

- **Global ocean surface heat fluxes revisited: A new dataset**
- **from maximum entropy production framework with heat**

storage and Bowen ratio optimizations

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 Abstract. Ocean evaporation (latent heat flux, LE) plays a crucial role in global precipitation patterns, water cycle dynamics, and energy exchange processes. However, current bulk methods for quantifying ocean evaporation are subject to significant uncertainties. The Maximum Entropy Production (MEP) theory offers a novel approach for estimating surface heat fluxes, but its effectiveness over ocean surfaces has not been validated. This study integrates heat storage effects and four empirical Bowen ratio formulas into the MEP theory to improve ocean LE estimation. We employed multi-source data from 129 globally distributed buoy stations and seven auxiliary turbulent flux datasets for validation and comparison. We first evaluated the MEP method using observed data from buoy stations, identifying the optimal Bowen ratio formula to enhance the model. Results indicate that accounting for heat storage and adjusting the Bowen ratio significantly 30 improve heat flux accuracy, with $R^2 = 0.99$ and a root mean squared error (RMSE) of 4.7 W·m⁻² compared to observations. Subsequently, we conducted a thorough evaluation of seven global turbulent flux datasets to identify the most accurate input variables (e.g., heat storage, net radiation, surface temperature) for applying the MEP method on a global ocean scale. The enhanced MEP method provided new estimates of the annual

34 average LE at 93 W·m⁻² and sensible heat at 12 W·m⁻² for the period 1988 to 2017. Validation against observations from 129 buoy stations demonstrated that the MEP-derived latent heat dataset achieved the 36 highest accuracy, with a mean error (ME) of 1.3 W·m⁻², an RMSE of 15.9 W·m⁻², and a Kling-Gupta Efficiency (KGE) of 0.89, outperforming four major long-term global heat flux datasets, including J- OFURO3, ERA5, MERRA2, and OAFlux. Additionally, we examined the long-term spatiotemporal variability of global ocean evaporation, identifying a significant increasing trend from 1988 to 2010 at a rate of 3.58 mm/yr, followed by a decline at a rate of -2.18 mm/yr from 2010 to 2017. The current dataset provides a new benchmark for the ocean surface energy budget and is expected to be valuable for research on global ocean warming, sea surface-atmosphere energy exchange, the water cycle and climate change. The monthly MEP heat flux dataset for 1988–2017 is publicly available at https://doi.org/10.6084/m9.figshare.26861767.v2 (Yang et al., 2024, last access: 28 August 2024).

1. Introduction

 The ocean system plays a pivotal role in regulating the global climate by receiving and redistributing heat and freshwater, thereby influencing Earth's energy balance and the dynamics of the water cycle (Li et al., 2023; Von Schuckmann et al., 2023; Marti et al., 2022; Johnson et al., 2020). A key component of this regulation is ocean evaporation (latent heat), which accounts for approximately 86% of atmospheric water vapor and is the primary driver of the global hydrological cycle (Yu, 2011). As climate change warms the ocean, evaporation rates are anticipated to rise, potentially intensifying the global hydrological cycle (Masson-Delmotte et al., 2021). This intensification could alter precipitation patterns, affecting regional water availability and freshwater ecosystems (Konapala et al., 2020; Roderick et al., 2014). Therefore, precise estimation of ocean evaporation is critical to understand and quantify the global energy and water budget (Iwasaki et al., 2014).

 Current methods for calculating surface latent heat (*LE*) and sensible heat flux (*H*) employ bulk transfer formulations that necessitate extensive parameterization inputs, including temperature gradients, humidity gradients, wind speed, and transfer coefficients (Fairall et al., 1996; Andreas et al., 2008). Despite their widespread application, these bulk methods encounter significant limitations primarily due to challenges in accurately parameterizing and empirically deriving coefficients (Zeng et al., 1998; Robertson et al., 2020). These methods heavily depend on assumptions regarding atmospheric stability and boundary layer dynamics, which may not consistently apply across diverse and complex environmental conditions (Fairall et al., 2003; Andreas et al., 2013). Furthermore, uncertainties in estimating turbulent transfer coefficients can lead to

 substantial errors in the estimation of latent heat flux. The high demands for parameterization and challenges in data acquisition contribute to considerable uncertainties when implementing bulk methods for calculations. While numerous energy balance-based algorithms have been developed to estimate global terrestrial evapotranspiration (Wang et al., 2012; Yang et al., 2023), similar efforts to apply these algorithms for estimating ocean surface heat flux remain unexplored. Therefore, proposing an innovative method for estimating ocean surface heat flux based on rational surface energy allocation could yield significant theoretical and practical implications. This approach may serve as an additional reference source for existing bulk methods and their derived datasets, offering a new methodological perspective for quantifying the uncertainty of ocean heat flux estimation. Ultimately, this could facilitate more accurate ocean flux estimation and enhance research on ocean energy allocation patterns.

 The Maximum Entropy Production (MEP) model, an energy-balance-based approach, has recently emerged as a novel method for simulating surface heat fluxes. Developed from Bayesian probability theory and information theory, it prioritizes the most probable partitioning of radiation fluxes (Wang & Bras, 2011). The MEP model has been rigorously validated across diverse surface types and varying degrees of surface wetness (Wang et al., 2014; Huang et al., 2017; Yang et al., 2022; Sun et al., 2022; Sun et al., 2023). Notably, the MEP model requires fewer input variables—net radiation, surface temperature, and specific humidity— yet provides accurate estimates of latent heat, sensible heat, and ground heat fluxes simultaneously. Unlike bulk methods (Fairall et al., 2003), which rely on wind speed, temperature gradient, and humidity gradient, the MEP model satisfies the energy balance constraint without these dependencies. This characteristic enhances its applicability and robustness across diverse environmental conditions. However, the previous application of the MEP model over ocean surfaces has revealed significant limitations, including notable underestimations of latent heat and overestimations of sensible heat flux (Huang et al., 2017). The global 86 multi-year averaged *LE* estimated by the MEP model indicates a value around 58 W·m⁻², much lower than 87 the range of $92~109$ W·m⁻² reported by other remote sensing or reanalysis-based products. Conversely, MEP estimates an averaged *H* of approximately 28 W·m⁻², which is significantly higher compared to values 89 ranging from 6 to 18 W·m⁻² found in other products. These discrepancies highlight substantial uncertainties in applying the MEP model to oceanic energy partitioning, highlighting the urgent need for further refinement and rigorous validation efforts.

 The primary objectives of this study are as follows: (1) to develop and validate the MEP approach for estimating ocean heat fluxes using observations from 129 stations; (2) to investigate the impact of heat storage on ocean energy allocation and the influence of the Bowen ratio on energy partitioning for heat flux estimations; (3) to produce a MEP-derived ocean heat fluxes product (spatial resolution: 0.25°; temporal coverage: 1988-2017) and present its spatiotemporal patterns.

2. Methods

2.1 Components of ocean surface energy balance

The global ocean energy balance equation is as follows (Meehl, 1984; Wang et al., 2021):

$$
R_n = LE + H + G \tag{1}
$$

135 **2.2 The Maximum Entropy Production theory**

136 2.2.1 The original MEP model

137 The MEP model simulate ocean surface heat fluxes using inputs variables of net radiation (*Rn*), surface skin 138 temperature (*Ts*), and surface specific humidity (*qs*) under the constraint of the surface energy balance. The 139 latent heat, sensible heat, and surface thermal energy flux (*Q*) are calculated as,

140
$$
[1 + B(\sigma) + \frac{B(\sigma)}{\sigma} \frac{I_s}{I_0} |H|^{-\frac{1}{6}}]H = R_n
$$
 (4)

$$
E = B(\sigma)H\tag{5}
$$

$$
Q = Rnl - E - H
$$
\n⁽⁶⁾

143
$$
B(\sigma) = 6(\sqrt{1 + \frac{11}{36}\sigma} - 1), \quad \sigma = \frac{\lambda^2}{c_p R_v} \frac{q_s}{T_s^2}
$$
 (7)

144
$$
I_0 = \rho_a c_p \sqrt{C_1 k z} (C_2 \frac{k z g}{\rho_a c_p T_r})^{\frac{1}{6}}
$$
 (8)

145 where $B(\sigma)$ is the reciprocal Bowen ratio, σ is a dimensionless parameter that characterizes the phase change at the ocean surface, λ (J⋅kg⁻¹) is the latent heat of vaporization of liquid surface, c_p (10³ J⋅kg⁻¹⋅K⁻¹) is the specific heat of air under constant pressure, and *Rv* (461 J·kg−1·K−1 ¹⁴⁷) is the gas constant of water vapor. 148 *I*₀ is the "apparent thermal inertia" of air and describes the turbulent transport process of the boundary layer 149 based on the Monin-Obukhov similarity theory (MOST) (Wang and Bras, 2010). I_s is the thermal inertia of 150 the ocean surface (J·m⁻²·K⁻¹·s^{-1/2}), and can be parametrized as $I_s = \sqrt{\rho c \lambda}$ (with density ρ , the specific 151 heat *c*) represents the physical property of surface $(I_s = 1.56 \times 10^3 \text{ J} \cdot \text{m}^{-2} \cdot \text{K}^{-1} \cdot \text{s}^{-1/2}$ for water surface and 152 1.92 \times 10³ J·m⁻²·K⁻¹·s^{-1/2} for ice surface). 153 Over the sea ice surface, assumed to be saturated, the specific humidity q_s can be derived as a function 154 of surface temperature *Ts* using the Clausius‐Clapeyron equation. (El Sharif et al., 2019; Shaman & Kohn, 155 2009).

156
$$
q_s = \varepsilon \frac{e_s(T_s)}{P} = \varepsilon \frac{e_0}{P} \exp[\frac{\lambda_s}{R_v}(\frac{1}{T_0} - \frac{1}{T_s})]
$$
(9)

157 where ε (= 0.622) represents the ratio of the molecular weight of water vapor to that of dry air, $e_{\varepsilon}(T_{\varepsilon})$ 158 denotes the saturation vapor pressure at temperature Ts, e_0 is the saturation vapor pressure at the reference 159 temperature T_0 (273.15 K), and *P* is the atmospheric pressure (mb).

160 2.2.2 Specific improvements on the MEP model

161 Equations (4) \sim (9) presented above represent the original formulas of the MEP model. According to the

- 162 MEP theory, the net solar radiation (*Rns*) entering the water surface medium is absorbed by the water body,
- 163 with the allocable radiation flux denoted as $R_{nl} = E + H + Q$ (Eq.6). Consequently, the expression for

164 ocean heat uptake (heat storage) is derived as $G = R_n - E - H = R_n + Q$. While this theory has received preliminary validation in shallower water bodies, such as lake surfaces (Wang et al., 2014), its applicability on deeper water bodies with larger heat storage capacities in ocean surfaces requires further evaluation. This study introduces two key hypotheses: (1) The substantial heat storage capacity of the ocean can exert a significant influence on seasonal latent and sensible fluxes, potentially introducing bias to the MEP equations, (2) The notable underestimation of latent heat flux and overestimation of sensible heat flux by the MEP model point to a significant deviation from the Bowen's ratio formula, necessitating a reasonable correction. To address this, the study proposes two approaches for enhancing the MEP formulas: (1) Considering the impact of heat storage in the MEP's energy balance equation, and (2) Adjusting the theoretical equilibrium Bowen ratio within the MEP model. This can be specifically represented as follows:

174
$$
[1 + \frac{1}{B_o^*}]H = R_n - G
$$
 (10)

$$
B_o^* = \frac{1}{B(\sigma)}\tag{11}
$$

176
$$
B_{oa} = a \times B_o^* + b
$$
 (12)

177 where B_0^* is the equilibrium Bowen ratio, which denotes the theoretical ratio of sensible heat flux to 178 latent heat flux when the surface and the atmosphere are in equilibrium regarding water vapor. 179 Correspondingly, the corresponding evaporation at this condition is known as equilibrium evaporation 180 (defined as the water vapor evaporating from a saturated surface into a saturated atmosphere). To accurately 181 predict actual evaporation, a reliable functional relationship needs to be established to predict B_{oa} from B_o^* . 182 Empirical studies have introduced coefficients to correlate B_o^* to B_{oa} under diverse environmental 183 circumstances; for instance, the Priestley–Taylor coefficient is expressed as (Priestley & Taylor, 1972).

184
$$
B_{oa} = 0.79 \times B_o^* - 0.21 = \frac{0.79 - 0.21 \times B(\sigma)}{B(\sigma)}
$$
(13)

185 Further studies have led to the emergence of more updated empirical coefficients. Hicks and Hess (1977) 186 estimated the actual Bowen ratio as $B_{oa} = 0.63 \times B_a^* - 0.15$ by aligning it with direct observations of the 187 fluxes. Yang & Roderick (2019) deduced an empirical coefficient of 0.24 and formulated it as

- 188 $B_{oa} = 0.24 \times B_{o}^{*}$ through fitting Bowen ratio and surface temperature data across the global ocean surface.
- Furthermore, Liu & Yang (2021) derived a new equation as $B_{oa} = 0.37 \times B_o^* 0.05$ based on the 190 atmospheric boundary layer model. Given their favorable spatial applicability and representativeness, this 191 study opted to utilize these four $B_{oa} \sim B_o^*$ formulas to refine the MEP model and assess their suitability. The 192 revised reciprocal actual Bowen ratio is represented as,

193
\n
$$
\begin{bmatrix}\nB(\sigma)_{a1} = \frac{1}{B_{oa}} = \frac{B(\sigma)}{0.79 - 0.21 \times B(\sigma)} \\
B(\sigma)_{a2} = \frac{1}{B_{oa}} = \frac{B(\sigma)}{0.63 - 0.15 \times B(\sigma)} \\
B(\sigma)_{a3} = \frac{1}{B_{oa}} = \frac{B(\sigma)}{0.24} \\
B(\sigma)_{a4} = \frac{1}{B_{oa}} = \frac{B(\sigma)}{0.37 - 0.05 \times B(\sigma)}\n\end{bmatrix}
$$
\n(14)

194 where $B(\sigma)_{a} \sim B(\sigma)_{a}$ represent the four empirical Bowen ratio formulas for comparisons in this 195 study. Thus, the improved MEP model is complemented as: replacing the original $B(\sigma)$ with the 196 corrected $B(\sigma)_a$, then combining Eq. (5), (7)-(9), and (14) into the MEP energy balance equation 197 considering heat storage (Eq. (10)), ultimately leading to the determination of latent and sensible heat flux.

198 **2.3 Input data for MEP model**

 The performance of both the original and improved Maximum Entropy Production (MEP) models is evaluated using observed data from in-situ buoy stations, as discussed in Section 3.1. Subsequently, the optimal empirical Bowen ratio formula for the MEP model is determined through multi-site assessments. The refined MEP model is then applied to estimate global heat fluxes based on long-term remote-sensing observations, detailed in Sections 3.2 and 3.3, following a comprehensive evaluation of input parameters. Specifically, the input variables of net radiation, heat storage, and sea surface temperature driving the improved MEP model are derived from the J-OFURO3 dataset, covering the period from 1988 to 2017 at a spatial resolution of 0.25° (detailed in Section 4.3).

2.4 Sensitivity analysis

To quantify the influence of input variables in the MEP model on evaporation estimate at the ocean surface,

sensitivity coefficients (S) are computed as (Beven, 1979; Isabelle et al., 2021),

$$
S_i = \frac{\partial LE}{\partial x_i} \frac{x_i}{LE} \tag{15}
$$

211 where S_i represents the sensitivity coefficient of *LE* to each variable x_i . The magnitude of S_i reflects the degree of impact of the variable's changes on LE; a larger absolute value indicates a greater influence of the variable on *LE*. A positive value signifies a positive correlation between evaporation and the variable's changes, while a negative value indicates a negative correlation. For example, a sensitivity coefficient of 0.5 represents that a 10% increase in the variable would result in a 5% increase in *LE*. The sensitivity levels can 216 be categorized based on the absolute value $|Si|$ (Lenhart et al., 2002; Yin et al., 2010): $|Si| > 1$ indicates very 217 high sensitivity, $1 > |Si| > 0.2$ denotes high sensitivity, $0.2 > |Si| > 0.05$ reflects moderate sensitivity, and $|Si|$ < 0.05 suggests negligible sensitivity.

2.5 Data fusion methods

 To identify the globally optimal heat storage input data (refer to Section 4.3), this study attempts to determine whether data fusion methods could yield results superior to individual datasets. This includes the Bayesian Three-Cornered Hat (BTCH) Method (He et al., 2020) and the Simple Arithmetic Average (AA) method. The Three-Cornered Hat (TCH) method has been widely applied to improve accuracy by integrating multi- source products, and it has been proven to outperform individual parent products (Long et al., 2017; Liu et al., 2021; Duan et al., 2024). Recent evaluations of three distinct data fusion methods (TCH, BTCH, and AA) in consolidating evapotranspiration estimates have affirmed their efficacy in filtering poor ET products, but their ability to reliably identify superior ET products remains uncertain (Shao et al., 2022). For instance, the AA method may yield better results than the BTCH method in some instances. Consequently, following a comparative analysis of the accuracy of individual, BTCH, and AA fusion products, this study selects the optimal heat storage dataset to drive the MEP model. Since BTCH is not the primary focus of this study, detailed method descriptions are referred to He et al. (2020).

232 **3. Data materials**

233 **3.1 In situ buoy observations**

 A total of 129 in situ buoy sites were employed for ocean heat fluxes calculation and validation with MEP model and its modified version, as listed in Table 1. About 96% of selected sites (124 of 129 all sites) are 236 collected from the Global Tropical Moored Buoy Array (available at https://www.pmel.noaa.gov/), which consists of the TAO/TRION Pacific Ocean (69 buoys), PIRATA Atlantic Ocean (23 buoys), and RAMA Indian ocean (32 buoys), and the remaining sites including Upper Ocean Processes Group (3 buoys) consists of Project WHOTS - WHOI Hawaii Ocean Time-series Station (available at https://uop.whoi.edu/ReferenceDataSets/whotsreference.html), Project NTAS - Northwest Tropical Atlantic Station and Project STRATUS (https://uop.whoi.edu/ReferenceDataSets/ntasreference.html), and the Pacific ocean climate stations (2 buoys) consists of KEO and PAPA moorings (https://www.pmel.noaa.gov/ocs/data/fluxdisdel/). The availability of all buoy stations refers to the "Data 244 availability" section. The observational sites cover the spatial range of 25°S~ 50.1°N latitude, temporal range span from 1989/12 to 2023/12. Observational meteorological variables and heat fluxes includes the net longwave radiation, net shortwave radiation, sea surface skin temperature, specific humidity at 2m height (if 247 available, or computed as the function of SST according to the Clausius-Clapeyron equation), latent heat flux and sensible heat flux. Limited by the availability of longwave radiation observations, the net radiation has a relatively shorter time series length compared to latent and sensible heat fluxes. The surface air-sea fluxes of buoy observations are computed using the COARE 3.0b algorithm, which have been widely applied for fluxes estimations and validations (Tang et al., 2023; Bentamy et al., 2017; Fairall et al., 2003). All the selected original buoy observation (except for KEO and Papa sites) records are in monthly temporal resolution, and the original daily observations of KEO and Papa has been aggregated to monthly by simple average method. The spatially distributed map of all selected sites is illustrated in Fig.S1.

255

256 **Table 1.** Information about observational ocean surface heat fluxes of 129 buoy sites

257 Note: The number of records represents the effective count (excluding NA values) of latent and sensible heat flux observations.

259 **3.2 Global turbulent heat flux datasets for evaluations**

 This study evaluates and compares 7 global turbulent heat flux products with observations, categorizing them into three types: Remote sensing-based, atmosphere reanalysis-based, and hybrid-based (Table 2). These seven products encompass monthly data spanning from 1988 to 2017, with spatial resolutions ranging from 263 0.25° to 1°. The criterion for dataset filtering prioritizes products that feature relatively longer time series, typically exceeding 15 years.

 The Clouds and Earth's Radiant Energy Systems Synoptic Edition 4A (CERES SYN1deg_Ed4A, 266 hereafter referred to as CERES4, available at https://ceres.larc.nasa.gov/data/) offers net radiation data, derived from clear-sky upward shortwave, downward shortwave flux, upward longwave, and downward longwave flux measurements (Wielicki et al., 1996; Rutan et al., 2015). Another remote sensing-based radiation product, the Global Energy and Water Cycle Experiment - Surface Radiation Budget (GEWEX-270 SRB, available at https://asdc.larc.nasa.gov/project/SRB) (Pinker et al., 1992), in conjunction with CERES4, demonstrates good accuracy in retrieving *Rn*, as validated by six global observing networks (Liang et al., 272 2022). The J-OFURO3 is the third-generation dataset developed by the Japanese Ocean Flux Data Sets with

- 274 use of the Remote-Sensing Observations (J-OFURO) research project (available at https://j-
- 275 ofuro.isee.nagoya-u.ac.jp/en/) (Tomita et al., 2019). It calculates turbulent heat flux with the latest version of

- 276 COARE3.0 algorithm, and provides datasets for *Rn, LE, H* and *SST* in this study. Validation with in situ 277 observations showed that J-OFURO3 offered a superior performance of latent heat compared to other 5 278 satellite products from 2002-2013 (Tomita et al., 2019). 279 Two Atmosphere reanalysis products including the fifth generation European Centre for Medium-Range
- 280 Weather Forecasts (ECMWF) atmospheric Re-Analysis52 (ERA5, available at 281 https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels-monthly-
- 282 means?tab=overview) (Hersbach et al., 2020), and the Modern-Era Retrospective analysis for Research and 283 Applications Version2 (MERRA2, available at 284 https://disc.gsfc.nasa.gov/datasets/M2TMNXOCN_5.12.4/summary) (Gelaro et al., 2017). Both ERA5 and 285 MERRA2 products employ the bulk formula based on the MOST to calculate heat fluxes. Validation results 286 from previous studies have demonstrated good consistency with buoy estimates regarding heat fluxes 287 (Pokhrel et al., 2020; Chen et al., 2020).
- 288 The OAFlux (available at https://oaflux.whoi.edu/), a hybrid-based product developed under the 289 Objectively Analyzed Air-Sea Fluxes (OAFlux) project at the Woods Hole Oceanographic Institution (WHOI) 290 (Yu et al., 2008), was utilized for comparisons with ocean heat fluxes derived from distinct methods. This 291 product calculates fluxes based on the COARE3.0 bulk algorithm and employs a variational objective 292 analysis to determine the optimal fitting of independent variables. Detailed descriptions on all utilized global 293 turbulent heat fluxes products, and their validation performances against buoy observations with reported 294 studies are available in Tang et al (2023).
- 295

296 **Table 2.** The information of the 7 used global radiation and heat fluxes products

297

298

3.3 Ocean heat content data

 Remote sensing data for heat storage (*G*) primarily derive from two categories: one is obtained from the residual of the energy balance equation (*Rn*-*LE*-*H*), including J-OFURO3, ERA5, and MERRA2; the other is calculated as changes in Ocean Heat Content (OHC). The ocean heat content data is obtained from IAP 304 OHC gridded analysis (IAPv4, available at http://www.ocean.iap.ac.cn/) dataset, covering ocean depth of 0- 6000m (Cheng et al., 2017), and has been extensively utilized in global ocean heat analysis, ocean warming, and climate change studies (Li et al., 2023; Cheng et al., 2022; Cheng et al., 2024). The delta OHC is calculated using the numerical differentiation method (Xu et al., 2019) as $OHC(i) = \frac{OHC(i+1) - OHC(i-1)}{2\Delta i}$ *i* $\Delta OHC(i) = \frac{OHC(i+1) - OHC(i-1)}{2\Delta i}$, *i* denotes the OHC of *i*-th month. At the WHOTS site, this study compared the OHC changes at different depths with the observed *G* (derived as *Rn*-*LE*-*H*) (Fig.S1). Since

 the OHC variation from 0~100m depth exhibits the smallest error with the observations, the data from 0~100m depth range were chosen as the heat storage. This study assesses the suitability of *G* flux and ∆OHC for global evaporation estimations, with the aim of minimizing the errors introduced by input variable data in the MEP model.

 This study evaluates the accuracy of all the variables *Rn*, *Ts*, and *G* using the aforementioned datasets on a global scale by comparing them against buoy observations (in Section 4.3), to optimize input accuracy 316 for driving the MEP model. To maintain consistency in the analysis, this study resamples all products to a 1° spatial resolution when comparing the Bowen ratio across multiple products. Nevertheless, when conducting site validations with buoy observations, the original resolution of the data is preserved to minimize uncertainty attributable to scale effects.

4. Results

4.1 The new MEP model with heat storage and the revised Bowen ratio formulas

 To demonstrate how the MEP model has been developed and improved, we show the comparisons of different MEP models in simulating heat fluxes across 129 global buoy stations (Fig.1). Limited by the 324 availability of R_{n} data, we used $LE + H$ instead of the available energy $(R_n - G)$, enabling the utilization of more observational records to verify the MEP model. The original MEP model (without considering heat

 After modifying MEP's energy allocation using four empirical Bowen ratio formulas (denoted as *M_0.24*, *M_0.79*, *M_0.63*, *M_0.37*), the accuracy of MEP predated latent and sensible heat have been 341 significantly improved. The MEP simulated *LE* exhibited strong agreement with observations, with all R^2 exceeding 0.97 and RMSE ranging from 4.7 W·m⁻² (for *M_0.24*) to 7.1 W·m⁻² (for *M_0.79*), which is lower 343 than that derived from equilibrium Bowen ratios (RMSE = 27 W·m⁻²). Both M_0 , 0.79 and M_0 , 0.63 tended to 344 underestimate *LE*, especially when *LE* exceeded 200 W·m⁻² (Fig. 1d and Fig.1e). The results for sensible heat flux simulated by MEP were similar to those for *LE*, the *M_0.24* outperformed the other three, showing the 346 smallest errors and highest R^2 .

348

Figure 1. Scatter density plots of monthly latent heat flux $(a-f)$ and sensible heat flux $(g-I)$ derived by the original and modified MEP methods versus observations from 129 buoy stations (as in Table 1). (a) The 350 original and modified MEP methods versus observations from 129 buoy stations (as in Table 1). (a) The original MEP method, (b) The modified MEP method considering the heat storage effect, (c) The modified 351 original MEP method, (b) The modified MEP method considering the heat storage effect, (c) The modified 352 MEP method considering both the heat storage and empirical Bowen ratio formula $B_{oa} = 0.24B_o^*$, (d) \sim (f) for 353 the modified MEP method considering both the heat storage and empirical Bowen ratio formulas 354 $B_{\alpha\alpha} = 0.79B_{\alpha}^*$ -0.21. $B_{\alpha\alpha} = 0.63B_{\alpha}^*$ -0.15. and $B_{\alpha\alpha} = 0.37B_{\alpha}^*$ -0.05. (g)~(f) are the same with (354 $B_{oa} = 0.79B_o^*$ -0.21*,* $B_{oa} = 0.63B_o^*$ -0.15, and $B_{oa} = 0.37B_o^*$ -0.05. (g)~(l) are the same with (a)~(f) but for 355 sensible heat flux. 356

 Specifically, the spatial errors for the four modified MEP formulas were obtained (Fig. 2), as well as the prediction errors across various observational buoy arrays (Fig.3). Overall, the four modified MEP formulas exhibit lower errors at low latitudes (10°S~10°N), but they demonstrate larger discrepancies at higher latitudes, especially for the KEO, WHOTS, and STRATUS buoy sites. Comparing the four formulas across 361 varying latitudes, the *M_0.24* formula exhibits the smallest RMSE (ranging from 3.6 to 12 W·m⁻²) (Fig. 3c), 362 while the *M_0.79* formula shows the largest errors (RMSE ranging from 3.9 to 26.6 W·m⁻²). This consistency

- 363 is also evident in the Kling-Gupta Efficiency (KGE) coefficient, with *M_0.24* demonstrating superior 364 performance in terms of accuracy, robustness, and adaptability. In term of *M_0.24* formula, the prediction 365 errors across observational arrays ranked as: RAMA < PIRATA < TAO/TRION < PaPa < KEO < STRATUS 366 < WHOTS < NTAS. The arrays with relatively larger RMSE (NTAS in the Atlantic Ocean, WHOTS, and 367 STRATUS in the Pacific Ocean) may originate from the larger observed values of LE (Fig. S2).
	- (a) MEP (M_0.24) (b) MEP (M_0.79) $\overline{5}$ $\frac{1}{100}$ 100 $\frac{1}{100}$ 100 (d) MEP (M_0.37) (c) MEP (M_0.63) **MSE** 25
20
15
10 50 $50 - 50$ $(W/m²)$

369

368

370 **Figure 2.** Spatial distribution of RMSE values in the comparison of latent heat flux estimated by the improved MEP method (modified by four different Bowen ratio formulas) with buoy observations fr 371 improved MEP method (modified by four different Bowen ratio formulas) with buoy observations from 129 stations.

Figure 3. Comparisons of latent heat flux estimated by the improved MEP method with buoy observations 376 from each buoy array in term of RMSE (a) KGE value (b), and latitudinal means of RMSE of four empirical 376 from each buoy array in term of RMSE (a) KGE value (b), and latitudinal means of RMSE of four empirical 377 Bowen ratio formulas (c). Latitudinal means are based on data from 129 available buoy sites. Bowen ratio formulas (c). Latitudinal means are based on data from 129 available buoy sites.

4.2 Dynamics of heat fluxes and Bowen ratio between original and improved MEP model

 To thoroughly investigate the role of heat storage in the partitioning of surface energy and its implications for the temporal dynamics of heat fluxes, we selected the KEO site for detailed analysis. This decision was based on the site's extensive long-term observational records and notable variability in flux patterns, which offer an ideal context for a rigorous comparison of model-simulated error margins. The improved MEP methods demonstrated comparable performance in estimating heat fluxes at the KEO site when compared with 128 other sites (Fig. S3, Fig. 1), with the MEP (M_0.24) model exhibited the most effective performance. Analysis of the time series data revealed significant variations in latent heat, sensible heat, and Bowen ratio (Fig. 4). In the original MEP theory, the estimated *LE* exhibits an opposite variation cycle (peak versus trough) compared to the observations. For instance, over a yearly period, the 389 observed peak in *LE* occurred in January 2005 (269 W·m⁻²) and the trough in June 2005 (6.9 W·m⁻²). In

- 390 contrast, the MEP simulated the peak in *LE* to occur in August 2005 (105 W·m⁻²) and the trough in December
-
- $2004 (0.7 W·m⁻²)$, resulting in a phase difference of 7 months for the peak and 6 months for the trough values.
- Sensible heat flux (Fig. 4b) showed similar phase differences: observed *H* peaked in January 2005 (79 W·m⁻

- 393 a) and reached its minimum in June 2005 (-3 W·m⁻²), whereas MEP simulated *H* to peak in August 2005 (46 $W(m^{-2})$ and reach its minimum in December 2004 (0.6 W·m⁻²), consistent with the pattern observed for *LE*. 395 It is noteworthy that the original MEP model simulated variations in LE and H align with R_n (Fig. S4), which 396 is reasonable over land where the small *G* value can often be disregarded. However, over the ocean, the 397 observed variations in R_n and *LE* do not align in terms of their cycles. The maximum R_n occurred in June 398 2004 (329 W·m⁻²) and the minimum occurred in December 2004 (142 W·m⁻²), with a 6-month delay in 399 relation to the variations in *LE*. Specifically, the peak *Rn* corresponded to the trough of *LE*, and the trough 400 *Rn* corresponded to the peak of *LE*. This delay indicates that the heat storage effect delays the peak of *LE* and 401 alters the seasonal variations of *LE* and *H*.
- 402

403

404 **Figure 4.** MEP model predicted latent heat flux (a), sensible heat flux (c), Bowen ratio (e) versus observations, 405 and corresponding boxplots (b, d, f) of these variables at KEO site from June 17, 2004, to August 12, 2023. 406 Note that the (a) and (c) only display results using MEP *(M_0.24)* among all four empirical Bowen ratio 407 formulas for clearer comparison.

 For the variation pattern of the Bowen ratio, both the original MEP formula and the modified formulas exhibit consistent patterns with the observed values. The observed maximum Bowen ratio occurred in January 2005 (0.29), and the minimum in June 2005 (-0.4). However, the original MEP formula simulated a maximum of 1.01 and a minimum of 0.44, indicating a significant overestimation compared to the observed Bowen ratio. This discrepancy suggests that on the ocean surface, the available energy (*Rn-G*) is predominantly allocated to *LE* (Fig.S4). Among four empirical formulas, *M_0.24* simulated *LE*, *H*, and Bowen ratio values closest to the observed values. The median of the observed Bowen ratio was 0.11, while the original MEP Bowen ratio was 0.66. Among the four modified Bowen ratio formulas (*M_0.24*, *M_0.79*, *M_0.63*, *M_0.37*), their median Bowen ratios were 0.15, 0.32, 0.27, and 0.19 respectively, with *M_0.24* being the closest to the observed Bowen ratio.

 Heat storage is crucial for the energy distribution process over the ocean surface. While the original MEP formulas have been effectively validated when applied to surfaces with shallow depths such as water and snow (Wang et al., 2014), they exhibit significant uncertainty when applied to the ocean surface. This discrepancy primarily arises from the fact that land is a non-transparent medium with relatively small heat storage values at monthly scales. Similarly, shallow water bodies also exhibit small heat storage values that can often be ignored. In the study by Wang et al. (2014), for example, two lakes with depths of 2m (Lake Tämnaren) and 4m (Lake Råksjö) still resulted in underestimated *LE*. However, for deeper lakes (generally > 3m depth), heat storage becomes significant and cannot be neglected (Zhao et al., 2016; Zhao & Gao, 2019). On deep ocean surfaces, with the most recent average depth estimate of 3,682 meters from NOAA satellite measurements, heat storage variations can influence depths up to 6,000 meters (Cheng et al., 2017). Therefore, the impact of heat storage is substantial and cannot be disregarded. In the original MEP theory, heat storage was not considered in the energy balance equation, where it was assumed that the net solar radiation (*Rns*) is 431 absorbed by the ocean and $R_{nL} = LE + H + Q$. Then, the heat storage was obtained as $G = R_{ns} + Q$. In this 432 study, we compared the characteristics of MEP-derived G ($R_{ns} + Q$) with the observed G flux ($G = R_n - LE$ – *H* (Fig. S5). MEP-derived *G* shows a good correlation (*R* = 0.96) and consistent trends with the observed 434 values (Fig. S5a & b), ranging from -4 to 81 W·m⁻². However, MEP-calculated *Q* (ranged from -210 to -65 435 W·m⁻²) exhibits a negative correlation with the observed G (which ranged from -386 to 200 W·m⁻²). Both MEP-derived *G* and *Q* fluxes are significantly underestimated. Therefore, the prediction errors in *LE* and *H*

- 437 originates from the inability to accurately quantify heat storage. Hence, considering the influence of heat
- 438 storage is crucial for accurately predicting *LE* and *H* over the ocean surface.
- 439 **4.3 Evaluation of global radiation and heat storage flux**
- 440 4.3.1 Evaluation of net radiation

 After considering the effect of heat storage and the Bowen ratio, the improved MEP method demonstrated its high performance at the site scale. The results suggest that improved MEP method holds substantial promise for further application at a global scale. To facilitate this, we assessed the primary input variables of 444 the improved MEP method (including R_n , G , and T_s) to identify datasets with the best accuracy.

 Net radiation, as the primary variable in the energy balance equation, significantly influences the 446 uncertainty of the MEP model (Huang et al., 2017). Selecting a reliable R_n product is essential for accurately estimating global latent and sensible heat fluxes. Previous studies have evaluated *Rn* at daily scales (Liang et al., 2022). In this study, we conducted a comprehensive evaluation of current mainstream monthly *Rn* products, including three remote sensing-based products (CERES, GEWEX-SRB, and JOFURO3) and two atmosphere reanalysis-based products (ERA5 and MERRA2). All products exhibited good consistency with 451 buoy observations (Table 3 and Fig. S6), with R^2 values greater than 0.78. In terms of RMSE, the error 452 rankings for all products were as: J-OFURO3 (10 W·m⁻²) < ERA5 (39.03 W·m⁻²) < CERES (40.67 W·m⁻²) 453 < GEWEX-SRB (41.83 W·m⁻²) < MERRA2 (49.23 W·m⁻²). It is evident that J-OFURO3 demonstrated the highest accuracy, as indicated by RMSE, NSE, and KGE statistics. This study is also consistent with previous assessments of global radiation (Liang et al., 2022), emphasizing J-OFURO3 as the least erroneous among all individual products and superior to existing alternatives including CERES4, ERA5, MERRA2, GEWEX-SRB, JRA55, OAFlux, and TropFlux.

458 **Table 3.** Evaluation of global monthly net radiation products against buoy observations

Products	R^2	ME $(W \cdot m^{-2})$	MAE $(W \cdot m^{-2})$	RMSE $(W \cdot m^{-2})$	PBIAS (%)	NSE	KGE
J-OFURO3	0.96	1.6	7.3	10.0	1.0	0.96	0.97
ERA5	0.79	28.8	30.3	39.0	17.8	0.45	0.77
MERRA ₂	0.78	39.7	41.2	49.2	24.8	0.15	0.68
CERES	0.81	31.4	32.6	40.6	19.6	0.42	0.76
GEWEX-SRB	0.78	32.6	33.8	41.8	20.2	0.37	0.76

459 Note: The evaluation period for all datasets is 1988-2017, except for CERES, which spans from March 2000

460 to December 2017. The best-performed statistics are indicated in bold type.

461 4.3.2 Evaluation of heat storage

 The study underscores the importance of considering heat storage in simulating heat fluxes using the improved MEP model. For the first time, we assessed global heat storage using the J-OFURO3, ERA5, MERRA2, and ΔOHC datasets. In addition to assessing these individual datasets, we investigated the potential for enhancing accuracy through data fusion methods. We employed the BTCH and AA method to fuse heat storage data and compared the accuracy between individual datasets and fused datasets (Table 4). The results reveal that while using the AA method (e.g., AA4) to fuse yields smaller errors compared to ERA5, MERRA2, and ΔOHC, it still failed to achieve the accuracy of the J-OFURO3 product. Similarly, the BTCH method, despite fusing data from three or four sources, also does not match the accuracy of the J-470 OFURO3 method, as indicated by metrics of R^2 , RMSE, and KGE. The heat storage derived from J-OFURO3 471 data shows high consistency with observations $(R^2=0.95)$, as illustrated in Fig. 5 (spatial distribution of errors depicted in Fig.S7). Therefore, this study adopts the heat storage data derived from the J-OFURO3 dataset as the input for the MEP model.

 To ensure consistency with radiation data source, the Sea surface temperature (SST) data from J- OFURO3 is utilized for *Ts* inputs, which is derived as the ensemble median from 12 global *SST* products (Tomita et al., 2019). Ultimately, the input variables including net radiation, heat storage, and sea surface temperature for driving MEP model are all determined from the J-OFURO3 dataset spanning from 1988 to 2017. Saturated specific humidity is computed as a function of *SST* and surface air pressure (from ERA5) 479 using the Clausius-Clapeyron equation. The reliability of gridded data for the variables R_n , G , and T_s are simultaneously examined at an observational site (Fig.S8), where all three variables demonstrated high 481 consistency with observed data from August 2004 to December 2017 (with $R^2 > 0.96$), effectively capturing 482 the monthly dynamics of R_n , G , and T_s .

484 **Table 4.** Assessment of monthly heat storage between global remote sensing datasets and buoy observations

Products	\mathbb{R}^2	МE $\mathbf{W}\cdot\mathbf{m}^{-2}$	MAE $(W \cdot m^{-2})$	RMSE $(W \cdot m^{-2})$	PBIAS $(\%)$	NSE	KGE
J-OFURO3	0.95	-3.5	15.3	19.7	-7.4	0.94	0.91
ERA5	0.88	7.0	25.1	33.2	14.8	0.84	0.80
MERRA ₂	0.86	11.6	27.1	36.1	24.5	0.81	0.72
OHC	0.35	-48.2	64.4	86.9	-101.9	-0.11	-0.10

485 Note: BTCH3-1 represents the fusion of three products (ERA5, MERRA2, and J-OFURO3) using the BTCH
486 method; TCH3-2 represents the fusion of ERA5, MERRA2, and OHC; BTCH4 represents the fusion of ERA5, 486 method; TCH3-2 represents the fusion of ERA5, MERRA2, and OHC; BTCH4 represents the fusion of ERA5,
487 J-OFURO3, MERRA, and OHC. AA denotes the Simple Arithmetic Average (AA) method. The evaluation 487 J-OFURO3, MERRA, and OHC. AA denotes the Simple Arithmetic Average (AA) method. The evaluation 488 period spans from 1988 to 2017, and the best-performed statistics are indicated in bold type.

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492 **Figure 5.** Assessment of heat storage (G) flux derived from remote sensed J-OFURO3 dataset against buoy 493 observations. Distinct colors represent data from different buoy arrays.

494

495 **4.4 Estimating long-term global ocean surface heat fluxes by improved MEP model**

496 4.4.1 New estimate of global latent and sensible heat fluxes

- 498 (i, e., *M_0.24*, hereinafter referred to as MEP for simplicity, while the original MEP formula is denoted as
- 499 *MEP (ori)*) for global scale estimation, producing new estimations of latent and sensible heat fluxes for the
- 500 period 1988-2017 (Table 5). The MEP model calculated the multi-year average *LE* as 92.87 W·m⁻² and the

⁴⁹⁷ After identifying the optimal driving dataset, this study employs the best-performed improved MEP method

 Regarding the global spatial pattern (Fig.6), the MEP-derived latent heat shows higher values in low- latitude regions but notably decreases beyond 45° latitude. The highest LE values are observed in the southern Indian Ocean near Australia, the Pacific and Atlantic regions near South America, and the Indian Ocean near southern Africa. The peak values are observed within western boundary current systems (ranging from 200 512 to 260 W·m⁻²), including the Gulf Stream in the North Atlantic and the Kuroshio in the western North Pacific. Impacted by the variations in oceanic currents near the equator, two general areas of higher *LE* have emerged 514 (Yu et al., 2011), leading to notably low *LE* at the equator $(88 \text{ W} \cdot \text{m}^2)$, peaking at ~18°S at 132 W·m⁻² (Fig. 6 & Fig.7). The MEP estimated *LE* exhibits a similar spatial pattern with other four products globally (Fig.6), particularly resembling OAFlux between 15°S and 15°N (Fig. 7). Overall, for the region between 30°S and 30°N, the ranking of LE values is as follows: OAFlux < MEP < J-OFURO3 < ERA5 < MERRA2, which is consistent with the magnitude of available energy. For sensible heat, MEP-derived H closely resembles that of ERA5 and MERRA2, with higher values predominantly occurred in two western boundary current systems, the South Indian Ocean near Australia area, and the Arctic Ocean. The improved MEP method mitigates the issue of overestimating *H* in mid-to-high latitudes compared to its original form (Fig.6l), resulting in more realistic spatial patterns. In high latitudes, J-OFURO3 exhibits higher H values than MEP and other comparable products in the Northern Hemisphere, with negative values observed between 45°S and 55°S. MEP generally estimates H within an intermediate range compared to other products, displaying a distribution that is more reasonable than that of J-OFURO3 product.

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LE products	LE $(W \cdot m^{-2})$	Evaporation (mm/yr)	H $(W \cdot m^{-2})$	G $(W \cdot m^{-2})$
MEP(0.24)	92.8	1195.5	12.2	19.7
ERA5	99.2	1277.8	12.0	34.2
MERRA2	100.5	1294.3	13.2	35.5
J-OFURO3	94.9	1222.2	10.1	19.7
OA flux	88.9	1145.1	10.4	
MEP (ori)	52.7	678.5	25.1	42.2

530 **Table 5.** Global area-averaged multi-annual mean estimates of latent heat flux

531 Note: The period spans from 1988 to 2017. The MEP (0.24) denotes the improved MEP model, while MEP (0.24) denotes the original MEP model. (ori) represents the original MEP model.

533

-OFURO3 LE ERA5L MEP LI (a) (b) $\left(c \right)$ Latent heat flux MERRA2 LE OAFlux LE MEP(ori) LE (d) (f) (e) (h) (i) (g) Sensible heat flux (j) (k) OAFlu: $\left(\mathsf{I}\right)$ MEP(S.

535 **Figure 6.** Global spatial maps of annual mean latent heat flux (*LE*) and sensible heat flux (*H*) during 1988- 536 2017. Panels (a)-(f) depict latent heat flux derived from the improved MEP method, J-OFURO3, ERA5,

 MERRA2, OAFlux, and the original MEP method. Panels (g)-(l) show sensible heat flux from the same datasets.

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 Figure 7. Meridional profiles of latent heat (left panel), sensible heat (middle panel) and their sum representing available energy (right panel) for the period 1988-2017.

4.4.2 Validation of global latent heat

 To evaluate the disparity between MEP estimates of LE and those of other existing products, this study validated global-scale LE using 129 observational sites (as depicted in Fig.8 & Table 6). MEP-estimated LE 548 showed strong consistency with buoy observations, achieving an R^2 of 0.79, a ME of 1.26 W·m⁻², and RMSE of 16 W·m⁻², all surpassing those of alternative products, underscoring its superior performance. Moreover, the MEP method exhibited superior performance with a higher NSE value of 0.77 and KGE of 0.89, demonstrating enhanced accuracy, reliability, and robustness. According to the RMSE evaluation criterion, the ranking of best-performed *LE* products is as: MEP, J-OFURO3, OAFlux, ERA5, MERRA2. In a recent comprehensive assessment of 15 global LE products (Tang et al., 2023), RMSE values ranged from 17.2 to

554 45.3 W·m⁻², in which J-OFURO3 emerged as the best-performing product with the lowest RMSE of 17.2 555 W·m⁻², highest correlation coefficient (R) of 0.89, and ME of 6.5 W·m⁻². Studies have also shown minimal bias are given by J-OFURO3 on daily scale (Bentamy et al., 2017). This superior performance can be attributed to the use of continuously updated bulk algorithms (COARE 3.0 version) by J-OFURO3, the ongoing optimization of near-surface parameters (Tomita & Kubota, 2018), as well as the improved spatial resolution (0.25°). In this study, the improved MEP estimates of *LE* outperformed that of J-OFURO3, 560 demonstrating higher accuracy and lower error (ME=1.26 W·m⁻²), thereby establishing it as the most accurate global *LE* product currently available.

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Figure 8. Scatter density plots of latent heat flux derived from distinct methods versus observations from 564 129 buoy stations during the period 1988-2017: (a) Improved MEP method, (b) J-OFURO3, (c) ERA5, (d) 564 129 buoy stations during the period 1988-2017: (a) Improved MEP method, (b) J-OFURO3, (c) ERA5, (d) 565 MERRA2, and (e) OAFlux. A total of 15444 records of latent heat observations are included.

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567	Table 6. Evaluation of latent heat flux from different methods against buoy observations											
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568 Note: The evaluation period spans from 1988 to 2017, and the best-performed statistics are indicated in bold

569 type.

4.4.3 Comparisons of Bowen ratios

 The improved MEP model achieves accurate LE estimates after refining the process of partitioning the surface energy budget, specifically through revisions to the Bowen ratio. The improved MEP method notably decreased the global-scale Bowen ratio, as illustrated in Fig. 9 and 10. Regarding latitude averages, the Bowen ratio of the original MEP formula ranged from 0.37 to 1.48 (with a median of 0.80), whereas the modified MEP Bowen ratio ranged from 0.09 to 0.35 (median of 0.18). Specifically, in the low-latitude region (10°S-10°N), the Bowen ratio of the modified MEP formula decreased from 0.37 to approximately 0.1, aligning closely with the Bowen ratios obtained from other reanalysis products (MERRA2, ERA5, OAFlux, and J-OFURO3). Globally, the median Bowen ratios of the products are as follows: MERRA2 (0.15), MEP (0.12), ERA5 (0.09), OAFlux (0.08), and J-OFURO3 (0.06). Spatially, the MEP Bowen ratio resembles ERA5 in mid to low latitudes but exhibits deviations from other products at high latitudes, where those products show fluctuating changes in the Bowen ratio (Fig.10). For instance, other products display abrupt transitions from negative to positive Bowen ratios in the Arctic and Antarctic regions, whereas MEP-derived values demonstrate greater stability in variations at higher latitudes. This discrepancy is likely due to the reanalysis products relying on the bulk method, which is sensitive to variations in wind speed and temperature gradients, leading to errors in simulating high wind speeds at the poles and causing fluctuations in latent and sensible heat. In contrast, the MEP model strictly adheres to energy conservation principles and operates independently of wind speed and temperature gradients, resulting in a more accurate estimate of the Bowen ratio. For example (Fig.S9), at the high-latitude PAPA buoy site (144.9°W, 50.1°N), the Bowen ratio estimated by MEP (median 0.24) closely matches the observed Bowen ratio (median 0.23). In contrast, all the other products underestimated the Bowen ratio, with J-OFURO3 (median -0.09) and OAFlux frequently exhibiting negative values. The Bowen ratio derived from MEP fits well with a Generalized Additive Model (GAM) (Fig.9). The implicit functional relationship between Bowen ratio and latitude is expressed as $(R^2 =$ 593 0.996, $p < 0.001$: B_{oa} (lat) = 0.207218 + $f(lat)$ + ε , where $f(lat)$ represents a smoothing function derived from 594 a smooth curve, and ε denotes the error term. However, the specific functional form of $f(lat)$ cannot be explicitly determined. Therefore, a polynomial regression method is employed to explicitly fit *Boa* and *lat*, 596 resulting in $(R^2 = 0.91, p < 0.001)$: $B_{oa} = 9.97 \times 10^{-2} - 3.45 \times 10^{-4} \times lat + 4.71 \times 10^{-5} \times lat^2 + \varepsilon$ (as in Fig.S10). This equation serves as a reference for partitioning surface energy over data-sparse oceanic regions.

 Figure 9. Global ocean latitudinal averaged Bowen ratio derived by the MEP method and four other products from 1988 to 2017. (a) Latitudinal averaged Bowen ratio derived from the MEP model using original and modified Bowen ratio formulas, with points fitted by a generalized additive model (GAM). (b) Statistical distribution of the latitudinal annual mean Bowen ratio.

 Figure 10. Global distribution of ocean annual mean Bowen ratio during 1988-2017: (a) Improved MEP method, (b) J-OFURO3, (c) ERA5, (d) MERRA2, (e) OAFlux, and (f) MEP original method.

4.5 Spatial-temporal variability of ocean evaporation

 Over the multi-year changes from 1988 and 2017, MEP, J-OFURO3, ERA5, and MERRA2 all exhibited significant increasing trends in *ET*. MEP estimated an evaporation increased rate of 2.31 mm/year, whereas OAFlux showed a non-significant trend (Fig.12). This upward trend in ET can largely be attributed to changes 623 in available energy, which increased at a rate of 0.274 $W/(m^2 \text{·year})$. For instance, during peak *ET* years such as 1989, 1992, 2003, and 2008, *Rn* was also at its highest; conversely, during years of minimum *ET* like 1991 and 1997, *Rn* was minimal. This consistency is in line with previous findings (Huang et al., 2017), where more than 50% of the uncertainty in MEP-modeled fluxes was attributed to the radiation term. While different methods yield varying magnitudes of *ET* changes, they generally exhibit a transition around 2010: an increasing trend from 1988 to around 2010 followed by a decreasing trend thereafter (Fig. 12a). For instance, MEP indicated an ET increase of 3.58 mm/year from 1988 to 2010, followed by a decrease at a rate of 2.18 mm/year after 2010. This shift primarily results from a decline in both available energy and surface temperature starting around 2010. Although *Ts* increased after 2012, the significant decrease in available energy was the main driver behind the decline in *ET*.

 Figure 12. Time series of area-averaged multi-annual mean evaporation from the improved MEP method (a), available energy (b), and sea surface temperature (c) over the global oceans during 1988-2017. The black dotted line in panel (a) represents year 2010, and the black dashed lines in panels (b) and (c) represent the linear regression lines.

5. Discussion

5.1 Quantifying impact of heat storage and radiation with sensitivity analysis

 The sensitivity analysis reveals the significant influence of input variables on latent heat flux derived from the MEP model. Notably, the heat storage (*G*) exhibits seasonal variations with both positive and negative values (Fig. 13). Positive *G* values coincide predominantly with summer in the Northern Hemisphere (winter in the Southern Hemisphere), specifically from June to August (Fig. 4 and Fig. S5). During this season, 649 intensified solar radiation enhances the net energy input (R_n) at the ocean surface, leading to heat absorption and retention. Consequently, the energy available (*Rn* - *G*) for evaporation diminishes. The analysis indicates that *Rn* significantly influences the energy-driven evaporation process, with a sensitivity coefficient exceeding 1 (median 1.74), highlighting its pivotal role. In contrast, *G* negatively impacts evaporation, as indicated by a sensitivity coefficient of -0.74. Specific humidity (median 0.08) and sea surface temperature have relatively minor effects, consistent with previous MEP model findings focused on terrestrial surfaces (Isabelle et al., 2021).

 Conversely, negative values of heat storage predominate during winter, particularly from December to February in the Northern Hemisphere (June to August in the Southern Hemisphere). Despite reduced solar radiation during this period, residual heat stored from summer gradually releases into the atmosphere, resulting in greater energy output than input. This surplus energy augments the available energy for evaporation, leading to a positive sensitivity coefficient for *G* (median 0.29), second only to *Rn* (median 0.71). Consequently, this process generally reduces sea surface temperature, resulting in a negative sensitivity coefficient for surface temperature. Overall, these findings underscore the significant influence of *Rn* on latent heat flux, with *G* ranking as the second most influential variable in MEP estimates over ocean surfaces. For instance, a 10% decrease in positive *G* yields a 7.4% increase in evaporation, while a 10% increase in negative *G* results in a 2.9% increase in evaporation, assuming other variables remain constant. Thus, *Rn* and *G* emerge as primary drivers of oceanic evaporation, with humidity and temperature exerting minimal influence.

 Furthermore, the pivotal role of available energy in determining *LE* is underscored by its direct relationship with energy allocation. Thus, the accuracy of available energy estimates directly influences *LE* simulations. Despite using bulk methods (COARE 3.0 algorithms) independent of radiation partitioning,

 discrepancies in *LE* simulations correlate with errors in available energy estimates (Tables 3 and 4). Notably, the MERRA2 product exhibited higher errors in simulating *Rn* and *G* compared to observations, leading to significant biases in *LE* estimation. In contrast, ERA5 product demonstrated superior performance in 674 simulating R_n and G , thereby achieving higher accuracy in *LE* estimation. Consequently, the energy-balance- based MEP model excels in accurately computing surface heat fluxes by directly reflecting energy allocation. Unlike bulk methods, the MEP approach reduces sensitivity to temperature and humidity gradients, thereby minimizing uncertainties in *LE* simulations (Pelletier et al., 2018). This advancement enhances the MEP model's utility in global energy and water cycle research, particularly pertinent for future climate change studies.

Figure 13. Sensitivity coefficient associated with inputs variables for the improved MEP method at all 129 buoy stations: (a) for positive G values, and (b) for negative G values. buoy stations: (a) for positive G values, and (b) for negative G values.

5.2 Discrepancy of empirical Bowen ratio formulas

 Bowen ratio plays a crucial role in understanding the surface energy partitioning process. In this study, four empirical formulas were utilized to modify the MEP model and were evaluated against observations of latent heat flux, each with distinct conditions of applicability and suitability for integration with the MEP model: $(1) B_{oa} = 0.63B_0^*$ -0.15 is derived from direct observational data fitting (Hicks and Hess, 1977). This formula is applicable for surface temperatures above 16°C, particularly within latitudes between 40°N and 40°S, making it more suitable for lower latitude regions. Therefore, it is more suitable for lower latitude regions; $(2) B_{oa} = 0.79B_0^*$ -0.21 is derived using the Priestley–Taylor model under advection-free conditions (Priestley

693 and Taylor, 1972). The coefficients are based on a mean α value of 1.26 (although this varies in practice). However, recent studies have shown significant discrepancies due to the neglect of the interaction between 695 *R_n* and *T_s* variations (Yang & Roderick, 2019); (3) $B_{oa} = 0.24B_o^*$ was developed to address this limitation 696 based on a maximum evaporation theory by considering the feedback mechanism between R_n and T_s (under 697 the circumstances of G to be small to negligible). The empirical coefficient (0.24) was determined by fitting Bowen ratio and surface temperature data across the global ocean surface (Yang & Roderick, 2019); and (4) $B_{oa} = 0.37B_o^*$ -0.05 was subsequently formulated based on principles derived from atmospheric boundary layer (ABL) theory (Liu & Yang, 2021), with coefficients also fitted from relationships between *Boa* and *Ts*. 701 It should be noted that the derivations of $B_{oa} = 0.24B_o^*$ and $B_{oa} = 0.37B_o^*$ -0.05 were based on fitting using latent heat data from the OAFlux dataset rather than direct buoy observations. Building upon the four 703 empirical relationships between B_{oa} and B_o^* from previous studies, this study assessed the applicability of these four empirical Bowen ratio formulas in estimating latent heat flux. The findings indicate that the MEP 705 model refined with $B_{oa} = 0.24B_o^*$, exhibits superior accuracy at both localized and global scales, effectively mitigating the underestimation of LE in its original formulation. Moreover, the results show that the improved MEP model closely aligns with buoy observations and achieves higher accuracy globally compared to OAFlux products (as depicted in Fig. 8), surpassing other bulk method-based products as well.

5.3 Contributions and implications of this study

 The main contributions of this study include: (1) The MEP model's energy balance equation over water surfaces was revised to explicitly consider heat storage effect. This correction highlights the importance of heat storage in estimating latent heat flux. (2) The energy partitioning of the MEP model was revised to incorporate empirical Bowen ratio formulas, significantly improving the heat flux estimations. (3) This study conducted the first thorough global assessment of heat storage using extensive buoy observations and remote sensed data, enabling the MEP model to produce the most accurate global latent heat flux estimates. This study addresses the issue of underestimating latent heat flux by the MEP model, increasing the global average 717 LE from 53 W·m⁻² to 93 W·m⁻², while reducing sensible heat flux from 25 W·m⁻² to 12 W·m⁻², improving the partitioning of energy budget. The improved MEP model provides precise LE estimates compared to existing datasets like J-OFURO3, ERA5, MERRA2, and OAFlux, enabling it to become a valuable benchmark dataset for global evaporation studies.

 This study applies the improved MEP model to ocean surface, with potential for future extension to lake and reservoir surfaces. Compared to the Penman model for water body evaporation (Tian et al., 2022; Zhao et al., 2022; Bai et al., 2023), major advantage of MEP method lies in its independence from wind speed, as long as the heat storage can be determined using an equilibrium temperature-based approach (McMahon et al., 2013; Zhao & Gao, 2019). The global LE dataset generated in this study, given MEP's insensitivity to variations in air temperature and humidity, can be applied in studies related to ocean salinity (Liu et al., 2019), ocean warming (Cheng et al., 2022), global climate change and water cycle research (Konapala et al., 2020).

6. Data availability

 The dataset produced using the MEP method, which includes global latent heat flux and sensible heat flux at a monthly scale from 1988 to 2017, can be freely downloaded from the Figshare platform (https://doi.org/10.6084/m9.figshare.26861767.v2, Yang et al., 2024). All the datasets used in this study are publicly available online and are described in the Data Materials section.

7. Conclusions

 In this study, we developed a global monthly latent heat flux product for the ocean covering the period from 1988 to 2017. This product is based on a maximum entropy production theory framework, incorporating heat

 storage and Bowen ratio optimizations. It represents the first energy-balance-based dataset that differs from existing global ocean heat flux datasets derived from bulk methods. To assess the accuracy of the input variables for the maximum entropy production framework, we utilized five global datasets, including two remote sensing-based and three from reanalysis-based, alongside four global datasets of heat storage derived from the energy balance equation and ocean heat content changes. We employed data fusion methods, including arithmetic averaging and the Bayesian three-cornered hat method, to identify optimal input datasets through validation against observations. The performance of the newly produced dataset was evaluated against extensive observations from 129 globally distributed buoy stations using multiple statistical metrics, and it was also compared with four auxiliary products: J-OFURO3, ERA5, MERRA2, and OAFlux. Additionally, we analyzed the long-term spatial-temporal variability of ocean latent heat flux. Ultimately, we investigated the impacts of ocean heat storage, net radiation, and Bowen ratio changes on heat flux estimations and surface energy partitioning.

 The MEP framework provides new estimates of global heat fluxes. The MEP-estimated long-term 760 annual mean latent heat flux is 93 W·m⁻² (equivalent to 1196 mm/year of evaporation) during the period from 1988 to 2017. This estimate is at an intermediate level compared to other global flux products, which range 762 from 90 W·m⁻² (OAFlux) to 101 W·m⁻² (MERRA2). The MEP-estimated sensible heat flux is 12 W·m⁻², 763 falling within the range of 10.17 W·m² (J-OFURO3) to 13 W·m² (MERRA2) reported by other current products. Compared with previous heat flux products, the MEP-estimated latent heat demonstrated higher 765 accuracy when validated against observations, with a ME of 1.26 W·m⁻², a RMSE of 16 W·m⁻², and a KGE value of 0.89, outperforming all other contemporary global products. Approximately 74% of oceanic regions experienced an increasing trend in evaporation from 1988 to 2017. Regarding long-term temporal variability, the global annual mean evaporation exhibited an increase rate of 3.58 mm/yr from 1988 to 2010 but subsequently decreased at a rate of 2.18 mm/yr from 2010 to 2017, which was consistent with changes in surface available energy.

 This study demonstrates that the improved MEP framework has significantly improved the accuracy of the original MEP theory, addressing both the underestimation of latent heat and the overestimation of sensible heat flux. This improvement was achieved by incorporating the impact of heat storage and modifying the Bowen ratio formula within the MEP theory. The consideration of heat storage resolved the issue of seasonal

- phase mismatches (approximately 6-month lags) between MEP estimates and buoy observations. Building upon this improvement, this study further optimized the energy partitioning process by correcting the Bowen ratio, linearly adjusting the equilibrium Bowen ratio to align with actual conditions. Four empirical Bowen 778 ratio formulas for modifying the MEP method were assessed globally, identifying $B_{oa} = 0.24B_o^*$ as the most accurate formula for estimating latent heat flux within MEP method. The impact of heat storage on estimating heat fluxes was quantified through the sensitivity analysis. Net radiation and heat storage were identified as the primary drivers of evaporation estimates. A 10% decrease in positive heat storage led to a 7.4% increase in evaporation, whereas a 10% increase in negative heat storage resulted in a 2.9% increase. Compared to existing bulk methods, the MEP model offers several advantages including the need for
- fewer input variables, independence from wind speed, and insensitivity to variations in temperature and humidity. The MEP derived ocean heat flux dataset has been validated and provides accurate estimates of latent heat flux. Additionally, this MEP method can be applied to estimate evaporation from other deep-water surfaces, such as lakes and reservoirs where heat storage is significant. Overall, the MEP-derived ocean heat flux dataset provides high global accuracy, fine spatial resolution (0.25°), and extensive long-term temporal records. This dataset is expected to be valuable for applications related to global ocean warming, hydrological cycles, and their interactions with other Earth system components in the context of climate change.
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