}{0.63 - 0.15 \times B(\sigma)} \\
B(\sigma)_{a3} = \frac{1}{B_{oa}} = \frac{B(\sigma)}{0.24} \\
B(\sigma)_{a4} = \frac{1}{B_{oa}} = \frac{B(\sigma)}{0.37 - 0.05 \times B(\sigma)}
\end{cases}$$
(14)

where  $B(\sigma)_{a1} \sim B(\sigma)_{a4}$  represent the four empirical Bowen ratio formulas for comparisons in this 194 study. Thus, the improved MEP model is complemented as: replacing the original  $B(\sigma)$  with the 195 corrected  $B(\sigma)_a$ , then combining Eq. (5), (7)-(9), and (14) into the MEP energy balance equation 196 197 considering heat storage (Eq. (10)), ultimately leading to the determination of latent and sensible heat flux.

#### 198 2.3 Input data for MEP model

199 The performance of both the original and improved Maximum Entropy Production (MEP) models is 200 evaluated using observed data from in-situ buoy stations, as discussed in Section 3.1. Subsequently, the 201 optimal empirical Bowen ratio formula for the MEP model is determined through multi-site assessments. 202 The refined MEP model is then applied to estimate global heat fluxes based on long-term remote-sensing 203 observations, detailed in Sections 3.2 and 3.3, following a comprehensive evaluation of input parameters. 204 Specifically, the input variables of net radiation, heat storage, and sea surface temperature driving the 205 improved MEP model are derived from the J-OFURO3 dataset, covering the period from 1988 to 2017 at a 206 spatial resolution of  $0.25^{\circ}$  (detailed in Section 4.3).





#### 207 2.4 Sensitivity analysis

208 To quantify the influence of input variables in the MEP model on evaporation estimate at the ocean surface,

209 sensitivity coefficients (S) are computed as (Beven, 1979; Isabelle et al., 2021),

210 
$$S_i = \frac{\partial LE}{\partial x_i} \frac{x_i}{LE}$$
(15)

211 where  $S_i$  represents the sensitivity coefficient of LE to each variable  $x_i$ . The magnitude of  $S_i$  reflects the 212 degree of impact of the variable's changes on LE; a larger absolute value indicates a greater influence of the 213 variable on LE. A positive value signifies a positive correlation between evaporation and the variable's 214 changes, while a negative value indicates a negative correlation. For example, a sensitivity coefficient of 0.5 215 represents that a 10% increase in the variable would result in a 5% increase in LE. The sensitivity levels can 216 be categorized based on the absolute value |Si| (Lenhart et al., 2002; Yin et al., 2010): |Si| > 1 indicates very 217 high sensitivity, 1 > |Si| > 0.2 denotes high sensitivity, 0.2 > |Si| > 0.05 reflects moderate sensitivity, and |Si|218 < 0.05 suggests negligible sensitivity.

#### 219 2.5 Data fusion methods

220 To identify the globally optimal heat storage input data (refer to Section 4.3), this study attempts to determine 221 whether data fusion methods could vield results superior to individual datasets. This includes the Bayesian 222 Three-Cornered Hat (BTCH) Method (He et al., 2020) and the Simple Arithmetic Average (AA) method. 223 The Three-Cornered Hat (TCH) method has been widely applied to improve accuracy by integrating multi-224 source products, and it has been proven to outperform individual parent products (Long et al., 2017; Liu et 225 al., 2021; Duan et al., 2024). Recent evaluations of three distinct data fusion methods (TCH, BTCH, and AA) 226 in consolidating evapotranspiration estimates have affirmed their efficacy in filtering poor ET products, but 227 their ability to reliably identify superior ET products remains uncertain (Shao et al., 2022). For instance, the 228 AA method may yield better results than the BTCH method in some instances. Consequently, following a 229 comparative analysis of the accuracy of individual, BTCH, and AA fusion products, this study selects the 230 optimal heat storage dataset to drive the MEP model. Since BTCH is not the primary focus of this study, 231 detailed method descriptions are referred to He et al. (2020).



**3. Data materials** 

### 233 3.1 In situ buoy observations

234 A total of 129 in situ buoy sites were employed for ocean heat fluxes calculation and validation with MEP 235 model and its modified version, as listed in Table 1. About 96% of selected sites (124 of 129 all sites) are 236 collected from the Global Tropical Moored Buoy Array (available at https://www.pmel.noaa.gov/), which 237 consists of the TAO/TRION Pacific Ocean (69 buoys), PIRATA Atlantic Ocean (23 buoys), and RAMA 238 Indian ocean (32 buoys), and the remaining sites including Upper Ocean Processes Group (3 buoys) consists 239 of Project WHOTS WHOI Hawaii Ocean Time-series Station (available at 240 https://uop.whoi.edu/ReferenceDataSets/whotsreference.html), Project NTAS - Northwest Tropical Atlantic Station and Project STRATUS (https://uop.whoi.edu/ReferenceDataSets/ntasreference.html), and the Pacific 241 242 ocean climate stations (2 buoys) consists of KEO and PAPA moorings 243 (https://www.pmel.noaa.gov/ocs/data/fluxdisdel/). The availability of all buoy stations refers to the "Data 244 availability" section. The observational sites cover the spatial range of 25°S~ 50.1°N latitude, temporal range 245 span from 1989/12 to 2023/12. Observational meteorological variables and heat fluxes includes the net 246 longwave radiation, net shortwave radiation, sea surface skin temperature, specific humidity at 2m height (if 247 available, or computed as the function of SST according to the Clausius-Clapeyron equation), latent heat 248 flux and sensible heat flux. Limited by the availability of longwave radiation observations, the net radiation 249 has a relatively shorter time series length compared to latent and sensible heat fluxes. The surface air-sea 250 fluxes of buoy observations are computed using the COARE 3.0b algorithm, which have been widely applied 251 for fluxes estimations and validations (Tang et al., 2023; Bentamy et al., 2017; Fairall et al., 2003). All the 252 selected original buoy observation (except for KEO and Papa sites) records are in monthly temporal resolution, and the original daily observations of KEO and Papa has been aggregated to monthly by simple 253 254 average method. The spatially distributed map of all selected sites is illustrated in Fig.S1.

255

#### 256 Table 1. Information about observational ocean surface heat fluxes of 129 buoy sites

Buoy array	Buoy amount	Spatial coverage	Temporal coverage	Number of LE (H) records	Number of $R_n$ records
TAO/TRION	69	165°E-95°W	1989/12/16-	12377	522
pacific		10°S-10°N	2023/12/16		





PIRATA Atlantic	23	40°W-10°E, 20°S-20°N	1997/9/16- 2023/12/16	2644	631
RAMA Indian	32	55°E-100°E, 25°S-15°N	2001/11/16- 2023/12/16	1862	286
WHOTS	1	158°W, 22.7°N	2004/08/15- 2021/08/15	205	205
NTAS	1	51°W, 15°N	2001-04/15- 2020/03/15	219	219
STRATUS	1	85.4°W, 19.6°S	2000/10/15- 2021/01/15	235	235
KEO	1	144.6°E, 32.3°N	2004/06/17- 2023/08/12	177	177
РАРА	1	144.9°W, 50.1°N	2007/06/08- 2023/11/14	181	181

Note: The number of records represents the effective count (excluding NA values) of latent and sensible heat
 flux observations.

259 3.2 Global turbulent heat flux datasets for evaluations

This study evaluates and compares 7 global turbulent heat flux products with observations, categorizing them into three types: Remote sensing-based, atmosphere reanalysis-based, and hybrid-based (Table 2). These seven products encompass monthly data spanning from 1988 to 2017, with spatial resolutions ranging from 0.25° to 1°. The criterion for dataset filtering prioritizes products that feature relatively longer time series, typically exceeding 15 years.

265 The Clouds and Earth's Radiant Energy Systems Synoptic Edition 4A (CERES SYN1deg Ed4A, 266 hereafter referred to as CERES4, available at https://ceres.larc.nasa.gov/data/) offers net radiation data, derived from clear-sky upward shortwave, downward shortwave flux, upward longwave, and downward 267 268 longwave flux measurements (Wielicki et al., 1996; Rutan et al., 2015). Another remote sensing-based 269 radiation product, the Global Energy and Water Cycle Experiment - Surface Radiation Budget (GEWEX-270 SRB, available at https://asdc.larc.nasa.gov/project/SRB) (Pinker et al., 1992), in conjunction with CERES4, 271 demonstrates good accuracy in retrieving  $R_n$ , as validated by six global observing networks (Liang et al., 272 2022). 273 The J-OFURO3 is the third-generation dataset developed by the Japanese Ocean Flux Data Sets with

- 274 use of the Remote-Sensing Observations (J-OFURO) research project (available at https://j-
- 275 ofuro.isee.nagoya-u.ac.jp/en/) (Tomita et al., 2019). It calculates turbulent heat flux with the latest version of





- 276 COARE3.0 algorithm, and provides datasets for  $R_n$ , LE, H and SST in this study. Validation with in situ 277 observations showed that J-OFURO3 offered a superior performance of latent heat compared to other 5 satellite products from 2002-2013 (Tomita et al., 2019). 278 279 Two Atmosphere reanalysis products including the fifth generation European Centre for Medium-Range 280 Weather Forecasts (ECMWF) atmospheric Re-Analysis52 (ERA5, available at 281 https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels-monthly-282 means?tab=overview) (Hersbach et al., 2020), and the Modern-Era Retrospective analysis for Research and 283 Applications Version2 (MERRA2, available at 284 https://disc.gsfc.nasa.gov/datasets/M2TMNXOCN 5.12.4/summary) (Gelaro et al., 2017). Both ERA5 and 285 MERRA2 products employ the bulk formula based on the MOST to calculate heat fluxes. Validation results from previous studies have demonstrated good consistency with buoy estimates regarding heat fluxes 286 287 (Pokhrel et al., 2020; Chen et al., 2020). The OAFlux (available at https://oaflux.whoi.edu/), a hybrid-based product developed under the 288 Objectively Analyzed Air-Sea Fluxes (OAFlux) project at the Woods Hole Oceanographic Institution (WHOI) 289 290 (Yu et al., 2008), was utilized for comparisons with ocean heat fluxes derived from distinct methods. This
- 291 product calculates fluxes based on the COARE3.0 bulk algorithm and employs a variational objective 292 analysis to determine the optimal fitting of independent variables. Detailed descriptions on all utilized global 293 turbulent heat fluxes products, and their validation performances against buoy observations with reported 294 studies are available in Tang et al (2023).
- 295

### 296 **Table 2.** The information of the 7 used global radiation and heat fluxes products

Product	Variables	Spatial resolution	Time span	Туре	Reference
CERES4	$R_n$	1°	2000-2017	Remote sensing	Rutan et al. (2015)
GEWEX-SRB	$R_n$	1°	1988-2017	Remote sensing	Pinker et al. (1992)
J-OFURO3	$R_n$ , SST, LE, H	0.25°	1988-2017	Remote sensing	Tomita et al. (2019)
ERA5	$R_n, LE, H, P$	0.25°	1988-2017	Atmosphere reanalysis	Hersbach. et al. (2020)





MERRA2	$R_n, LE, H$	$1/2^{\circ} \times 2/3^{\circ}$	1988-2017	Atmosphere reanalysis	Gelaro et al. (2017)
OAFlux	LE, H	1°	1988-2017	Hybrid-based	Yu et al. (2008)
IAPv4-OHC	ОНС	1°	1988-2017	Hybrid-based	Cheng et al. (2017)

297

298



#### 300 3.3 Ocean heat content data

301 Remote sensing data for heat storage (G) primarily derive from two categories: one is obtained from the 302 residual of the energy balance equation ( $R_n$ -LE-H), including J-OFURO3, ERA5, and MERRA2; the other 303 is calculated as changes in Ocean Heat Content (OHC). The ocean heat content data is obtained from IAP 304 OHC gridded analysis (IAPv4, available at http://www.ocean.iap.ac.cn/) dataset, covering ocean depth of 0-305 6000m (Cheng et al., 2017), and has been extensively utilized in global ocean heat analysis, ocean warming, and climate change studies (Li et al., 2023; Cheng et al., 2022; Cheng et al., 2024). The delta OHC is 306 307 calculated numerical 2019) as using the differentiation method (Xu et al.,  $\Delta OHC(i) = \frac{OHC(i+1) - OHC(i-1)}{2\Delta i}, i \text{ denotes the OHC of } i\text{-th month. At the WHOTS site, this study}$ 308 309 compared the OHC changes at different depths with the observed G (derived as Rn-LE-H) (Fig.S1). Since 310 the OHC variation from 0~100m depth exhibits the smallest error with the observations, the data from

312  $\triangle OHC$  for global evaporation estimations, with the aim of minimizing the errors introduced by input 313 variable data in the MEP model.

0~100m depth range were chosen as the heat storage. This study assesses the suitability of G flux and

This study evaluates the accuracy of all the variables  $R_n$ ,  $T_s$ , and G using the aforementioned datasets on a global scale by comparing them against buoy observations (in Section 4.3), to optimize input accuracy for driving the MEP model. To maintain consistency in the analysis, this study resamples all products to a 1° spatial resolution when comparing the Bowen ratio across multiple products. Nevertheless, when conducting site validations with buoy observations, the original resolution of the data is preserved to minimize uncertainty attributable to scale effects.

#### 320 **4. Results**

311

#### 321 4.1 The new MEP model with heat storage and the revised Bowen ratio formulas

To demonstrate how the MEP model has been developed and improved, we show the comparisons of different MEP models in simulating heat fluxes across 129 global buoy stations (Fig.1). Limited by the availability of  $R_{nL}$  data, we used LE + H instead of the available energy  $(R_n - G)$ , enabling the utilization of more observational records to verify the MEP model. The original MEP model (without considering heat



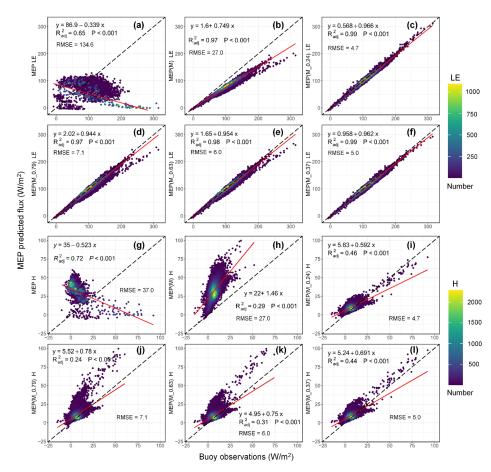


326	storage) shows a significant negative correlation between $LE$ and $H$ (with $R^2$ exceeds 0.65 as in Fig.1a &
327	Fig.1c), with considerable errors, where the RMSE of <i>LE</i> is 134.6 W·m <sup>-2</sup> and that of <i>H</i> is 37 W·m <sup>-2</sup> . Upon
328	modification by considering the influence of heat storage effects (Represented as MEP_M, as depicted in
329	Fig.1b & Fig.1h), the MEP-simulated <i>LE</i> shows a good consistency ( $R^2 = 0.97$ ) with the buoy observations,
330	but an approximate 25% underestimation (slope = 0.75) was observed, with RMSE reduced to 27 $W \cdot m^{-2}$ .
331	However, it reveals an overall underestimation (approximate 25%) of $LE$ and a large overestimation of $H$ .
332	This finding agrees with previous research findings that equilibrium evaporation tends to underestimate
333	actual evaporation from saturated surfaces by 20%~30% (Yang & Roderick, 2019; Philip, 1987). The
334	physical significance of this phenomenon can be explained as the equilibrium evaporation being considered
335	the lower limit of actual evaporation from saturated surfaces, causing typically falls below the actual
336	evaporation (Priestley and Taylor, 1972). To address the deviation between $B_{oa}$ and $B_{o}^{*}$ , it is necessary to
337	convert the equilibrium Bowen ratio into the actual Bowen ratio, allowing for a more reasonable and accurate
338	allocation of surface energy budget.

After modifying MEP's energy allocation using four empirical Bowen ratio formulas (denoted as 339 M 0.24, M 0.79, M 0.63, M 0.37), the accuracy of MEP predated latent and sensible heat have been 340 significantly improved. The MEP simulated LE exhibited strong agreement with observations, with all R<sup>2</sup> 341 342 exceeding 0.97 and RMSE ranging from 4.7 W·m<sup>-2</sup> (for M 0.24) to 7.1 W·m<sup>-2</sup> (for M 0.79), which is lower than that derived from equilibrium Bowen ratios (RMSE = 27 W  $\cdot$  m<sup>-2</sup>). Both *M* 0.79 and *M* 0.63 tended to 343 underestimate LE, especially when LE exceeded 200 W·m<sup>-2</sup> (Fig. 1d and Fig.1e). The results for sensible heat 344 345 flux simulated by MEP were similar to those for LE, the  $M_0.24$  outperformed the other three, showing the smallest errors and highest R<sup>2</sup>. 346







348

Figure 1. Scatter density plots of monthly latent heat flux (a~f) and sensible heat flux (g~l) derived by the original and modified MEP methods versus observations from 129 buoy stations (as in Table 1). (a) The original MEP method, (b) The modified MEP method considering the heat storage effect, (c) The modified MEP method considering both the heat storage and empirical Bowen ratio formula  $B_{oa}=0.24B_o^*$ , (d)~(f) for the modified MEP method considering both the heat storage and empirical Bowen ratio formulas  $B_{oa}=0.79B_o^*-0.21$ ,  $B_{oa}=0.63B_o^*-0.15$ , and  $B_{oa}=0.37B_o^*-0.05$ . (g)~(l) are the same with (a)~(f) but for sensible heat flux.

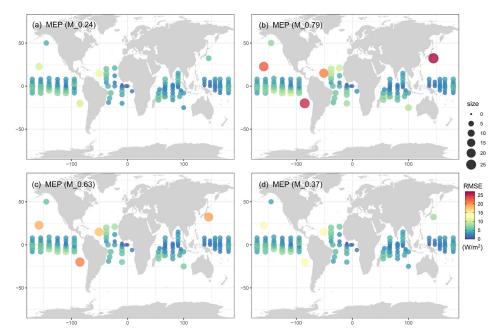
Specifically, the spatial errors for the four modified MEP formulas were obtained (Fig. 2), as well as the prediction errors across various observational buoy arrays (Fig.3). Overall, the four modified MEP formulas exhibit lower errors at low latitudes ( $10^{\circ}S\sim10^{\circ}N$ ), but they demonstrate larger discrepancies at higher latitudes, especially for the KEO, WHOTS, and STRATUS buoy sites. Comparing the four formulas across varying latitudes, the  $M_{-}0.24$  formula exhibits the smallest RMSE (ranging from 3.6 to 12 W·m<sup>-2</sup>) (Fig. 3c), while the  $M_{-}0.79$  formula shows the largest errors (RMSE ranging from 3.9 to 26.6 W·m<sup>-2</sup>). This consistency





- is also evident in the Kling-Gupta Efficiency (KGE) coefficient, with  $M_0.24$  demonstrating superior performance in terms of accuracy, robustness, and adaptability. In term of  $M_0.24$  formula, the prediction errors across observational arrays ranked as: RAMA < PIRATA < TAO/TRION < PaPa < KEO < STRATUS < WHOTS < NTAS. The arrays with relatively larger RMSE (NTAS in the Atlantic Ocean, WHOTS, and
- 367 STRATUS in the Pacific Ocean) may originate from the larger observed values of LE (Fig. S2).



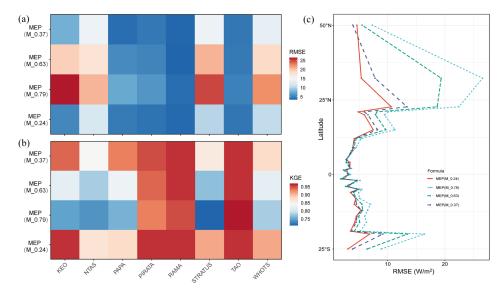


369

Figure 2. Spatial distribution of RMSE values in the comparison of latent heat flux estimated by the
 improved MEP method (modified by four different Bowen ratio formulas) with buoy observations from
 129 stations.







<sup>374</sup> 

Figure 3. Comparisons of latent heat flux estimated by the improved MEP method with buoy observations
from each buoy array in term of RMSE (a) KGE value (b), and latitudinal means of RMSE of four empirical
Bowen ratio formulas (c). Latitudinal means are based on data from 129 available buoy sites.

## 379 4.2 Dynamics of heat fluxes and Bowen ratio between original and improved MEP model

To thoroughly investigate the role of heat storage in the partitioning of surface energy and its implications for the temporal dynamics of heat fluxes, we selected the KEO site for detailed analysis. This decision was based on the site's extensive long-term observational records and notable variability in flux patterns, which offer an ideal context for a rigorous comparison of model-simulated error margins. The improved MEP methods demonstrated comparable performance in estimating heat fluxes at the KEO site when compared with 128 other sites (Fig. S3, Fig. 1), with the MEP (M\_0.24) model exhibited the

386 most effective performance. Analysis of the time series data revealed significant variations in latent heat,

387 sensible heat, and Bowen ratio (Fig. 4). In the original MEP theory, the estimated *LE* exhibits an opposite

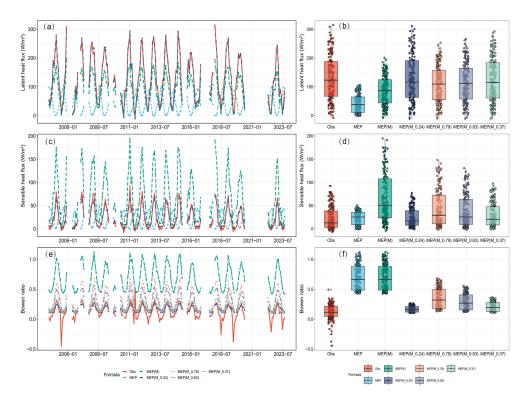
- 388 variation cycle (peak versus trough) compared to the observations. For instance, over a yearly period, the
- observed peak in LE occurred in January 2005 (269 W·m<sup>-2</sup>) and the trough in June 2005 (6.9 W·m<sup>-2</sup>). In
- 390 contrast, the MEP simulated the peak in LE to occur in August 2005 ( $105 \text{ W}\cdot\text{m}^{-2}$ ) and the trough in December
- $391 = 2004 (0.7 \text{ W} \cdot \text{m}^{-2})$ , resulting in a phase difference of 7 months for the peak and 6 months for the trough values.
- 392 Sensible heat flux (Fig. 4b) showed similar phase differences: observed H peaked in January 2005 (79 W m





393 <sup>2</sup>) and reached its minimum in June 2005 (-3 W·m<sup>-2</sup>), whereas MEP simulated H to peak in August 2005 (46 394 W·m<sup>-2</sup>) and reach its minimum in December 2004 (0.6 W·m<sup>-2</sup>), consistent with the pattern observed for LE. It is noteworthy that the original MEP model simulated variations in LE and H align with  $R_n$  (Fig. S4), which 395 is reasonable over land where the small G value can often be disregarded. However, over the ocean, the 396 397 observed variations in  $R_n$  and LE do not align in terms of their cycles. The maximum  $R_n$  occurred in June 2004 (329 W·m<sup>-2</sup>) and the minimum occurred in December 2004 (142 W·m<sup>-2</sup>), with a 6-month delay in 398 relation to the variations in LE. Specifically, the peak  $R_n$  corresponded to the trough of LE, and the trough 399 400  $R_n$  corresponded to the peak of *LE*. This delay indicates that the heat storage effect delays the peak of *LE* and 401 alters the seasonal variations of LE and H.

402



403

404Figure 4. MEP model predicted latent heat flux (a), sensible heat flux (c), Bowen ratio (e) versus observations,405and corresponding boxplots (b, d, f) of these variables at KEO site from June 17, 2004, to August 12, 2023.406Note that the (a) and (c) only display results using MEP  $(M_0.24)$  among all four empirical Bowen ratio407formulas for clearer comparison.





409 For the variation pattern of the Bowen ratio, both the original MEP formula and the modified formulas 410 exhibit consistent patterns with the observed values. The observed maximum Bowen ratio occurred in January 2005 (0.29), and the minimum in June 2005 (-0.4). However, the original MEP formula simulated a 411 412 maximum of 1.01 and a minimum of 0.44, indicating a significant overestimation compared to the observed 413 Bowen ratio. This discrepancy suggests that on the ocean surface, the available energy  $(R_n-G)$  is 414 predominantly allocated to LE (Fig.S4). Among four empirical formulas, M 0.24 simulated LE, H, and 415 Bowen ratio values closest to the observed values. The median of the observed Bowen ratio was 0.11, while 416 the original MEP Bowen ratio was 0.66. Among the four modified Bowen ratio formulas (M 0.24, M 0.79, 417 M 0.63, M 0.37), their median Bowen ratios were 0.15, 0.32, 0.27, and 0.19 respectively, with M 0.24 being 418 the closest to the observed Bowen ratio.

419 Heat storage is crucial for the energy distribution process over the ocean surface. While the original 420 MEP formulas have been effectively validated when applied to surfaces with shallow depths such as water 421 and snow (Wang et al., 2014), they exhibit significant uncertainty when applied to the ocean surface. This 422 discrepancy primarily arises from the fact that land is a non-transparent medium with relatively small heat 423 storage values at monthly scales. Similarly, shallow water bodies also exhibit small heat storage values that 424 can often be ignored. In the study by Wang et al. (2014), for example, two lakes with depths of 2m (Lake 425 Tämnaren) and 4m (Lake Råksjö) still resulted in underestimated LE. However, for deeper lakes (generally > 426 3m depth), heat storage becomes significant and cannot be neglected (Zhao et al., 2016; Zhao & Gao, 2019). 427 On deep ocean surfaces, with the most recent average depth estimate of 3,682 meters from NOAA satellite measurements, heat storage variations can influence depths up to 6,000 meters (Cheng et al., 2017). Therefore, 428 429 the impact of heat storage is substantial and cannot be disregarded. In the original MEP theory, heat storage 430 was not considered in the energy balance equation, where it was assumed that the net solar radiation  $(R_{ns})$  is 431 absorbed by the ocean and  $R_{nL} = LE + H + Q$ . Then, the heat storage was obtained as  $G = R_{ns} + Q$ . In this 432 study, we compared the characteristics of MEP-derived G ( $R_{ns} + Q$ ) with the observed G flux ( $G = R_n - LE$ 433 -H (Fig. S5). MEP-derived G shows a good correlation (R = 0.96) and consistent trends with the observed 434 values (Fig. S5a & b), ranging from -4 to 81 W  $\cdot$  m<sup>-2</sup>. However, MEP-calculated Q (ranged from -210 to -65 435  $W \cdot m^{-2}$ ) exhibits a negative correlation with the observed G (which ranged from -386 to 200  $W \cdot m^{-2}$ ). Both MEP-derived G and Q fluxes are significantly underestimated. Therefore, the prediction errors in LE and H 436





- 437 originates from the inability to accurately quantify heat storage. Hence, considering the influence of heat
- 438 storage is crucial for accurately predicting *LE* and *H* over the ocean surface.
- 439 4.3 Evaluation of global radiation and heat storage flux
- 440 4.3.1 Evaluation of net radiation

After considering the effect of heat storage and the Bowen ratio, the improved MEP method demonstrated its high performance at the site scale. The results suggest that improved MEP method holds substantial promise for further application at a global scale. To facilitate this, we assessed the primary input variables of the improved MEP method (including  $R_n$ , G, and  $T_s$ ) to identify datasets with the best accuracy.

445 Net radiation, as the primary variable in the energy balance equation, significantly influences the 446 uncertainty of the MEP model (Huang et al., 2017). Selecting a reliable  $R_n$  product is essential for accurately 447 estimating global latent and sensible heat fluxes. Previous studies have evaluated  $R_n$  at daily scales (Liang et 448 al., 2022). In this study, we conducted a comprehensive evaluation of current mainstream monthly  $R_n$ 449 products, including three remote sensing-based products (CERES, GEWEX-SRB, and JOFURO3) and two 450 atmosphere reanalysis-based products (ERA5 and MERRA2). All products exhibited good consistency with 451 buoy observations (Table 3 and Fig. S6), with  $R^2$  values greater than 0.78. In terms of RMSE, the error 452 rankings for all products were as: J-OFURO3 (10 W·m<sup>-2</sup>) < ERA5 (39.03 W·m<sup>-2</sup>) < CERES (40.67 W·m<sup>-2</sup>) 453 < GEWEX-SRB (41.83 W·m<sup>-2</sup>) < MERRA2 (49.23 W·m<sup>-2</sup>). It is evident that J-OFURO3 demonstrated the highest accuracy, as indicated by RMSE, NSE, and KGE statistics. This study is also consistent with previous 454 455 assessments of global radiation (Liang et al., 2022), emphasizing J-OFURO3 as the least erroneous among 456 all individual products and superior to existing alternatives including CERES4, ERA5, MERRA2, GEWEX-457 SRB, JRA55, OAFlux, and TropFlux.

458 **Table 3.** Evaluation of global monthly net radiation products against buoy observations

	-	-	-	-	-		
Products	R <sup>2</sup>	ME	MAE	RMSE	PBIAS	NSE	KGE
		(W·m <sup>-2</sup> )	(W·m <sup>-2</sup> )	$(W \cdot m^{-2})$	(%)		
J-OFURO3	0.96	1.6	7.3	10.0	1.0	0.96	0.97
ERA5	0.79	28.8	30.3	39.0	17.8	0.45	0.77
MERRA2	0.78	39.7	41.2	49.2	24.8	0.15	0.68
CERES	0.81	31.4	32.6	40.6	19.6	0.42	0.76
GEWEX-SRB	0.78	32.6	33.8	41.8	20.2	0.37	0.76

459 Note: The evaluation period for all datasets is 1988-2017, except for CERES, which spans from March 2000

to December 2017. The best-performed statistics are indicated in bold type.





#### 461 4.3.2 Evaluation of heat storage

462	The study underscores the importance of considering heat storage in simulating heat fluxes using the
463	improved MEP model. For the first time, we assessed global heat storage using the J-OFURO3, ERA5,
464	MERRA2, and $\Delta OHC$ datasets. In addition to assessing these individual datasets, we investigated the
465	potential for enhancing accuracy through data fusion methods. We employed the BTCH and AA method to
466	fuse heat storage data and compared the accuracy between individual datasets and fused datasets (Table 4).
467	The results reveal that while using the AA method (e.g., AA4) to fuse yields smaller errors compared to
468	ERA5, MERRA2, and $\Delta$ OHC, it still failed to achieve the accuracy of the J-OFURO3 product. Similarly, the
469	BTCH method, despite fusing data from three or four sources, also does not match the accuracy of the J-
470	OFURO3 method, as indicated by metrics of R <sup>2</sup> , RMSE, and KGE. The heat storage derived from J-OFURO3
471	data shows high consistency with observations ( $R^2=0.95$ ), as illustrated in Fig. 5 (spatial distribution of errors
472	depicted in Fig.S7). Therefore, this study adopts the heat storage data derived from the J-OFURO3 dataset
473	as the input for the MEP model.

474 To ensure consistency with radiation data source, the Sea surface temperature (SST) data from J-475 OFURO3 is utilized for  $T_s$  inputs, which is derived as the ensemble median from 12 global SST products 476 (Tomita et al., 2019). Ultimately, the input variables including net radiation, heat storage, and sea surface 477 temperature for driving MEP model are all determined from the J-OFURO3 dataset spanning from 1988 to 478 2017. Saturated specific humidity is computed as a function of SST and surface air pressure (from ERA5) 479 using the Clausius-Clapeyron equation. The reliability of gridded data for the variables  $R_n$ , G, and  $T_s$  are 480 simultaneously examined at an observational site (Fig.S8), where all three variables demonstrated high 481 consistency with observed data from August 2004 to December 2017 (with  $R^2 > 0.96$ ), effectively capturing 482 the monthly dynamics of  $R_n$ , G, and  $T_s$ .

484 **Table 4.** Assessment of monthly heat storage between global remote sensing datasets and buoy observations

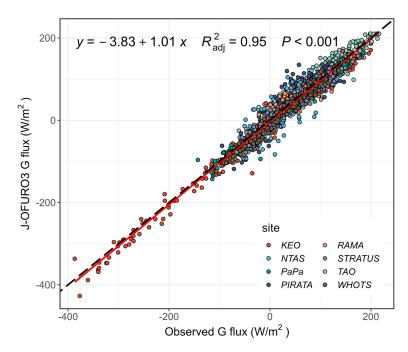
Products	R <sup>2</sup>	ME (W⋅m <sup>-2</sup> )	MAE (W·m <sup>-2</sup> )	RMSE (W·m <sup>-2</sup> )	PBIAS (%)	NSE	KGE	-
J-OFURO3	0.95	-3.5	15.3	19.7	-7.4	0.94	0.91	
ERA5	0.88	7.0	25.1	33.2	14.8	0.84	0.80	
MERRA2	0.86	11.6	27.1	36.1	24.5	0.81	0.72	
OHC	0.35	-48.2	64.4	86.9	-101.9	-0.11	-0.10	



BTCH3-1 (E M J)	0.89	7.1	22.8	30.5	15.1	0.86	0.81
(E M J) BTCH3-2 (E M O)	0.88	4.6	24.0	31.4	9.9	0.85	0.86
BTCH4	0.91	5.9	19.7	26.2	12.5	0.90	0.86
AA2(EM)	0.87	9.3	25.4	34.1	19.7	0.83	0.76
AA3 (EMJ)	0.91	4.7	20.2	26.7	10.1	0.90	0.87
AA4 (E M J O)	0.91	11.5	21.4	28.6	24.4	0.88	0.74

Note: BTCH3-1 represents the fusion of three products (ERA5, MERRA2, and J-OFURO3) using the BTCH
method; TCH3-2 represents the fusion of ERA5, MERRA2, and OHC; BTCH4 represents the fusion of ERA5,
J-OFURO3, MERRA, and OHC. AA denotes the Simple Arithmetic Average (AA) method. The evaluation
period spans from 1988 to 2017, and the best-performed statistics are indicated in bold type.

- 489
- 490



491

Figure 5. Assessment of heat storage (G) flux derived from remote sensed J-OFURO3 dataset against buoy
 observations. Distinct colors represent data from different buoy arrays.

## 494

## 495 4.4 Estimating long-term global ocean surface heat fluxes by improved MEP model

### 496 4.4.1 New estimate of global latent and sensible heat fluxes

- 498 (i, e., M 0.24, hereinafter referred to as MEP for simplicity, while the original MEP formula is denoted as
- 499 MEP (ori)) for global scale estimation, producing new estimations of latent and sensible heat fluxes for the
- period 1988-2017 (Table 5). The MEP model calculated the multi-year average LE as 92.87 W m<sup>-2</sup> and the

<sup>497</sup> After identifying the optimal driving dataset, this study employs the best-performed improved MEP method





501	sensible heat flux as 12.27 W·m <sup>-2</sup> from 1988 to 2017. In comparison, LE ranges from 88.95 (OAFlux) to
502	100.54 W·m <sup>-2</sup> (MERRA2), and H ranges from 10.17 (J-OFURO3) to 13.16 W·m <sup>-2</sup> (MERRA2) for the other
503	four products. The original MEP method yielded estimates of LE as 52.70 W·m <sup>-2</sup> and H as 25.07 W·m <sup>-2</sup> ,
504	significantly underestimating $LE$ and overestimating $H$ compared to estimates from other products. As
505	previously demonstrated (Sections 4.1 & 4.2), the original MEP method overestimated G (42.20 $\text{W}\cdot\text{m}^{-2}$ ) and
506	exhibited notable deviations in the Bowen ratio. Therefore, the improved MEP method provides a more
507	reasonable global estimation of LE and H.

508 Regarding the global spatial pattern (Fig.6), the MEP-derived latent heat shows higher values in low-509 latitude regions but notably decreases beyond 45° latitude. The highest LE values are observed in the southern 510 Indian Ocean near Australia, the Pacific and Atlantic regions near South America, and the Indian Ocean near 511 southern Africa. The peak values are observed within western boundary current systems (ranging from 200 512 to 260 W·m<sup>-2</sup>), including the Gulf Stream in the North Atlantic and the Kuroshio in the western North Pacific. Impacted by the variations in oceanic currents near the equator, two general areas of higher LE have emerged 513 (Yu et al., 2011), leading to notably low LE at the equator (88 W·m<sup>-2</sup>), peaking at ~18°S at 132 W·m<sup>-2</sup> (Fig. 514 515 6 & Fig.7). The MEP estimated LE exhibits a similar spatial pattern with other four products globally (Fig.6), 516 particularly resembling OAFlux between 15°S and 15°N (Fig. 7). Overall, for the region between 30°S and 30°N, the ranking of LE values is as follows: OAFlux < MEP < J-OFURO3 < ERA5 < MERRA2, which is 517 518 consistent with the magnitude of available energy. For sensible heat, MEP-derived H closely resembles that 519 of ERA5 and MERRA2, with higher values predominantly occurred in two western boundary current systems, 520 the South Indian Ocean near Australia area, and the Arctic Ocean. The improved MEP method mitigates the 521 issue of overestimating H in mid-to-high latitudes compared to its original form (Fig.61), resulting in more 522 realistic spatial patterns. In high latitudes, J-OFURO3 exhibits higher H values than MEP and other 523 comparable products in the Northern Hemisphere, with negative values observed between 45°S and 55°S. 524 MEP generally estimates H within an intermediate range compared to other products, displaying a 525 distribution that is more reasonable than that of J-OFURO3 product.

- 526
- 527
- 528
- 529





LE products	LE (W·m <sup>-2</sup> )	Evaporation (mm/yr)	$H (W \cdot m^{-2})$	G (W·m⁻²)	
MEP (0.24)	92.8	1195.5	12.2	19.7	
ERA5	99.2	1277.8	12.0	34.2	
MERRA2	100.5	1294.3	13.2	35.5	
J-OFURO3	94.9	1222.2	10.1	19.7	
OAflux	88.9	1145.1	10.4	/	
MEP (ori)	52.7	678.5	25.1	42.2	

530 Table 5. Global area-averaged multi-annual mean estimates of latent heat flux

Note: The period spans from 1988 to 2017. The MEP (0.24) denotes the improved MEP model, while MEP 531 532

(ori) represents the original MEP model.

533

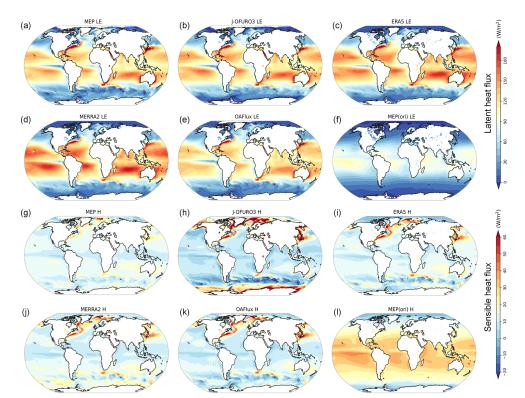


Figure 6. Global spatial maps of annual mean latent heat flux (LE) and sensible heat flux (H) during 1988-535 536 2017. Panels (a)-(f) depict latent heat flux derived from the improved MEP method, J-OFURO3, ERA5,

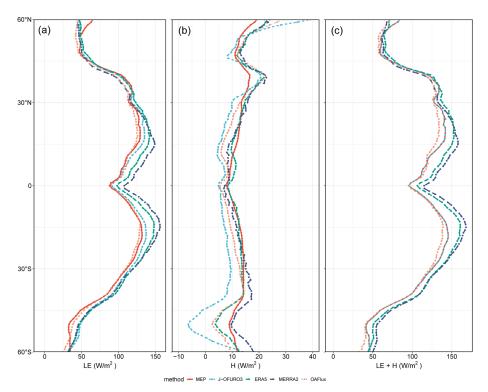




537 MERRA2, OAFlux, and the original MEP method. Panels (g)-(l) show sensible heat flux from the same

- 538 datasets.
- 539

540



541

542 **Figure 7.** Meridional profiles of latent heat (left panel), sensible heat (middle panel) and their sum 543 representing available energy (right panel) for the period 1988-2017.

544

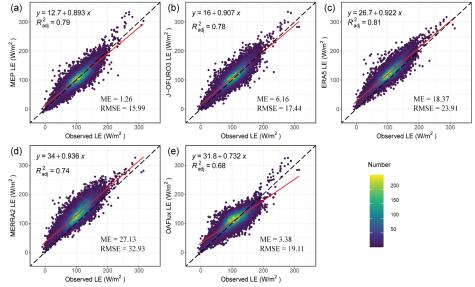
## 545 4.4.2 Validation of global latent heat

To evaluate the disparity between MEP estimates of LE and those of other existing products, this study 546 547 validated global-scale LE using 129 observational sites (as depicted in Fig.8 & Table 6). MEP-estimated LE showed strong consistency with buoy observations, achieving an R<sup>2</sup> of 0.79, a ME of 1.26 W·m<sup>-2</sup>, and RMSE 548 549 of 16 W·m<sup>-2</sup>, all surpassing those of alternative products, underscoring its superior performance. Moreover, 550 the MEP method exhibited superior performance with a higher NSE value of 0.77 and KGE of 0.89, 551 demonstrating enhanced accuracy, reliability, and robustness. According to the RMSE evaluation criterion, 552 the ranking of best-performed LE products is as: MEP, J-OFURO3, OAFlux, ERA5, MERRA2. In a recent 553 comprehensive assessment of 15 global LE products (Tang et al., 2023), RMSE values ranged from 17.2 to





- 45.3 W·m<sup>-2</sup>, in which J-OFURO3 emerged as the best-performing product with the lowest RMSE of 17.2 554 W·m<sup>-2</sup>, highest correlation coefficient (R) of 0.89, and ME of 6.5 W·m<sup>-2</sup>. Studies have also shown minimal 555 bias are given by J-OFURO3 on daily scale (Bentamy et al., 2017). This superior performance can be 556 557 attributed to the use of continuously updated bulk algorithms (COARE 3.0 version) by J-OFURO3, the 558 ongoing optimization of near-surface parameters (Tomita & Kubota, 2018), as well as the improved spatial 559 resolution (0.25°). In this study, the improved MEP estimates of LE outperformed that of J-OFURO3, demonstrating higher accuracy and lower error (ME=1.26 W·m<sup>-2</sup>), thereby establishing it as the most accurate 560 561 global LE product currently available.



562

Figure 8. Scatter density plots of latent heat flux derived from distinct methods versus observations from
 129 buoy stations during the period 1988-2017: (a) Improved MEP method, (b) J-OFURO3, (c) ERA5, (d)
 MERRA2, and (e) OAFlux. A total of 15444 records of latent heat observations are included.

566

5(7	<b>T-11</b> . C E-1, $f_{1}$ , $f_{1}$ , $f_{1}$ , $f_{1}$ , $f_{2}$ , $f_{3}$ , $f$
567	<b>I anie 6</b> Evaluation of latent near tilly from different methods against bliov observations
507	<b>Table 6.</b> Evaluation of latent heat flux from different methods against buoy observations

Products	R <sup>2</sup>	ME	MAE	RMSE	PBIAS (%)	NSE	KGE
		(W·m <sup>-2</sup> )	$(W \cdot m^{-2})$	$(W \cdot m^{-2})$			
MEP	0.79	1.3	12.2	15.9	1.2	0.77	0.89
J-OFURO3	0.78	6.3	13.4	17.4	5.8	0.73	0.87
ERA5	0.81	18.4	19.9	23.9	17.3	0.48	0.80
MERRA2	0.74	27.1	28.1	32.9	25.5	0.02	0.70
OAFlux	0.68	3.4	14.9	19.1	3.2	0.67	0.79

568 Note: The evaluation period spans from 1988 to 2017, and the best-performed statistics are indicated in bold

569 type.

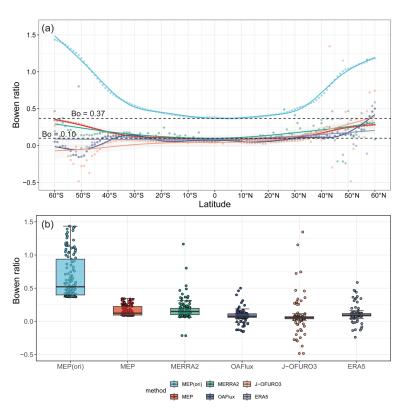


#### 570 4.4.3 Comparisons of Bowen ratios

571 The improved MEP model achieves accurate LE estimates after refining the process of partitioning the 572 surface energy budget, specifically through revisions to the Bowen ratio. The improved MEP method notably decreased the global-scale Bowen ratio, as illustrated in Fig. 9 and 10. Regarding latitude averages, the 573 574 Bowen ratio of the original MEP formula ranged from 0.37 to 1.48 (with a median of 0.80), whereas the 575 modified MEP Bowen ratio ranged from 0.09 to 0.35 (median of 0.18). Specifically, in the low-latitude region (10°S-10°N), the Bowen ratio of the modified MEP formula decreased from 0.37 to approximately 0.1, 576 577 aligning closely with the Bowen ratios obtained from other reanalysis products (MERRA2, ERA5, OAFlux, 578 and J-OFURO3). Globally, the median Bowen ratios of the products are as follows: MERRA2 (0.15), MEP 579 (0.12), ERA5 (0.09), OAFlux (0.08), and J-OFURO3 (0.06). Spatially, the MEP Bowen ratio resembles 580 ERA5 in mid to low latitudes but exhibits deviations from other products at high latitudes, where those 581 products show fluctuating changes in the Bowen ratio (Fig.10). For instance, other products display abrupt 582 transitions from negative to positive Bowen ratios in the Arctic and Antarctic regions, whereas MEP-derived 583 values demonstrate greater stability in variations at higher latitudes. This discrepancy is likely due to the 584 reanalysis products relying on the bulk method, which is sensitive to variations in wind speed and temperature 585 gradients, leading to errors in simulating high wind speeds at the poles and causing fluctuations in latent and 586 sensible heat. In contrast, the MEP model strictly adheres to energy conservation principles and operates 587 independently of wind speed and temperature gradients, resulting in a more accurate estimate of the Bowen 588 ratio. For example (Fig.S9), at the high-latitude PAPA buoy site (144.9°W, 50.1°N), the Bowen ratio 589 estimated by MEP (median 0.24) closely matches the observed Bowen ratio (median 0.23). In contrast, all the other products underestimated the Bowen ratio, with J-OFURO3 (median -0.09) and OAFlux frequently 590 591 exhibiting negative values. The Bowen ratio derived from MEP fits well with a Generalized Additive Model 592 (GAM) (Fig.9). The implicit functional relationship between Bowen ratio and latitude is expressed as  $(R^2 =$ 593 0.996, p < 0.001):  $B_{oa}$  (*lat*) =  $0.207218 + f(lat) + \varepsilon$ , where f(lat) represents a smoothing function derived from 594 a smooth curve, and  $\varepsilon$  denotes the error term. However, the specific functional form of f(lat) cannot be 595 explicitly determined. Therefore, a polynomial regression method is employed to explicitly fit B<sub>oa</sub> and lat, resulting in  $(R^2 = 0.91, p < 0.001)$ :  $B_{oa} = 9.97 \times 10^{-2} - 3.45 \times 10^{-4} \times lat + 4.71 \times 10^{-5} \times lat^2 + \varepsilon$  (as in Fig.S10). 596 597 This equation serves as a reference for partitioning surface energy over data-sparse oceanic regions.

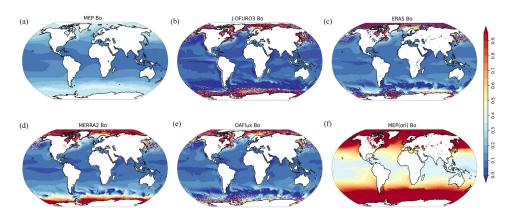






598

Figure 9. Global ocean latitudinal averaged Bowen ratio derived by the MEP method and four other products from 1988 to 2017. (a) Latitudinal averaged Bowen ratio derived from the MEP model using original and modified Bowen ratio formulas, with points fitted by a generalized additive model (GAM). (b) Statistical distribution of the latitudinal annual mean Bowen ratio.



604

Figure 10. Global distribution of ocean annual mean Bowen ratio during 1988-2017: (a) Improved MEP
 method, (b) J-OFURO3, (c) ERA5, (d) MERRA2, (e) OAFlux, and (f) MEP original method.





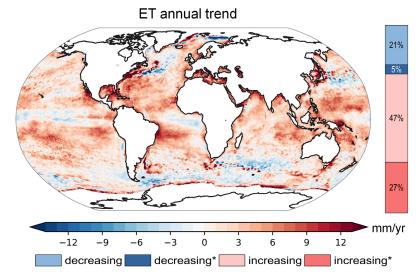
#### 608 4.5 Spatial-temporal variability of ocean evaporation

609	Heat flux reflects the energy exchange between the ocean and the atmosphere, while evaporation (ET) reflects
610	moisture exchange within the water cycle. The spatiotemporal patterns of evaporation were analyzed using
611	Sen's slope and the Mann-Kendall test methods (Fig.11). Globally, approximately 74% (with 27%
612	statistically significant) showed an increasing trend, while 26% (with 21% statistically significant) exhibited
613	a decreasing trend. The regions with the highest increasing trends were predominantly observed near western
614	boundary current systems, the convergence zones of the East Australian Current and the South Equatorial
615	Current, and the convergence zones of the Eastern South Equatorial Current and the Brazil Current along
616	South America. Decreasing trends were primarily observed in equatorial regions of the Pacific and Atlantic
617	Oceans, as well as near the Labrador and Kuroshio currents and north of the Antarctic Circle. It is indicated
618	that regions with significant increases (decreases) in evaporation generally correspond closely to the
619	distribution of major warm currents (cold currents) spatially.

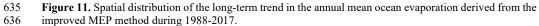
Over the multi-year changes from 1988 and 2017, MEP, J-OFURO3, ERA5, and MERRA2 all exhibited 620 621 significant increasing trends in ET. MEP estimated an evaporation increased rate of 2.31 mm/year, whereas OAFlux showed a non-significant trend (Fig.12). This upward trend in ET can largely be attributed to changes 622 623 in available energy, which increased at a rate of 0.274 W/( $m^2$ ·year). For instance, during peak ET years such 624 as 1989, 1992, 2003, and 2008,  $R_n$  was also at its highest; conversely, during years of minimum ET like 1991 625 and 1997,  $R_n$  was minimal. This consistency is in line with previous findings (Huang et al., 2017), where 626 more than 50% of the uncertainty in MEP-modeled fluxes was attributed to the radiation term. While different 627 methods yield varying magnitudes of ET changes, they generally exhibit a transition around 2010: an increasing trend from 1988 to around 2010 followed by a decreasing trend thereafter (Fig. 12a). For instance, 628 629 MEP indicated an ET increase of 3.58 mm/year from 1988 to 2010, followed by a decrease at a rate of 2.18 630 mm/year after 2010. This shift primarily results from a decline in both available energy and surface 631 temperature starting around 2010. Although  $T_s$  increased after 2012, the significant decrease in available 632 energy was the main driver behind the decline in ET.







634



637

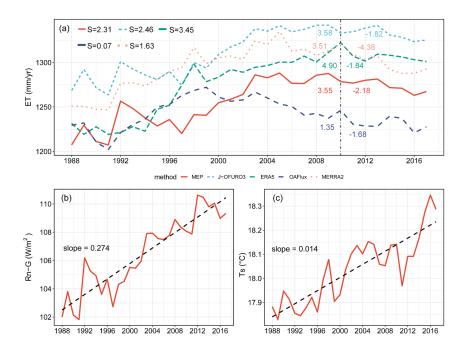


Figure 12. Time series of area-averaged multi-annual mean evaporation from the improved MEP method (a), available energy (b), and sea surface temperature (c) over the global oceans during 1988-2017. The black dotted line in panel (a) represents year 2010, and the black dashed lines in panels (b) and (c) represent the linear regression lines.





#### 643 **5. Discussion**

## 644 5.1 Quantifying impact of heat storage and radiation with sensitivity analysis

645 The sensitivity analysis reveals the significant influence of input variables on latent heat flux derived from 646 the MEP model. Notably, the heat storage (G) exhibits seasonal variations with both positive and negative values (Fig. 13). Positive G values coincide predominantly with summer in the Northern Hemisphere (winter 647 in the Southern Hemisphere), specifically from June to August (Fig. 4 and Fig. S5). During this season, 648 649 intensified solar radiation enhances the net energy input  $(R_n)$  at the ocean surface, leading to heat absorption and retention. Consequently, the energy available  $(R_n - G)$  for evaporation diminishes. The analysis indicates 650 651 that  $R_n$  significantly influences the energy-driven evaporation process, with a sensitivity coefficient 652 exceeding 1 (median 1.74), highlighting its pivotal role. In contrast, G negatively impacts evaporation, as 653 indicated by a sensitivity coefficient of -0.74. Specific humidity (median 0.08) and sea surface temperature 654 have relatively minor effects, consistent with previous MEP model findings focused on terrestrial surfaces 655 (Isabelle et al., 2021).

Conversely, negative values of heat storage predominate during winter, particularly from December to 656 657 February in the Northern Hemisphere (June to August in the Southern Hemisphere). Despite reduced solar 658 radiation during this period, residual heat stored from summer gradually releases into the atmosphere, 659 resulting in greater energy output than input. This surplus energy augments the available energy for 660 evaporation, leading to a positive sensitivity coefficient for G (median 0.29), second only to  $R_n$  (median 0.71). 661 Consequently, this process generally reduces sea surface temperature, resulting in a negative sensitivity 662 coefficient for surface temperature. Overall, these findings underscore the significant influence of  $R_n$  on 663 latent heat flux, with G ranking as the second most influential variable in MEP estimates over ocean surfaces. 664 For instance, a 10% decrease in positive G yields a 7.4% increase in evaporation, while a 10% increase in negative G results in a 2.9% increase in evaporation, assuming other variables remain constant. Thus,  $R_n$  and 665 666 G emerge as primary drivers of oceanic evaporation, with humidity and temperature exerting minimal 667 influence.

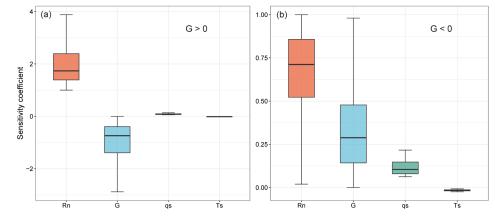
Furthermore, the pivotal role of available energy in determining *LE* is underscored by its direct relationship with energy allocation. Thus, the accuracy of available energy estimates directly influences *LE* simulations. Despite using bulk methods (COARE 3.0 algorithms) independent of radiation partitioning,





671 discrepancies in LE simulations correlate with errors in available energy estimates (Tables 3 and 4). Notably, 672 the MERRA2 product exhibited higher errors in simulating  $R_n$  and G compared to observations, leading to 673 significant biases in LE estimation. In contrast, ERA5 product demonstrated superior performance in 674 simulating  $R_n$  and G, thereby achieving higher accuracy in LE estimation. Consequently, the energy-balance-675 based MEP model excels in accurately computing surface heat fluxes by directly reflecting energy allocation. 676 Unlike bulk methods, the MEP approach reduces sensitivity to temperature and humidity gradients, thereby 677 minimizing uncertainties in LE simulations (Pelletier et al., 2018). This advancement enhances the MEP 678 model's utility in global energy and water cycle research, particularly pertinent for future climate change 679 studies.

680



681

Figure 13. Sensitivity coefficient associated with inputs variables for the improved MEP method at all 129
buoy stations: (a) for positive *G* values, and (b) for negative *G* values.

## 685 5.2 Discrepancy of empirical Bowen ratio formulas

Bowen ratio plays a crucial role in understanding the surface energy partitioning process. In this study, four empirical formulas were utilized to modify the MEP model and were evaluated against observations of latent heat flux, each with distinct conditions of applicability and suitability for integration with the MEP model:  $(1) B_{oa}=0.63B_o^*-0.15$  is derived from direct observational data fitting (Hicks and Hess, 1977). This formula is applicable for surface temperatures above 16°C, particularly within latitudes between 40°N and 40°S, making it more suitable for lower latitude regions. Therefore, it is more suitable for lower latitude regions;  $(2) B_{oa}=0.79B_o^*-0.21$  is derived using the Priestley–Taylor model under advection-free conditions (Priestley





693 and Taylor, 1972). The coefficients are based on a mean  $\alpha$  value of 1.26 (although this varies in practice). 694 However, recent studies have shown significant discrepancies due to the neglect of the interaction between 695  $R_n$  and  $T_s$  variations (Yang & Roderick, 2019); (3)  $B_{oa}=0.24B_o^*$  was developed to address this limitation 696 based on a maximum evaporation theory by considering the feedback mechanism between  $R_n$  and  $T_s$  (under 697 the circumstances of G to be small to negligible). The empirical coefficient (0.24) was determined by fitting 698 Bowen ratio and surface temperature data across the global ocean surface (Yang & Roderick, 2019); and (4) 699  $B_{oq} = 0.37B_o^* - 0.05$  was subsequently formulated based on principles derived from atmospheric boundary 700 layer (ABL) theory (Liu & Yang, 2021), with coefficients also fitted from relationships between  $B_{oa}$  and  $T_s$ . 701 It should be noted that the derivations of  $B_{oa}=0.24B_o^*$  and  $B_{oa}=0.37B_o^*-0.05$  were based on fitting using 702 latent heat data from the OAFlux dataset rather than direct buoy observations. Building upon the four empirical relationships between  $B_{oa}$  and  $B_{o}^{*}$  from previous studies, this study assessed the applicability of 703 704 these four empirical Bowen ratio formulas in estimating latent heat flux. The findings indicate that the MEP 705 model refined with  $B_{aa}=0.24B_{a}^{*}$ , exhibits superior accuracy at both localized and global scales, effectively mitigating the underestimation of LE in its original formulation. Moreover, the results show that the improved 706 707 MEP model closely aligns with buoy observations and achieves higher accuracy globally compared to 708 OAFlux products (as depicted in Fig. 8), surpassing other bulk method-based products as well.

#### 709 5.3 Contributions and implications of this study

710 The main contributions of this study include: (1) The MEP model's energy balance equation over water 711 surfaces was revised to explicitly consider heat storage effect. This correction highlights the importance of 712 heat storage in estimating latent heat flux. (2) The energy partitioning of the MEP model was revised to 713 incorporate empirical Bowen ratio formulas, significantly improving the heat flux estimations. (3) This study 714 conducted the first thorough global assessment of heat storage using extensive buoy observations and remote 715 sensed data, enabling the MEP model to produce the most accurate global latent heat flux estimates. This 716 study addresses the issue of underestimating latent heat flux by the MEP model, increasing the global average LE from 53 W·m<sup>-2</sup> to 93 W·m<sup>-2</sup>, while reducing sensible heat flux from 25 W·m<sup>-2</sup> to 12 W·m<sup>-2</sup>, improving 717 718 the partitioning of energy budget. The improved MEP model provides precise LE estimates compared to 719 existing datasets like J-OFURO3, ERA5, MERRA2, and OAFlux, enabling it to become a valuable 720 benchmark dataset for global evaporation studies.





721	From a methodological perspective, the improved MEP method presents a new approach for estimating
722	heat flux that diverges from existing bulk methods. The bulk method traditionally requires input parameters
723	including air temperature, specific humidity, wind speed, sea surface temperature, and atmospheric pressure,
724	as well as the observational height of all parameters (Fairal et al., 2003; Tomita et al., 2021). In contrast to
725	the bulk method, which requires a high demand for driving variables and shows lower sensitivity to
726	temperature variations. It requires only net radiation, heat storage, and surface temperature to simultaneously
727	estimate latent heat and sensible heat fluxes. Furthermore, the improved MEP model is not constrained by
728	the magnitude of heat storage and theoretically can be applied across various temporal scales (including sub-
729	daily and daily), beyond the monthly scale used in this study. This underscores the applicability of the MEP
730	method in addressing the constraints of traditional bulk methods, providing another independent approach to
731	estimating heat fluxes across diverse environmental conditions.

This study applies the improved MEP model to ocean surface, with potential for future extension to lake and reservoir surfaces. Compared to the Penman model for water body evaporation (Tian et al., 2022; Zhao et al., 2022; Bai et al., 2023), major advantage of MEP method lies in its independence from wind speed, as long as the heat storage can be determined using an equilibrium temperature-based approach (McMahon et al., 2013; Zhao & Gao, 2019). The global LE dataset generated in this study, given MEP's insensitivity to variations in air temperature and humidity, can be applied in studies related to ocean salinity (Liu et al., 2019), ocean warming (Cheng et al., 2022), global climate change and water cycle research (Konapala et al., 2020).

## 739 6. Data availability

The dataset produced using the MEP method, which includes global latent heat flux and sensible heat flux at a monthly scale from 1988 to 2017, can be freely downloaded from the Figshare platform (<u>https://doi.org/10.6084/m9.figshare.26861767.v2</u>, Yang et al., 2024). All the datasets used in this study are publicly available online and are described in the Data Materials section.

### 744 7. Conclusions

In this study, we developed a global monthly latent heat flux product for the ocean covering the period from
1988 to 2017. This product is based on a maximum entropy production theory framework, incorporating heat





747 storage and Bowen ratio optimizations. It represents the first energy-balance-based dataset that differs from 748 existing global ocean heat flux datasets derived from bulk methods. To assess the accuracy of the input 749 variables for the maximum entropy production framework, we utilized five global datasets, including two 750 remote sensing-based and three from reanalysis-based, alongside four global datasets of heat storage derived 751 from the energy balance equation and ocean heat content changes. We employed data fusion methods, 752 including arithmetic averaging and the Bayesian three-cornered hat method, to identify optimal input datasets 753 through validation against observations. The performance of the newly produced dataset was evaluated 754 against extensive observations from 129 globally distributed buoy stations using multiple statistical metrics, 755 and it was also compared with four auxiliary products: J-OFURO3, ERA5, MERRA2, and OAFlux. 756 Additionally, we analyzed the long-term spatial-temporal variability of ocean latent heat flux. Ultimately, we 757 investigated the impacts of ocean heat storage, net radiation, and Bowen ratio changes on heat flux 758 estimations and surface energy partitioning.

759 The MEP framework provides new estimates of global heat fluxes. The MEP-estimated long-term annual mean latent heat flux is 93 W·m<sup>-2</sup> (equivalent to 1196 mm/year of evaporation) during the period from 760 761 1988 to 2017. This estimate is at an intermediate level compared to other global flux products, which range 762 from 90 W·m<sup>-2</sup> (OAFlux) to 101 W·m<sup>-2</sup> (MERRA2). The MEP-estimated sensible heat flux is 12 W·m<sup>-2</sup>, falling within the range of 10.17 W·m<sup>2</sup> (J-OFURO3) to 13 W·m<sup>2</sup> (MERRA2) reported by other current 763 764 products. Compared with previous heat flux products, the MEP-estimated latent heat demonstrated higher accuracy when validated against observations, with a ME of 1.26  $W \cdot m^{-2}$ , a RMSE of 16  $W \cdot m^{-2}$ , and a KGE 765 value of 0.89, outperforming all other contemporary global products. Approximately 74% of oceanic regions 766 experienced an increasing trend in evaporation from 1988 to 2017. Regarding long-term temporal variability, 767 768 the global annual mean evaporation exhibited an increase rate of 3.58 mm/yr from 1988 to 2010 but 769 subsequently decreased at a rate of 2.18 mm/yr from 2010 to 2017, which was consistent with changes in 770 surface available energy.

This study demonstrates that the improved MEP framework has significantly improved the accuracy of the original MEP theory, addressing both the underestimation of latent heat and the overestimation of sensible heat flux. This improvement was achieved by incorporating the impact of heat storage and modifying the Bowen ratio formula within the MEP theory. The consideration of heat storage resolved the issue of seasonal





- 775 phase mismatches (approximately 6-month lags) between MEP estimates and buoy observations. Building 776 upon this improvement, this study further optimized the energy partitioning process by correcting the Bowen 777 ratio, linearly adjusting the equilibrium Bowen ratio to align with actual conditions. Four empirical Bowen ratio formulas for modifying the MEP method were assessed globally, identifying  $B_{oa}=0.24B_o^*$  as the most 778 779 accurate formula for estimating latent heat flux within MEP method. The impact of heat storage on estimating 780 heat fluxes was quantified through the sensitivity analysis. Net radiation and heat storage were identified as 781 the primary drivers of evaporation estimates. A 10% decrease in positive heat storage led to a 7.4% increase 782 in evaporation, whereas a 10% increase in negative heat storage resulted in a 2.9% increase. 783 Compared to existing bulk methods, the MEP model offers several advantages including the need for 784 fewer input variables, independence from wind speed, and insensitivity to variations in temperature and 785 humidity. The MEP derived ocean heat flux dataset has been validated and provides accurate estimates of 786 latent heat flux. Additionally, this MEP method can be applied to estimate evaporation from other deep-water 787 surfaces, such as lakes and reservoirs where heat storage is significant. Overall, the MEP-derived ocean heat
- flux dataset provides high global accuracy, fine spatial resolution  $(0.25^{\circ})$ , and extensive long-term temporal
- 789 records. This dataset is expected to be valuable for applications related to global ocean warming, hydrological
- 790 cycles, and their interactions with other Earth system components in the context of climate change.
- 791





792	Supplement. The Supplementary material related to this article is submitted during submission.
793	
794	Author contributions. YY and HS developed the methodology and designed the experiments, WZ
795	contributed the conceptual design, YY and WZ collected and processed the data, YY wrote the first draft of
796	the paper under the supervision of other authors. All authors participated in the revies and editing of the paper.
797	
798	Competing interests. The contact author has declared that none of the authors has any competing interests.
799	
800	Acknowledgments. We acknowledge the GTMBA Project Office of NOAA/PMEL for providing the Global
801	Tropical Moored Buoy Array observations. This study was primarily funded by the Third Xinjiang Scientific
802	Expedition Program (Grant No.2022xjkk0105) (H.S.). The authors acknowledge funding from the NSFC
803	project (52079055, 52011530128). H.S. and W.Z. acknowledges funding from the NSFC-STINT projects
804	(No. 202100-3211 and CH2019-8281). W. Z. was supported by the grants from Swedish Research Council

805 VR (2020-05338), and Swedish National space Agency (209/19).





## 806 **References**

807	Andreas, E. L., & Cash, B. A.: A new formulation for the Bowen ratio over saturated surfaces. Journal of
808	Applied Meteorology and Climatology, 35(8), 1279-1289, 1996.
809	Andreas, E. L., Jordan, R. E., Mahrt, L., & Vickers, D.: Estimating the Bowen ratio over the open and ice-
810	covered ocean. Journal of Geophysical Research: Oceans, 118(9), 4334-4345, 2013.
811	Andreas, E. L., Persson, P. O. G., & Hare, J. E.: A bulk turbulent air-sea flux algorithm for high-wind, spray
812	conditions. Journal of Physical Oceanography, 38(7), 1581-1596, 2008.
813	Bai, P., & Guo, X.: Development of a 60-year high-resolution water body evaporation dataset in China.
814	Agricultural and Forest Meteorology, 334, 109428, 2023.
815	Bentamy, A., Piolle, J. F., Grouazel, A., Danielson, R., Gulev, S., Paul, F., & Josey, S. A.: Review and
816	assessment of latent and sensible heat flux accuracy over the global oceans. Remote Sensing of
817	Environment, 201, 196-218, 2017.
818	Beven, K.: A sensitivity analysis of the Penman-Monteith actual evapotranspiration estimates. Journal of
819	Hydrology, 44(3-4), 169-190, 1979.
820	Bosilovich, M. G., Robertson, F. R., & Chen, J.: Global energy and water budgets in merra. Journal of
821	Climate, 24(22), 5721-5739, 2011.
822	Bourras, D.: Comparison of five satellite-derived latent heat flux products to moored buoy data. Journal of
823	Climate, 19(24), 6291-6313, 2006.
824	Chen, X., Yao, Y., Li, Y., Zhang, Y., Jia, K., Zhang, X., & Guo, X.: ANN-based estimation of low-latitude
825	monthly ocean latent heat flux by ensemble satellite and reanalysis products. Sensors, 20(17), 4773,
826	2020.
827	Cheng, L., Pan, Y., Tan, Z., Zheng, H., Zhu, Y., Wei, W., & Zhu, J.: IAPv4 ocean temperature and ocean
828	heat content gridded dataset. Earth System Science Data Discussions, 2024, 1-56, 2024.
829	Cheng, L., Trenberth, K. E., Fasullo, J., Boyer, T., Abraham, J., & Zhu, J.: Improved estimates of ocean heat
830	content from 1960 to 2015. Science Advances, 3(3), e1601545, 2017.
831	Cheng, L., von Schuckmann, K., Abraham, J. P., Trenberth, K. E., Mann, M. E., Zanna, L., & Lin, X.: Past
832	and future ocean warming. Nature Reviews Earth & Environment, 3(11), 776-794, 2022.
833	Duan, S. B., Zhou, S., Li, Z. L., Liu, X., Chang, S., Liu, M., & Shang, G.: Improving monthly mean land
834	surface temperature estimation by merging four products using the generalized three-cornered hat
835	method and maximum likelihood estimation. Remote Sensing of Environment, 302, 113989, 2024.
836	Fairall, C. W., Bradley, E. F., Hare, J. E., Grachev, A. A., & Edson, J. B.: Bulk parameterization of air-sea
837	fluxes: Updates and verification for the COARE algorithm. Journal of climate, 16(4), 571-591, 2003.
838	Fairall, C. W., Bradley, E. F., Rogers, D. P., Edson, J. B., & Young, G. S.: Bulk parameterization of air-sea
839	fluxes for tropical ocean-global atmosphere coupled-ocean atmosphere response experiment. Journal of
840	Geophysical Research: Oceans, 101(C2), 3747-3764, 1996.





841	Gelaro, R., McCarty, W., Suárez, M. J., Todling, R., Molod, A., Takacs, L., & Zhao, B.: The modern-era
842	retrospective analysis for research and applications, version 2 (MERRA-2). Journal of climate, 30(14),
843	5419-5454, 2017.
844	Guo, J., Li, W., Chang, X., Zhu, G., Liu, X., & Guo, B.: Terrestrial water storage changes over Xinjiang
845	extracted by combining Gaussian filter and multichannel singular spectrum analysis from GRACE.
846	Geophysical Journal International, 213(1), 397-407, 2018.
847	He, X., Xu, T., Xia, Y., Bateni, S. M., Guo, Z., Liu, S., & Zhao, J.: A Bayesian three-cornered hat (BTCH)
848	method: improving the terrestrial evapotranspiration estimation. Remote Sensing, 12(5), 878, 2020.
849	Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., & Thépaut, J. N.: The
850	ERA5 global reanalysis. Quarterly Journal of the Royal Meteorological Society, 146(730), 1999-2049,
851	2020.
852	Hicks, B. B., & Hess, G. D.: On the Bowen ratio and surface temperature at sea. Journal of physical
853	oceanography, 7(1), 141-145, 1977.
854	Huang, S. Y., Deng, Y., & Wang, J.: Revisiting the global surface energy budgets with maximum-entropy-
855	production model of surface heat fluxes. Climate Dynamics, 49, 1531-1545, 2017.
856	Isabelle, P. E., Viens, L., Nadeau, D. F., Anctil, F., Wang, J., & Maheu, A.: Sensitivity analysis of the
857	maximum entropy production method to model evaporation in boreal and temperate forests.
858	Geophysical Research Letters, 48(13), e2020GL091919, 2021.
859	Iwasaki, S., Kubota, M., & Watabe, T.: Assessment of various global freshwater flux products for the global
860	ice-free oceans. Remote sensing of environment, 140, 549-561, 2014.
861	Jo, Y. H., Yan, X. H., Pan, J., He, M. X., & Liu, W. T.: Calculation of the Bowen ratio in the tropical Pacific
862	using sea surface temperature data. Journal of Geophysical Research: Oceans, 107(C9), 17-1, 2002.
863	Johnson, G. C., & Lyman, J. M.: Warming trends increasingly dominate global ocean. Nature Climate
864	Change, 10(8), 757-761, 2020.
865	Konapala, G., Mishra, A. K., Wada, Y., & Mann, M. E.: Climate change will affect global water availability
866	through compounding changes in seasonal precipitation and evaporation. Nature communications, 11(1),
867	3044, 2020.
868	Lenhart, T., Eckhardt, K., Fohrer, N., & Frede, H. G.: Comparison of two different approaches of sensitivity
869	analysis. Physics and Chemistry of the Earth, Parts A/B/C, 27(9-10), 645-654, 2002.
870	Li, Z., England, M. H., & Groeskamp, S.: Recent acceleration in global ocean heat accumulation by mode
871	and intermediate waters. Nature Communications, 14(1), 6888, 2023.
872	Liang, H., Jiang, B., Liang, S., Peng, J., Li, S., Han, J., & Zhang, X.: a global long-term ocean surface
873	daily/0.05 net radiation product from 1983-2020. Scientific Data, 9(1), 337, 2022.
874	Liu, C., Liang, X., Ponte, R. M., Vinogradova, N., & Wang, O.: Vertical redistribution of salt and layered
875	changes in global ocean salinity. Nature communications, 10(1), 3445, 2019.





876	Liu, J., Chai, L., Dong, J., Zheng, D., Wigneron, J. P., Liu, S., & Lu, Z.: Uncertainty analysis of eleven
877	multisource soil moisture products in the third pole environment based on the three-corned hat method.
878	Remote sensing of environment, 255, 112225, 2021.
879	Liu, Z., & Yang, H.: Estimation of water surface energy partitioning with a conceptual atmospheric boundary
880	layer model. Geophysical Research Letters, 48(9), e2021GL092643, 2021.
881	Long, D., Pan, Y., Zhou, J., Chen, Y., Hou, X., Hong, Y., & Longuevergne, L.: Global analysis of
882	spatiotemporal variability in merged total water storage changes using multiple GRACE products and
883	global hydrological models. Remote sensing of environment, 192, 198-216, 2017.
884	Marti, F., Blazquez, A., Meyssignac, B., Ablain, M., Barnoud, A., Fraudeau, R., & Benveniste, J.:
885	Monitoring the ocean heat content change and the Earth energy imbalance from space altimetry and
886	space gravimetry. Earth System Science Data, 14(1), 229-249, 2022.
887	Masson-Delmotte V, Zhai P, Pirani S, Connors C, Péan S, Berger N, et al.: IPCC, 2021: Summary for
888	policymakers. in: Climate change 2021: The physical science basis. contribution of working group I to
889	the sixth assessment report of the intergovernmental panel on climate change, 2021.
890	McMahon, T. A., Peel, M. C., Lowe, L., Srikanthan, R., & McVicar, T. R.: Estimating actual, potential,
891	reference crop and pan evaporation using standard meteorological data: a pragmatic synthesis.
892	Hydrology and Earth System Sciences, 17(4), 1331-1363, 2013.
893	Meehl, G. A.: A calculation of ocean heat storage and effective ocean surface layer depths for the Northern
894	Hemisphere. Journal of physical oceanography, 14(11), 1747-1761, 1984.
895	Pelletier, C., Lemarié, F., & Blayo, E.: Sensitivity analysis and metamodels for the bulk parametrization of
896	turbulent air-sea fluxes. Quarterly Journal of the Royal Meteorological Society, 144(712), 658-669,
897	2018.
898	Philip, J.R.: A physical bound on the Bowen ratio. Journal of Climate and Applied Meteorology, 26, 1043-
899	1045, 1987.
900	Pinker, R. T., & Laszlo, I.: Modeling surface solar irradiance for satellite applications on a global scale.
901	Journal of Applied Meteorology and Climatology, 31(2), 194-211, 1992.
902	Pokhrel, S., Dutta, U., Rahaman, H., Chaudhari, H., Hazra, A., Saha, S. K., & Veeranjaneyulu, C.: Evaluation
903	of different heat flux products over the tropical Indian Ocean. Earth and Space Science, 7(6),
904	e2019EA000988, 2020.
905	Priestley, C. H. B., & Taylor, R. J.: On the assessment of surface heat flux and evaporation using large-scale
906	parameters. Monthly weather review, 100(2), 81-92, 1972.
907	Robertson, F. R., Roberts, J. B., Bosilovich, M. G., Bentamy, A., Clayson, C. A., Fennig, K., & Slivinski,
908	L. C.: Uncertainties in ocean latent heat flux variations over recent decades in satellite-based estimates
909	and reduced observation reanalyses. Journal of Climate, 33(19), 8415-8437, 2020.
910	Roderick, M. L., Sun, F., Lim, W. H., & Farquhar, G. D.: A general framework for understanding the response
911	of the water cycle to global warming over land and ocean. Hydrology and Earth System Sciences, 18(5),
912	1575-1589, 2014.





913 Rutan, D. A., Kato, S., Doelling, D. R., Rose, F. G., Nguyen, L. T., Caldwell, T. E., & Loeb, N. G.: CERES 914 synoptic product: Methodology and validation of surface radiant flux. Journal of Atmospheric and 915 Oceanic Technology, 32(6), 1121-1143, 2015. 916 Shaman, J., & Kohn, M.: Absolute humidity modulates influenza survival, transmission, and seasonality. 917 Proceedings of the National Academy of Sciences, 106(9), 3243-3248, 2009. 918 Shao, X., Zhang, Y., Liu, C., Chiew, F. H., Tian, J., Ma, N., & Zhang, X.: Can indirect evaluation methods 919 and their fusion products reduce uncertainty in actual evapotranspiration estimates?. Water Resources 920 Research, 58(6), e2021WR031069, 2022. 921 Smith, S. R., Hughes, P. J., & Bourassa, M. A.: A comparison of nine monthly air-sea flux products. 922 International Journal of Climatology, 31(7), 1002-1027, 2011. 923 Sun, H., Chen, J., Yang, Y., Yan, D., Xue, J., Wang, J., & Zhang, W.: Assessment of long-term water stress 924 for ecosystems across China using the maximum entropy production theory-based evapotranspiration 925 product. Journal of Cleaner Production, 349, 131414, 2022. 926 Sun, H., Sun, X., Chen, J., Deng, X., Yang, Y., Qin, H., ... & Zhang, W.: Different types of meteorological drought and their impact on agriculture in Central China. Journal of Hydrology, 627, 130423, 2023. 927 Tang, R., Wang, Y., Jiang, Y., Liu, M., Peng, Z., Hu, Y., ... & Li, Z. L.: A review of global products of air-928 929 sea turbulent heat flux: accuracy, mean, variability, and trend. Earth-Science Reviews, 104662, 2023. 930 Tian, W., Liu, X., Wang, K., Bai, P., Liu, C., & Liang, X.: Estimation of global reservoir evaporation losses. 931 Journal of Hydrology, 607, 127524, 2022. 932 Tomita, H., Hihara, T., & Kubota, M.: Improved satellite estimation of near-surface humidity using vertical 933 water vapor profile information. Geophysical Research Letters, 45(2), 899-906, 2018. 934 Tomita, H., Hihara, T., Kako, S. I., Kubota, M., & Kutsuwada, K.: An introduction to J-OFURO3, a third-935 generation Japanese ocean flux data set using remote-sensing observations. Journal of Oceanography, 936 75(2), 171-194, 2019. 937 Tomita, H., Kutsuwada, K., Kubota, M., & Hihara, T.: Advances in the estimation of global surface net heat 938 flux based on satellite observation: J-OFURO3 V1. 1. Frontiers in Marine Science, 8, 612361, 2021. 939 Von Schuckmann, K., Minière, A., Gues, F., Cuesta-Valero, F. J., Kirchengast, G., Adusumilli, S., ... & Zemp, 940 M.: Heat stored in the Earth system 1960–2020: where does the energy go?. Earth System Science Data, 941 15(4), 1675-1709, 2023. 942 Wang, F., Shen, Y., Chen, Q., & Wang, W.: Bridging the gap between GRACE and GRACE follow-on 943 monthly gravity field solutions using improved multichannel singular spectrum analysis. Journal of 944 Hydrology, 594, 125972, 2021. 945 Wang, J., & Bras, R. L .: A model of evapotranspiration based on the theory of maximum entropy production. 946 Water Resources Research, 47(3), 2011. 947 Wang, J., & Bras, R. L.: An extremum solution of the Monin-Obukhov similarity equations. Journal of the atmospheric sciences, 67(2), 485-499, 2010. 948





949	Wang, J., Bras, R. L., Nieves, V., & Deng, Y.: A model of energy budgets over water, snow, and ice surfaces.
950	Journal of Geophysical Research: Atmospheres, 119(10), 6034-6051, 2014.
951	Wang, K., & Dickinson, R. E.: A review of global terrestrial evapotranspiration: Observation, modeling,
952	climatology, and climatic variability. Reviews of Geophysics, 50(2), 2012.
953	Wang, W., Chakraborty, T. C., Xiao, W., & Lee, X.: Ocean surface energy balance allows a constraint on the
954	sensitivity of precipitation to global warming. Nature Communications, 12(1), 2115, 2021.
955	Wentz, F. J., Ricciardulli, L., Hilburn, K., & Mears, C.: How much more rain will global warming bring?.
956	Science, 317(5835), 233-235. 2007.
957	Wielicki, B. A., B. R. Barkstrom, E. F. Harrison, R. B. Lee III, G. L. Smith, and J. E. Cooper.: Clouds and
958	the Earth's Radiant Energy System (CERES): An Earth Observing System Experiment, Bull. Amer.
959	Meteor. Soc., 77, 853-868, 1996.
960	Wielicki, B. A., Barkstrom, B. R., Harrison, E. F., Lee III, R. B., Smith, G. L., & Cooper, J. E.: Clouds and
961	the Earth's Radiant Energy System (CERES): An earth observing system experiment. Bulletin of the
962	American Meteorological Society, 77(5), 853-868, 1996.
963	Xu, T., Guo, Z., Xia, Y., Ferreira, V. G., Liu, S., Wang, K., & Zhao, C.: Evaluation of twelve
964	evapotranspiration products from machine learning, remote sensing and land surface models over
965	conterminous United States. Journal of Hydrology, 578, 124105, 2019.
966	Yang, Y., & Roderick, M. L.: Radiation, surface temperature and evaporation over wet surfaces. Quarterly
967	Journal of the Royal Meteorological Society, 145(720), 1118-1129, 2019.
968	Yang, Y., Roderick, M. L., Guo, H., Miralles, D. G., Zhang, L., Fatichi, S., & Yang, D.: Evapotranspiration
969	on a greening Earth. Nature Reviews Earth & Environment, 4(9), 626-641, 2023.
970	Yang, Y., Sun, H., Zhu, M., Wang, J., & Zhang, W.: An R package of maximum entropy production model
971	to estimate 41 years of global evapotranspiration. Journal of Hydrology, 614, 128639, 2022.
972	Yin, Y., Wu, S., Chen, G., & Dai, E.: Attribution analyses of potential evapotranspiration changes in China
973	since the 1960s. Theoretical and applied climatology, 101, 19-28, 2010.
974	Yu, L., X. Jin, and R. A. Weller.: Multidecade Global Flux Datasets from the Objectively Analyzed Air-sea
975	Fluxes (OAFlux) Project: Latent and sensible heat fluxes, ocean evaporation, and related surface
976	meteorological variables. Woods Hole Oceanograp, 2008.
977	Yu, L.: A global relationship between the ocean water cycle and near-surface salinity. Journal of Geophysical
978	Research: Oceans, 116(C10), 2011.
979	Zeng, X., Zhao, M., & Dickinson, R. E.: Intercomparison of bulk aerodynamic algorithms for the
980	computation of sea surface fluxes using TOGA COARE and TAO data. Journal of Climate, 11(10),
981	2628-2644, 1998.
982	Zhao, G., & Gao, H.: Estimating reservoir evaporation losses for the United States: Fusing remote sensing
983	and modeling approaches. Remote Sensing of Environment, 226, 109-124, 2019.
984	Zhao, G., Gao, H., Naz, B. S., Kao, S. C., & Voisin, N.: Integrating a reservoir regulation scheme into a
985	spatially distributed hydrological model. Advances in Water Resources, 98, 16-31, 2016.





- 986 Zhao, G., Li, Y., Zhou, L., & Gao, H.: Evaporative water loss of 1.42 million global lakes. Nature
- 987 Communications, 13(1), 3686, 2022.