A regional pCO_2 climatology of the Baltic Sea from in situ pCO_2 observations and a model-based extrapolation approach

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Abstract. Ocean surface pCO_2 estimates are of great interest for the calculation of air-sea CO_2 fluxes, oceanic uptake of anthropogenic CO_2, and eventually the Global Carbon Budget. They are accessible from direct observations, which are discrete in space and time and thus always sparse, or from biogeochemical models, which only approximate reality. Here, a combined method for the extrapolation of pCO_2 observations is presented that uses (1) model-based patterns of variability from an EOF analysis of variability with (2) observational data to constrain EOF pattern amplitudes in (3) an ensemble approach, which locally adjusts the spatial scale of the mapping to the density of the observations. Thus, data-constrained, gap- and discontinuity-free mapped fields including local error estimates are obtained without the need for or dependence on ancillary data (like, e.g., satellite sea surface temperature maps). This extrapolation approach is generic in that it can be applied to any oceanic or coastal region covered by a suitable model and observations. It is used here to establish a regional pCO_2 climatology of the Baltic Sea, largely based on ICOS-DE SOOP *Finnmaid* surface pCO_2 observations between Lübeck-Travemünde (Germany) and Helsinki (Finland). The climatology can serve as improved input for atmosphere-ocean CO_2 flux estimation in this coastal environment.

1 Introduction

The ocean plays a major role in the global carbon cycle, and has a controlling function on the atmospheric CO_2 content on longer time scales (DeVries, 2022). Since the rise of atmospheric CO_2 concentrations since the beginning of the pre-industrial period (year 1750), the ocean has taken up ∼25 % of the CO_2 released from human activities (Friedlingstein et al., 2022), with the annual uptake mainly related to the increase in the air-sea pCO_2 imbalance. The role of coastal and continental shelf waters is more complex. Apart from atmospheric CO_2 levels, changes in nutrient loads and organic matter supply from land, changes in weathering in the drainage basin, and even changes on the functioning and composition of biological key players on various levels can lead to changes in the inorganic carbon system and thus, the source-sink function of coastal seas (e.g., Laruelle et al., 2018; Müller et al., 2016; Carstensen and Duarte, 2019; Kuliński et al., 2022). Moreover, coastal seas provide an important conduit of land-derived carbon into the open ocean's interior (e.g., Thomas et al., 2004).

For the Baltic Sea, several attempts have been made to quantify the net CO_2 air-sea balance in form of a pCO_2 climatology, as well as to derive trends in surface water pCO_2, with partly contradicting results (e.g., Omstedt et al., 2009; Parard et al., 2016, 2017; Becker et al., 2021; Neumann et al., 2022; Wesslander et al., 2010). Most of the approaches either used the

output from biogeochemical models, or tried to create pCO$_2$ fields from mapped proxy data and observational data using extrapolation approaches. Seasonal mapping of pCO$_2$ is particularly challenging for the Baltic Sea due to its high regional and temporal variability, a salinity gradient affecting, e.g., CO$_2$-equilibra, and a large seasonal amplitude caused by high net productivity in spring summer and entrainment of waters enriched in remineralization products due to mixed layer deepening in fall and winter (Schneider and Müller, 2018).

Climatologies of pCO$_2$ on a global or ocean-wide scale are an important tool for the quantification of the oceanic CO$_2$ sink in the framework of e.g. the Global Carbon Budget (Landschützer et al., 2013; Friedlingstein et al., 2022). Tailored regional analysis can help to gain insight into changes in the source-sink behaviour of distinct regions, as recently demonstrated for the northern European shelf, including the Baltic Sea (Becker et al., 2021).

A robust climatology and trend for the Baltic Sea has, apart from refining the estimate of the net CO$_2$ flux in relation to the Global Carbon Budget, several implications. As the entire Baltic Sea area belongs to the territorial waters or exclusive economic zones (EEZ) of one of the pan-Baltic nations, the air-sea CO$_2$ fluxes might be of importance for current and future carbon management and accounting schemes in the framework of national emission reduction targets (Luisetti et al., 2020). A pCO$_2$ climatology could also serve as a baseline for potential negative emissions applications, including blue carbon or coastal alkalinity enhancement (GESAMP, 2019). Knowledge of monthly pCO$_2$ fields and their variability might also help to identify and quantify the impact of perturbations and extreme events, e.g. heat waves (Humborg et al., 2019).

In this work, we build a foundation for such applications. We first present a novel extrapolation approach, followed by construction of a Baltic Sea pCO$_2$ climatology. The extrapolation approach is then evaluated and put into context with existing mapping methods. Notable features of the seasonal pCO$_2$ climatology are discussed and special attention given to the regional long-term pCO$_2$ trend before we conclude our work.

2 Methods

2.1 Extrapolation approach

For mapping from scarce observational data to spatially-filled maps of the Baltic Sea, we use an ensemble of truncated EOF reconstructions. For a more detailed description than the brief summary below, please consult appendix A.

Empirical orthogonal function (EOF) decomposition or singular value decomposition (SVD) have been used widely in atmospheric and ocean science (e.g., Lorenz, 1956; Weare et al., 1976; Weare and Newell, 1977; Hannachi et al., 2007). They can be used to efficiently reduce dimensionality of the original dataset (Lorenz, 1956; Davis, 1976; Preisendorfer, 1988; Monahan et al., 2009; Jolliffe and Cadima, 2016). Here, we use the EOF decomposition of a model dataset $\mathbf{X}$ of pCO$_2$ in the Baltic Sea to obtain spatial EOF patterns e_i of pCO$_2$ variability.

In a second step, observational pCO$_2$ data $\mathbf{Y}$ are used in conjunction with these spatial patterns of variability in a truncated EOF reconstruction to constrain the EOF spatial patterns' amplitudes (Kaplan et al., 2000; Preisendorfer, 1988) and thus, to extrapolate from scarce observational data to the full domain (section A3). This step represents an optimization of a cost function Q (Eq. A19), which in our case takes also the observational data uncertainty into account to avoid overfitting (section A4).

For a given EOF reconstruction with l spatial modes, we thus obtain both an extrapolated field as well as an estimate of the mapping uncertainty $\sigma_{\mathbf{P}}$, representing the uncertainty on the extrapolation with the given data constraints. In addition, we derive a representational error estimate $\sigma_{\mathbf{P}'}$ for the variance not resolved by the given EOF reconstruction due to truncation and use of just l modes (section A4).

However, the choice of how many EOF modes to use for a given truncated EOF reconstruction, or at which level to truncate, is an arbitrary choice, often inspired by a certain threshold of total variance explained (e.g., Kaplan et al., 2000).

In a third step, we therefore use an ensemble approach to circumvent this problem: Instead of a single EOF reconstruction with a fixed number of modes l, we use a series of EOF reconstructions from just one mode up to a maximum number of $l_{\max}$ modes (section A5). This series is then combined by a weighted ensemble at each location with the individual EOF reconstruction's mapping uncertainties as weights (Eqs. A25, A26; section A6).

Note that the weights are spatially resolved and depend on the available data constraints, i.e., the ensemble weights provide for locality, which includes adaptation of the mapping's spatial scales to the data constraint density, thus providing for a more robust extrapolation and more realistic uncertainty estimates than with a fixed number l of EOF modes.

We thus obtain an ensemble mean $p\mathrm{CO}_2$ value x_{reconstr}, the average number of modes $\bar{l}$ used in the ensemble of reconstructions at a given location, and an uncertainty estimate $\sigma_{\mathrm{reconstr}}$ (Eq. A28), which consists of the sample variance about the ensemble mean value, the ensemble-averaged mapping uncertainty $\sigma_{\mathbf{P}}$ (from each truncated EOF reconstruction with l from $1 \ldots l_{\max}$), and the ensemble-averaged representational error $\sigma_{\mathbf{P}'}$ (from each EOF reconstruction) (section A6). All these quantities are obtained without gaps on the full spatial domain of the original model dataset $\mathbf{X}$.

Finally, due to high temporal dynamics of our Baltic Sea environment, we use an expansion of the EOF reconstruction approach to not only reconstruct the data value, but both data value and a (short-term) linear trend in order to temporally collate (temporally extended) observations into a time-coherent, synoptic picture (section A7; Elken et al., 2019).

2.2 Baltic Sea $p\mathrm{CO}_2$ climatology

Given limitations of modelled data, we aimed to produce an observation-based $p\mathrm{CO}_2$ climatology. For this, we used (a) the above extrapolation approach with spatial patterns based on ecosystem model data as well as (b) observations of surface $p\mathrm{CO}_2$ from SOCAT to produce a monthly climatology of $p\mathrm{CO}_2$ as well as of the linear, short-term $p\mathrm{CO}_2$ trend to temporally collate $p\mathrm{CO}_2$ observations (section A7) within a month (see Fig. 1 for a visualization of the approach).

2.2.1 Spatial patterns of variability

Spatial patterns of variability e_i for our extrapolation approach are based on model data from a Baltic Sea setup of the Ecological ReGional Ocean Model (ERGOM version 1.2). This version of ERGOM includes a simple carbon cycle as described in Kuznetsov and Neumann (2013) with amendments to allow for non-Redfield stoichiometry as outlined in Neumann et al. (2022). In principle, any carbon-containing biogeochemical ocean model of choice can be used as basis for the patterns of variability e_i. Nonetheless, a better carbon representation in the model likely provides better-suited e_i patterns of variability.
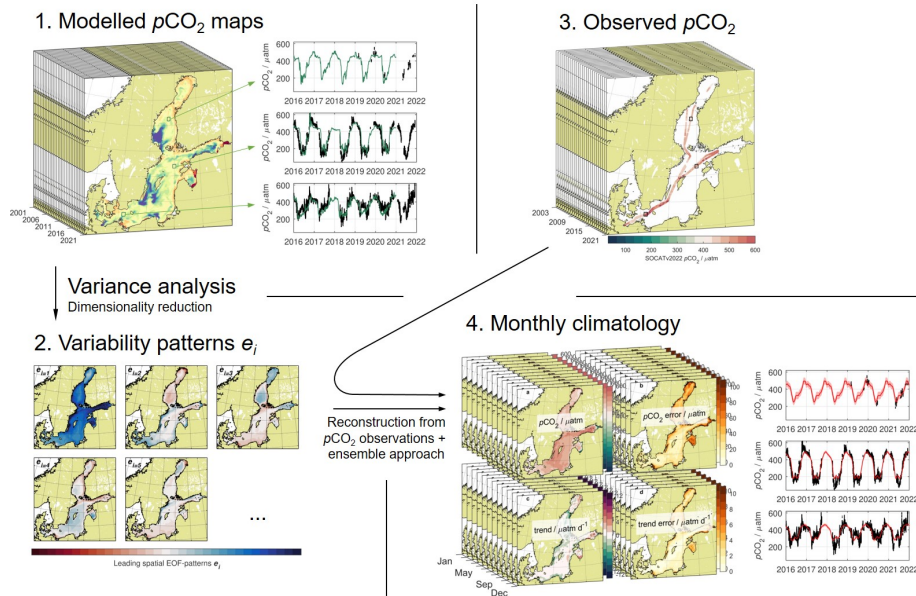
Figure 1. Approach to build a regional pCO_2 climatology of the Baltic Sea. (1) pCO_2 data from an ecosystem model are mathematically analyzed for dominant patterns of variability e_i in a truncated EOF analysis. (2) Patterns of variability and (3) pCO_2 observations of a given month are used to reconstruct Baltic Sea pCO_2 distributions $\overline{\mathcal{X}}$, which are combined through an ensemble approach into (4) a monthly climatology of surface pCO_2 incl. pCO_2 error estimate and (short-term) pCO_2 trend incl. pCO_2 trend error estimate. For illustration, time series are given for three sample locations for model pCO_2 (green), pCO_2 observations (black), and climatological pCO_2 (red).

The model data variability characteristics are illustrated in the appendix (Fig. A1). Less than 1 % of locations show a temporal decorrelation scale ≤ 7 days, so that we chose a weekly aggregation of the model data for variability pattern extraction. For the climatology itself, we chose a more typical monthly resolution.

ERGOM has been shown to adequately mirror observations of the large scale nitrate, phosphate, oxygen, and carbon dis-
95 tribution (Neumann et al., 2022; Eilola et al., 2011; Neumann et al., 2015). However, shortcomings still exist in the exact magnitude and timing of phytoplankton carbon uptake and release throughout the seasons (Neumann et al., 2022; Fig. 4).

From an ERGOM version 1.2 model run from 1948 – 2020 we used the last 20 years of modelled surface pCO_2 from 2001 to 2020 averaged into 1044 weekly means. The model run has a horizontal resolution of 3 nautical miles, which yields a dataset **X** with 12010 grid points m for the Baltic Sea area South of the Skaggerak (i.e., HELCOM subbasins 2 to 17, HELCOM
100 Secretariat, 2017) and 1044 time steps n.

From these model data **X**, patterns of variability e_i were extracted by empirical orthogonal function (EOF) analysis (see appendix A for details). The DINEOF analysis of our model data retained 224 EOF modes with a minimal cross-validation error of 22.6 μatm to the model data and a total explained variance of 98.6 %. The spatial patterns e_i have the same 3 n.m. resolution as the model data.
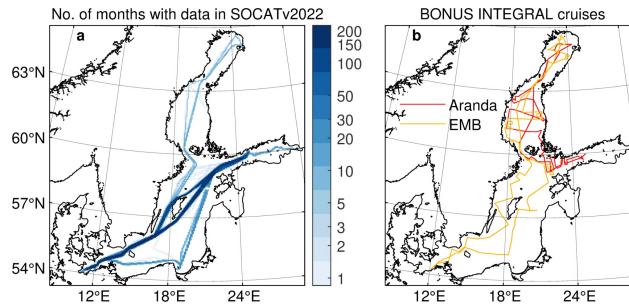
Figure 2. (a) Map of the Baltic Sea with number of individual months with pCO_2 observations available in SOCATv2022 between June 2003 and Dec. 2021 (max. 223 months). (b) Cruise tracks of BONUS INTEGRAL cruises on RV *Aranda* in Feb./Mar. 2019 and RV *Elisabeth Mann Borgese* in May/June 2019.

2.2.2 Surface pCO_2 Observations

Surface pCO_2 measurements in the Baltic Sea were obtained from SOCAT version 2022 (Pfeil et al., 2013; Bakker et al., 2016, https://www.socat.info), which collects surface pCO_2 data from underway observations of ships of opportunity (SOOPs) or research vessels. All observations are based on CO_2 measurements in air equilibrated with sea surface waters (Körtzinger et al., 1996; Pierrot et al., 2009) with a typical accuracy of $2-5$ μatm, in some cases ≤ 10 μatm, which is indicated by the respective quality flag A – E (Pierrot et al., 2009; Bakker et al., 2016).

Here, Baltic Sea pCO_2 data for the period June 2003 to Dec. 2021 were used. They were either from the ICOS-DE SOOP *Finnpartner/Finnmaid* line (Schneider et al., 2006; Gülzow et al., 2011) between Lübeck-Travemünde and Helsinki, which covers the Southern and Central Baltic Sea, or the ICOS-SE SOOP *Tavastland* line between Lübeck-Travemünde and Oulu/ Kemi, which additionally covers the Northern basins starting from 2019 (Fig. 2a). Additional surface pCO_2 data originated from RV *Aranda* cruise ARA04/2019 in Feb./Mar. 2019 and RV *Elisabeth Mann Borgese* cruise EMB214 (Rehder et al., 2021) in May/June 2019 (Fig. 2b), which were performed as part of the BONUS INTEGRAL project. Data processing and quality control followed the SOCAT guidelines. In total, data coverage in the Southern and Central Baltic Sea is high, with locally up to 189 out of 223 months covered (i.e., June 2003 to Dec. 2021). Data in the Northern Baltic Sea, however, is only available since Feb. 2019 with observations during a total of 15 out of 35 months.

2.2.3 Monthly climatology construction

For every month t of the 189 months with observations, the observations were centred temporally on the 15th of each month as $t_\circ$ (see section A7) so that the extrapolation approach provides a field $\overline{\mathcal{X}}$ with the spatial distribution of

– the reconstructed pCO_2 ($x_{t,\mathrm{reconstr}}$, Eq. A27) at $t_\circ$,

– the pCO_2 error estimate ($\sigma_{t,\mathrm{reconstr}}$, Eq. A28) at $t_\circ$,

– the (short-term) pCO_2 trend at $t_\circ$,
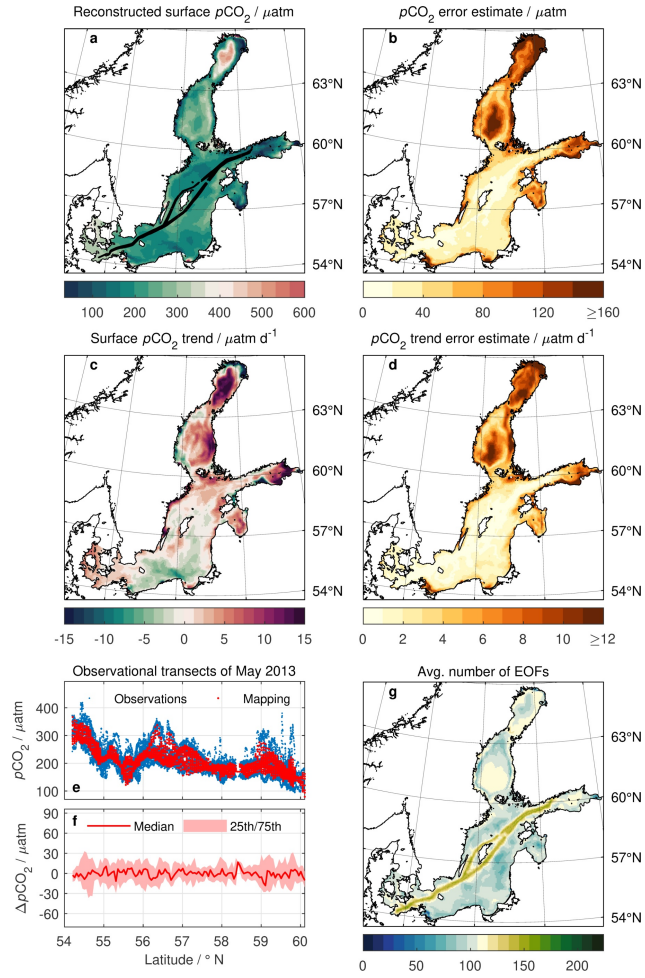
Figure 3. Monthly fields $\overline{\mathcal{X}}$ of surface pCO_2 reconstruction for May 2013: (a) Reconstructed pCO_2 $x_{t,\mathrm{reconstr}}$ with observation locations given as black dots. (b) pCO_2 error estimate $\sigma_{t,\mathrm{reconstr}}$ with small values nearby observations. (c) pCO_2 trend and (d) its error estimate. (e) Observed (blue) and reconstructed pCO_2 (red) against latitude as well as (f) their difference as median (solid line) and interquartile range (pale shading). (g) Average number of patterns $\bar{l}$ of the reconstruction: Above average $\bar{l}$ indicates use of high-order, smaller scale patterns e_i, notably nearby data constraints from observations, whereas below average $\bar{l}$ indicates areas where low-order, larger scale patterns e_i dominate in the reconstruction ensemble (see Eq. A26). Compare Fig. A2 for a reconstruction without temporal trend (section A7).

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– an error estimate on the pCO_2 trend at $t_\circ$, and

– the average number of patterns e_i used in the reconstruction ($\bar{l}$, Eq. A25)

for each of month with observations (e.g., Fig. 3 for $\overline{\mathcal{X}}$'s of May 2013 as illustration).

The construction of a monthly pCO_2 climatology for the entire Baltic Sea has its bottleneck in the temporal coverage of the Northern basins, i.e., the Bothnian Sea, the Quark, and the Bothnian Bay. While the central and Southern Baltic Sea has ca. 85 % of all months since June 2003 covered, observations in the Northern basins start only in Feb. 2019 with 43 % monthly coverage until the end of 2021. While the extrapolation approach provides fully filled maps of pCO_2, including the Northern basins, also for months pre-Feb. 2019, they are associated with larger uncertainties, i.e., limited explanatory power in the Northern basins (e.g., Fig. 3b). To not create a wrong impression of seasonality or interannual variability, especially if the mapping uncertainty fields $\sigma_{t,\mathrm{reconstr}}$ are not respected by a casual user, we chose to provide a mean seasonal climatology $\mathbf{Y}$. Here, the weighting of the climatology (Eq. 1; see below) ensures the preference of reconstructions with proper observation constraints (i.e., Feb. 2019 and onwards for the Northern basins) over reconstructions without (i.e., pre-Feb. 2019).

For a given location m, χ_m denotes the (reconstructed) time series of $\overline{\mathcal{X}}$ (with size 1×189) and y_m the time series of the mean monthly climatology $\mathbf{Y}$ (with size 1×12), respectively. The monthly means y_m were then obtained by:

$$w_m \cdot \chi = w_t \cdot \left(\mathbf{O}_m^{\mathbf{T}} y_m^{\mathbf{T}} + g_m \cdot (t - t_{\mathrm{ref}}) \right) \text{ with} \tag{1}$$

$$w_m = 1 / \sigma_{m,\mathrm{reconstr}}^2 \; , \tag{2}$$

where w_m is the time series of inverse variance weights (Eq. 2) with size 1×189 at the given location m, $\mathbf{O}_m$ a time series operator or matrix of size 12×189 that selects the monthly mean y_m corresponding to the month of χ_m, $t - t_{\mathrm{ref}}$ the time difference (in decimal years) between each of the 189 monthly $\overline{\mathcal{X}}$ and a reference time, t_{ref}, and g_m an extra degree of freedom to allow for a linear long-term trend in $\overline{\mathcal{X}}$ for each location m (e.g., surface pCO_2). As reference time, the middle of 2013 was chosen, which closely corresponds to the mean date of all observations.

Eq. 1 represents a system of 189 linear equations with 13 degrees of freedom to calculate 12 weighted mean values y_m and a long-term trend g_m. Through the inverse variance weights (Eq. 2), monthly maps χ_m with better constrained data, i.e., smaller variance of reconstruction $\sigma_{m,\mathrm{reconstr}}^2$ at the given location m (and for the given month), obtain preference in the weighted mean (Eq. 1).

When done for each point m, one obtains the mean seasonal climatology $\mathbf{Y}$ (with size $m \times 12$), centered on 2013, as well as a map of its mean linear (long-term) trend $\mathbf{G}$ (with size $m \times 1$) for every of the five fields $\overline{\mathcal{X}}$ discussed.

2.2.4 Dataset description

The dataset (Bittig et al., 2023) consists of two plain-text files. One contains the mean seasonal climatology $\mathbf{Y}$ and the other the mean linear (long-term) trend $\mathbf{G}$. Based on the 3 nautical miles resolution of the original model data, both feature 12010 grid points m for HELCOM subbasins 2 to 17. For months January through December, the climatology file gives pCO_2 in μatm, pCO_2 error estimate (1σ) in μatm, (short-term) pCO_2 trend for the 15th of each month in μatm d^{-1}, (short-term) pCO_2 trend error estimate (1σ) in μatm d^{-1}, and the average number of patterns ($\bar{l}$) (see Fig. A3, A4). The long-term trend file gives both the long-term linear trend $\mathbf{G}$ in μatm yr^{-1} (Fig. 7) and its error estimate (1σ) in μatm yr^{-1}.

 3 Results

3.1 Extrapolation approach

The mapping approach gives fully filled fields on the entire spatial domain from scattered observational data. The mapped pCO_2 is in a similar range and frequency distribution as observations with improvements in terms of distribution and correlation over the original model pCO_2 (Fig. 4a). The mapped fields are smooth and without spatial gaps or discontinuities. The pCO_2 error

165 estimate is reduced in spatial vicinity to observations. In contrast, pCO_2 error is markedly increased both near shore as well as in subbasins not covered by observations, e.g. the Northern basins or the Gulf of Riga for a SOOP *Finnmaid*-based reconstruction (e.g., Fig. 3b). Still, pCO_2 values remain within reasonable margins even in those areas (e.g., Fig. 3a). We can not observe a tendency of the mapping approach to give extreme values or outliers in absence of observations (compare Fig. 4a). Rather, with little or no data constraints, variability pattern e_i amplitudes in the ensemble tend towards zero, i.e., towards zero deviation,

170 which is equivalent to the spatially-resolved temporal mean pCO_2 of the model (Appendix A).

Addition of a linear temporal trend to collate observations to a common time $t_\circ$ helps to reduce the mismatch between temporally-spread observations and a full-domain mapping of a dynamic coastal system (compare, e.g., Fig. 3e, f and Fig. A2c, d, respectively).

However, for about half the grid points of the 189 monthly mappings, the magnitude of the short-term temporal pCO_2 trend

175 (e.g., Fig. 3c) at a given location m is insignificant, i.e., within its trend error estimate (e.g., Fig. 3d). At the same time, a considerable portion of the significant pCO_2 trends are found at grid points m in the direct footprint of observations where the trend error estimates are small in the first place. This demonstrates that a monthly temporal resolution is sufficient for construction of a Baltic Sea pCO_2 climatology with our approach.

3.2 Quality of interpolation and extrapolation

180 To assess the quality of obtained fields, we consider (a) the mapped result against the original observations, and (b) a comparison of mappings from concurrent subsets of observations.

For the first aspect, we consider the residual pCO_2 against SOCAT observations for all 189 monthly mapped fields from the climatology construction (e.g., Fig. 3e, f). We use typical metrics for interpolation methods (correlation, bias, standard deviation). As the monthly fields $\overline{\mathcal{X}}$ were constructed from those observations, this assesses primarily to which degree the data

185 constraints were taken into account for the mapping, e.g., the balance between point-to-point reproduction and smoothing with the given patterns of variability e_i.

The comparison shows highly correlated pCO_2 data ($\mathrm{R}^2 = 0.95$), a similar pCO_2 distribution (Fig. 4a), and an unbiased mapping with a standard deviation of 26 μatm (Fig. 4b). This, includes both misfits of the mapped fields as well as variations within observations of a given grid point location (compare spread between observations and mapping in Fig. 3e). The error

190 estimate is of a similar magnitude (Fig. 4c) and well co-located, i.e., residuals are within $1\times$ the error estimate in 68 % of cases (Fig. 4d).
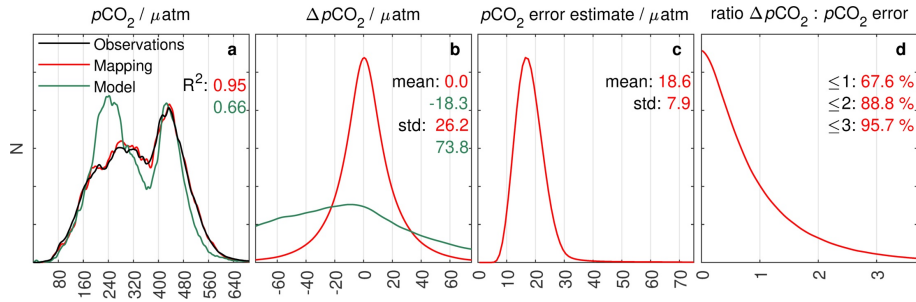
Figure 4. Histograms for: (a) pCO_2 observations (black) as described in section 2.2.2, pCO_2 reconstructed at the observation times and locations from the 189 monthly mappings (red), and model pCO_2 extracted at the observation times and locations (green). Reconstructed and observed pCO_2 data are highly correlated (R^2) and they show a similar distribution. Correlation between modelled and observed pCO_2 is weaker and their distributions show noticeable differences. (b) The pCO_2 difference between reconstructed (red) or modelled (green) pCO_2 and observed pCO_2. There is no bias in the reconstruction, while differences between model and observations show a much wider range than the reconstructed pCO_2. (c) The pCO_2 error estimate $\sigma_{\mathrm{reconstr}}$ of the reconstruction at the observation times and locations. (d) The ratio between pCO_2 difference and pCO_2 error estimate, where a ratio ≤ 1 means that the observed pCO_2 is within $1 \times \sigma_{\mathrm{reconstr}}$ of the mapped pCO_2.

The second aspect, how data constraints in one area transfer to accurate predictions in another part of the domain, is more difficult to assess objectively. It requires the observational data to be split into a subset that is used for mapping and a subset that is deemed as independent and used for evaluation. How this subsetting is done, however, directly influences the outcome of the evaluation. I.e., while such evaluations may seem instructive and generalizable, they are highly dependable on design and thus carry some degree of arbitrary.

To illustrate, we consider a series of monthly mappings for May 2019, the month with highest density of observations in our 189 monthly mappings. We use chess board-like grids with alternating white and black boxes for subsetting, where observations in white boxes are used for mapping and observations in black boxes used for evaluation. Grid box sizes are varied from 1°x1°, 2°x2° to 3°x3° (Fig. 5a, e, i for example grids). To check for dependence on specific data distribution, the 1°x1°, 2°x2° and 3°x3° subsetting grids were shifted spatially in latitude and longitude so that every grid size had 8 different realizations each with different sets of data in the mapping and evaluation subsets, respectively (Fig. 5).

For 1°x1° subsetting, the 8 realizations show a relatively coherent picture: Differences ΔpCO_2 between mapped and observed pCO_2 (Fig. 5b) are slightly larger (by $5-12$ μatm) than for interpolated data (Fig. 4b) and mostly unbiased. pCO_2 error estimates are elevated (Fig. 5c vs. Fig. 4c) while the ratio of differences and error estimate, i.e., the colocation of bias and error estimate, shows as similar distribution for both extrapolation (Fig. 5d) and interpolation (Fig. 4d). With increasing spatial scales of the 2°x2° and 3°x3° subsetting, pCO_2 differences as well error estimates get larger as would be expected (Fig. 5f, j and g, k). Encouragingly, however, the ratio of differences and error estimate preserve a similar shape (Fig. 5h, l), i.e., the mapping approach seems to provide suitable mapping error estimates.
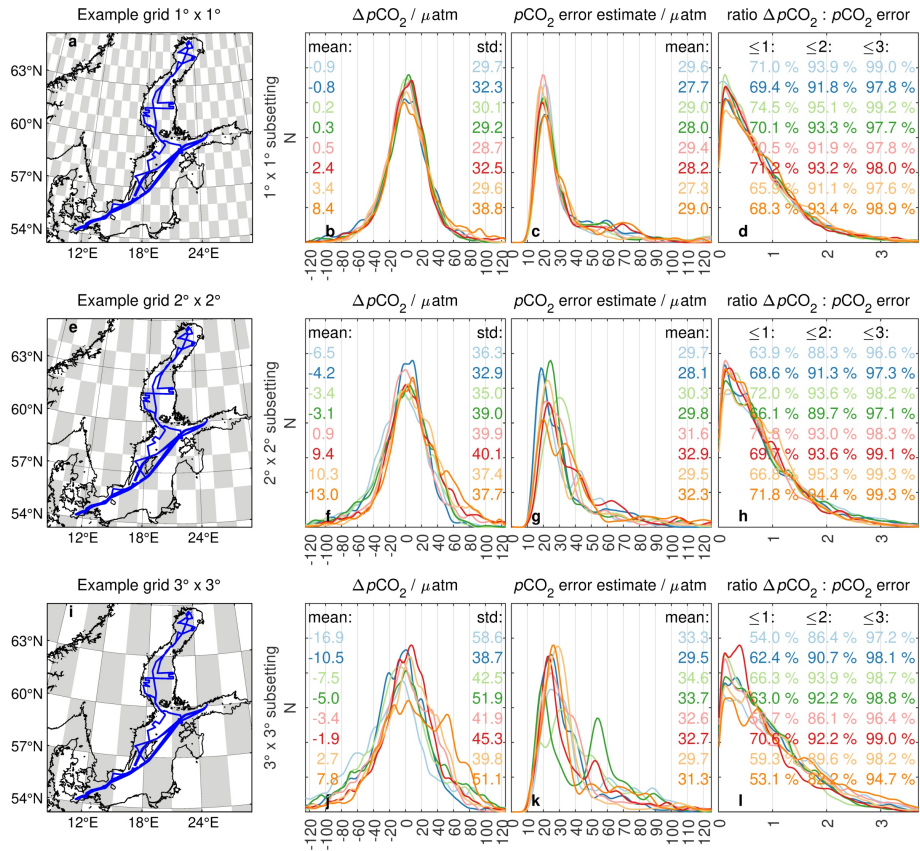
Figure 5. Subsetting evaluations for May 2019 observations using 1°x1° subsets (top row; a-d), 2°x2° subsets (middle row; e-h), and 3°x3° subsets (bottom row; i-l), respectively, with maps (a, e, i) illustrating one example subsetting grid where observations (blue) in white boxes are used for pCO_2 reconstruction and observations in grey boxes for evaluation. Histograms are for: (b, f, j) The pCO_2 difference between reconstructed and observed pCO_2 within the evaluation boxes. (c, g, k) The pCO_2 error estimate $\sigma_{\mathrm{reconstr}}$ of the reconstruction at the observation times and locations within the evaluation boxes. (d, h, l) The ratio between pCO_2 difference and pCO_2 error estimate within the evaluation boxes, where a ratio ≤ 1 means that the observed pCO_2 is within $1 \times \sigma_{\mathrm{reconstr}}$ of the mapped pCO_2. The colours represent 8 different 1°x1°, 2°x2°, and 3°x3° subsetting grids only offset spatially in latitude/longitude.

210   More concerning, however, are increasing differences between the 8 realizations with increasing spatial scales. Especially for the 3°x3° subsetting, some realizations show a pCO_2 bias, which additionally can be different between realizations (blue vs. orange realizations, Fig. 5j), as well as noticeable differences in pCO_2 error estimate and thus mapped pCO_2 (e.g., green realization, Fig. 5k). This illustrates a strong dependence on the specific choice of subsetting, i.e., which data are included in mapping and which data are excluded for validation.

215   We conclude that with a given choice of subsetting, one implicitly chooses what statistical values one wants to get out. While our evaluation could be described as being well-designed, it turns out to be starting point-dependent. If a month with less data coverage were chosen, differences between realizations (i.e., which data end up in the training or validation subset) would
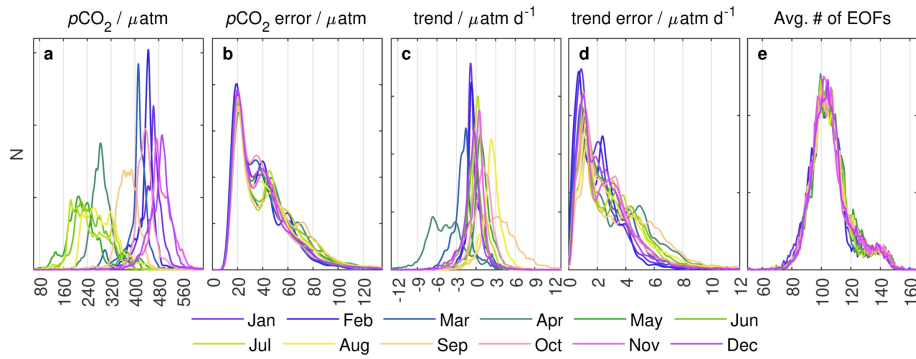
Figure 6. Smoothed histograms for the five output fields of the climatology $\mathbf{Y}$: (a) reconstructed pCO_2 $x_{t,\mathrm{reconstr}}$, (b) pCO_2 error estimate $\sigma_{t,\mathrm{reconstr}}$, (c) pCO_2 short-term trend, (d) error estimate on the pCO_2 short-term trend, and (e) average number of patterns $\bar{l}$ used in the reconstruction. The colour code indicates the respective month. pCO_2 follows a typical seasonal cycle, while the pCO_2 error estimate and number of patterns show no apparent seasonal variations. pCO_2 trends show higher magnitudes during spring (Mar./Apr.) and late summer (Aug./Sep.), which is mirrored by enhanced pCO_2 trend error estimates in these months.

be even larger. Therefore, based on the above illustration, any subsetting-based evaluation needs to be taken with a sufficient amount of caution, as the subsetting design will imprint itself on the outcome.

3.3 Baltic Sea pCO_2 climatology

3.3.1 pCO_2 distribution

The mean seasonal pCO_2 distribution x_{reconstr} matches previously published seasonal cycles of surface pCO_2 in the Western and central Baltic Sea (Schneider and Müller, 2018): A strong spring bloom pCO_2 drawdown occurs between March and May to a low around 200 μatm in May, some slight increase in June and a second summer bloom low in July, followed by relaxation towards atmospheric levels in September/October and supersaturated levels during late autumn and winter, peaking around 500 μatm in December (Fig. 6a; Fig. A3 and A4, 1st column).

Regionally, the Western basins lead the mean seasonal cycle, while the central Gotland basin and the Gulf of Finland trail behind. The productive season is even shorter in the Northern basins, with the major pCO_2 drawdown in the Bothnian Sea occurring in June (Fig. A3 and A4, 1st column). Similarly, the seasonal amplitude is less pronounced in the Western or Northern basins than in the Gotland basin, and is most intense in the Gulf of Finland. For the Northern basins, this is the first fully seasonal climatology from pCO_2 observations.

The pCO_2 error estimate $\sigma_{\mathrm{reconstr}}$ shows a minimum of 12 μatm. Close to observations, the pCO_2 error estimate of the mean seasonal climatology is on the order of 20 μatm and as such close to the value of the individual mappings (compare Fig. 6b vs. Fig. 4c). Further away, $\sigma_{\mathrm{reconstr}}$ increases up to a level around 90 μatm (95th percentile), with a spatial preference for high $\sigma_{\mathrm{reconstr}}$ in the Northern basins as well as in the Gulf of Riga, Oder bight, and other sheltered, near-shore areas (Fig. A3 and A4, 2nd column).

3.3.2 pCO_2 short-term trends

In general, the short-term pCO_2 trends follow the mean seasonal pCO_2 cycle with on average negative trends, i.e., decreasing pCO_2, during winter and spring. Positive trends prevail during late summer and autumn (Fig. 6c) with strongest trend magnitudes occurring in the Northern Baltic Proper and the Gulf of Finland (Fig. A3 and A4, 3rd column).

However in 8 out of 12 months, the majority of estimated trends are insignificant, i.e., more than 70 % are smaller than their error estimate, indicating that inclusion of a short-term trend in the mapping may not be required for these months. Only in March and April as well as in August and September, the majority of pCO_2 trends is significant (despite at the same time elevated pCO_2 trend error estimate in some areas, see Fig. 6d). I.e., significant short-term pCO_2 trend magnitudes fall together with the strong springtime pCO_2 drawdown as well as with autumnal mixed layer deepening and entrainment of high-pCO_2 waters (Fig. 6; more in Jacobs et al., 2021).

Like for the pCO_2 distribution, trend error estimates are increased in the Northern basins as well as for the Gulf of Riga, Oder bight, and other sheltered, near-shore areas (Fig. A3 and A4, 4th column).

3.3.3 Number of patterns or mapping scales

The average number of patterns $\bar{l}$ per month can be seen as a qualitative indicator to show preference for reconstructions with larger or smaller spatial scales, respectively, in the weighted mean (Eq. A25) of the reconstruction.

For the climatology $\mathbf{Y}$, $\bar{l}$ shows a maximum around 105 patterns (Fig. 6e). This level is at about 45 % of the maximum number of patterns, i.e., indicating only a slight preference for reconstructions with larger than average scales in the weighted mean. However, a notable fraction with higher number of patterns $\bar{l}$ with peak around 140 patterns exist (Fig. 6e). These are located in vicinity to observations, where preference in the weighted mean is on reconstructions with stronger small scale features (see, e.g., Fig. 3g).

There is no seasonal imprint to the average number of patterns $\bar{l}$, which is in contrast to the pCO_2 as well as the pCO_2 short-term trend distribution (Fig. 6).

3.4 Long-term pCO_2 trend

The mean climatology $\mathbf{Y}$ is constructed from the 189 monthly mappings $\overline{\mathcal{X}}$ and a linear long-term trend $\mathbf{G}$ (see Eq. 1 and section 2.2.3). For pCO_2, the analysis shows a significant long-term pCO_2 increase of $+1.4\pm0.5$ μatm yr^{-1} (1 σ) in the Southern Baltic Sea from the Great Belt to the Bornholm basin and Southern parts of the Gotland basin (Fig. 7). A similar increase ($+1.5\pm0.7$ μatm yr^{-1}) is obtained in selected regions of the Northern Baltic Proper, the Åland Sea and the Gulf of Finland. A positive trend in pCO_2 is also visible in coastal areas along the Finnish coast in the Northern basins as well as in the Gulf of Riga. However, multi-year observations in those areas are unavailable to support a long-term pCO_2 trend (see section 2.2.2; Fig. 2). In all other areas, the data available do not indicate a significant long-term trend, i.e., one that is outside the 68.3 % (1 σ) confidence bound. This includes in particular the Western and Eastern Gotland basin, but also the Northern
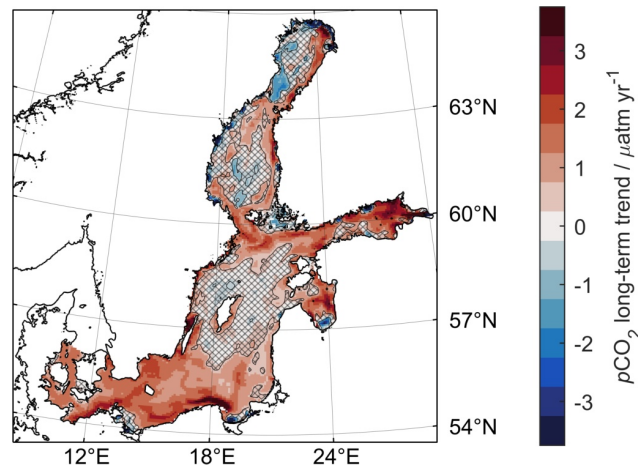
Figure 7. Long-term trend **G** of surface pCO_2 from the monthly mappings and the climatology construction (Eq. 1). Areas where the long-term trend is not significant are cross-hatched. In the Southern Baltic Sea, a significant increase of +1.4 μatm yr^{-1} is obtained from the observations. Selected parts of the Northern Baltic Proper, the Åland Sea and the Gulf of Finland give a similar increase of +1.5 μatm yr^{-1}, while the Western and Eastern Gotland basin show no significant long-term trend.

basins (Fig. 7), where the observational time series is likely too short to allow for the detection of a significant long-term trend (Fig. 2).

4 Discussion

4.1 Extrapolation approach

The extrapolation approach uses an EOF analysis of the data covariance **Q** as foundation. When working with an EOF reconstruction, one needs to bear in mind the purely mathematical nature of the EOF modes' e_i construction: They are built by (1) maximizing the (partial) variance they explain and by (2) being orthogonal to all previous EOF modes (Preisendorfer, 1988; Monahan et al., 2009; Dommenget, 2015). They may therefore indicate some causal connection within the original data **X**, which requires confirmation by other means. They may, however, just as well group some portion of (partial) variance in one part of the domain with some portion of (partial) variance in another part of the domain just to mathematically maximize the amount of (partial) variance of the given EOF mode e_i. This can give rise to apparent EOF mode "teleconnections", where one part of the data or spatial domain are seemingly tightly coupled with another part of the data, e.g., for the second EOF mode $e_{i=2}$, which has always a dipole pattern. Often, there is a temptation to attribute such couplings or "teleconnections" to a driving mechanism. However, given its origin, patterns of EOF modes should be interpreted with great caution (and only with ancillary, supporting data) and best seen of mathematical rather than of mechanistic nature (Monahan et al., 2009; Dommenget, 2015). We therefore did not try to assign physical mechanisms or drivers to specific EOF patterns e_i in our work.

The use of EOF modes as basis for extrapolation ensures that the extrapolated map covers the full spatial domain, that it is continuous/gap-free, and that it is discontinuity-free.

A key aspect of truncated EOF reconstructions is the number l of significant modes included. Our cross-validation approach provided a relatively large number of $l_{\max} = 224$ modes. The relatively large number of modes is a prerequisite for a small representational error $\mathbf{P}'$, i.e., for the covariance not resolved by the collection of truncated EOF modes, which gives a lower bound on the uncertainty of the mapping $\sigma_{\mathrm{reconstr}}$ (Eq. A28). In our case, the average $\sigma_{\mathbf{P}'}$ when using all 224 patterns e_i amounts to 14.7 μatm. If only the first 50 patterns e_i were included, the average representational error would be as high as 29.1 μatm.

A reconstruction with a small number of modes provides for a more uniform, large-scale homogeneous field, where gaps in the data are filled by the large-scale picture. However, such reconstructions may lack the flexibility to reproduce real features of the observations, e.g., through too strong smoothing. Conversely, a large number of modes provides for a fine, small-scale field with high flexibility. However, features in some areas without nearby observations may be badly constrained with the risk of "ghost" signals.

By using an ensemble of reconstructions that cover the entire range of $1 \ldots l_{\mathbf{max}}$ modes and by using the mapping variance $\sigma_{\mathbf{P}}^2$ as weights (Eqs. A25, A26), we find an optimal trade-off in our mapping approach, where both aspects are balanced. This way, the scales used in the mapping are adjusted spatially according to the distribution of observations as constraints.

The cost function of the mapping approach minimizes the residual between observations and mapped data (Eq. A19). This way, a synoptic $p\mathrm{CO}_2$ mapping is obtained. If observations, however, are temporally extended compared to the system's temporal dynamics, the $p\mathrm{CO}_2$ mapping can be distorted and not represent a synoptic picture, depending on the spatial and temporal pattern by which observations are obtained (Elken et al., 2019).

The introduction of a temporal trend at each location (section A7) as additional degree of freedom reduces such distortion caused by sampling. It both improves the fit to the data (compare Fig. A2c, d vs. Fig. 3e, f) and provides extra information:

- For a given mapping, a strong or weak trend indicates where temporal dynamics are high or low and informs on where frequency of observations should be enhanced or not, respectively.

- For a time series of mappings, information on both the value and trend allows for a more accurate interpolation by cubic Hermite spline (Appendix B) compared to a standard, linear interpolation of the values alone (e.g., Fig. 8).

For our mapping of surface $p\mathrm{CO}_2$ in monthly intervals, we conclude that the inclusion of a temporal trend in the mapping is required, particularly for spring and autumn. For months without strong trends, we do not see adverse effects in the mapped $p\mathrm{CO}_2$ compared to an extrapolation without inclusion of a temporal trend.

The dynamics of the $p\mathrm{CO}_2$ field are prescribed by the model data covariance matrix $\mathbf{Q}$ (Fig. A1a). The closer the model and real-world variability match, the easier it is for the mapping to reflect reality and to provide a most realistic picture. Nonetheless, also for a model dataset $\mathbf{X}$ that may lack in some real-world features or their magnitude, the observational constraints provide for an improvement in the mapped field compared to the original model (Fig. 4).
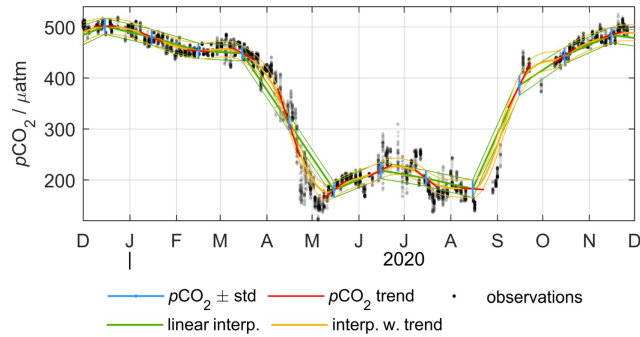
Figure 8. Difference between monthly point-by-point interpolation (green) or interpolation with a trend (orange) in a dynamic coastal system. Example data are from the Northern Baltic Proper (ca. 021° 00' E, 58° 45' N) with pCO_2 observations $\mathbf{X}$ shown in black. They are the basis for monthly mapped fields $\overline{\mathcal{X}}$ of surface pCO_2 (blue) as well as for a linear (short-term) pCO_2 trend (red). Compared to a linear interpolation between monthly pCO_2 values (green), interpolation including the trend information (orange) gives a better reproduction of the observed dynamics particularly in spring and autumn. A cubic Hermite spline was used for the calculation (Appendix B).

The mapping error estimates are elevated where observations are scarce or dynamics are high to start with. For our pCO_2 mapping, the model covariance $\mathbf{Q}$ is the origin for a pronounced coast-basin difference in the pCO_2 variance caused both by physical and biological drivers in the model. This prescribed data covariance distribution is retained in the mapping error estimates $\sigma_{\mathrm{reconstr}}$. E.g., they are enlarged in dynamic river plumes, in the sheltered, shallow Gulf of Riga, or in other near-shore areas, unless there are observations to constrain dynamics and thus reduce $\sigma_{\mathrm{reconstr}}$. In regions with few observations, $\sigma_{\mathrm{reconstr}}$ approaches the prescribed data variance from $\mathbf{Q}$ (Fig. A1a).

We do not observe a seasonality in the number of patterns $\bar{l}$ of the mapping (Fig. 6e). At the same time, the pCO_2 value varies strongly between seasons. In addition, there is a slight preference for observations to occur in spring, summer, and autumn over winter months. However, there is no discernible difference in the spatial coverage of pCO_2 observations between seasons (data not shown). The aseasonality of $\bar{l}$ can be explained by the "large-scale" mapping error $\sigma_{\mathbf{P}}$, used for the ensemble weights (Eq. A26), to only depend on the distribution of samples $\mathbf{H}_t$ and their respective observational error estimates $\mathbf{S}$. Therefore, the extrapolation approach does not discriminate or distinguish by (pCO_2) value and there is no seasonal imprint in the number of patterns.

4.2 Comparison with other pCO_2 mapping approaches

SOCAT observations have been used previously to build surface pCO_2 climatologies of the Baltic Sea (see Fig. 9 for examples). They rely on observation-driven extrapolation approaches, which can be grouped into different categories: (a) one, where sparse data points are extrapolated based on some statistic metric of influence, e.g., a spatial decorrelation length or time scale, and (b) one where parametrizations with proxy data in combination with filled fields of those proxies are used for extrapolation (Rödenbeck et al., 2015).
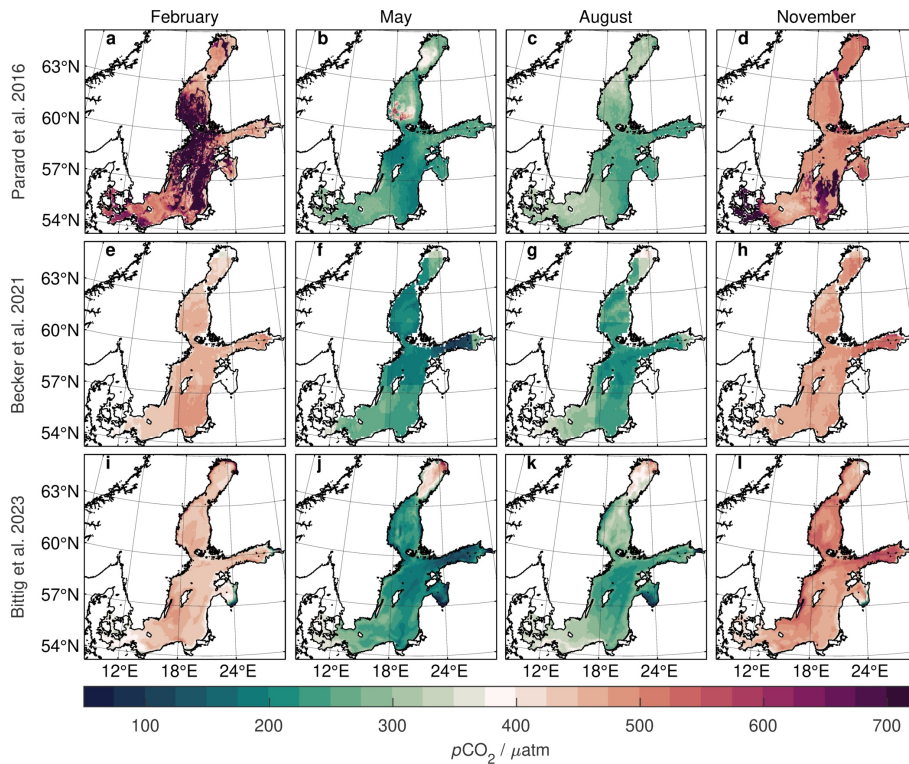
Figure 9. Mean monthly pCO$_2$ distribution for one month per season (left to right) for different climatologies: Parard et al. 2016 (a-d), Becker et al. 2021 (e-h), and this work (i-l). The first two climatologies are proxy-based, where artefacts of the proxy directly translate to pCO$_2$, e.g., for winter time satellite retrievals (a, d) or the subtle 5°x4° gridding in Becker et al. 2021 (e-h). Our approach uses observed pCO$_2$ data directly for mapping, which gives fewer artefacts but is only applicable when pCO$_2$ observations are available.

Our mapping approach belongs to the first category. For a given month or time window, we use the available pCO$_2$ data directly and 1:1 without added transformation to inform the extrapolated pCO$_2$ map. As (spatial) metric of influence, the variability patterns are used. This gives a direct link between observations of a given month or time window and the mapped field. Conversely, if there are no pCO$_2$ observations in a given time window, this directly translates to a (time) gap in the mapped fields for any approach of the first category.

Most previous pCO$_2$ mappings in the Baltic Sea belong to the second category (e.g., Parard et al., 2016; Becker et al., 2021). In a first step, they use all available pCO$_2$ data together with co-located proxies (e.g., location, sea surface temperature, chlorophyll *a* concentration, water depth, distance to coast, season, ...) to establish a relationship or parametrization between proxies and pCO$_2$. In a second step, distributions of those proxy parameters are used to establish a pCO$_2$ distribution in time and space. Here, pCO$_2$ data of a given month do *not* directly inform the extrapolated pCO$_2$ map, but only indirectly through the established relationship using all data. Conversely, if there are no pCO$_2$ observations in a given time window but proxy data

are available, they can be used to estimate a pCO_2 map nonetheless, i.e., (temporal) gap filling is possible with the two-step procedure of approaches of the second category.

As a drawback, mapped pCO_2 fields of the second category rely on the validity of the proxy relationship and equally important on good proxy input data. In some cases, e.g., satellite-based sea surface temperature or chlorophyll a concentration, proxies may be (seasonally) prone to artefacts, e.g., due to stronger cloud cover in winter months. Such artefacts then directly translate into mapped pCO_2 fields and may create unrealistic patterns or out of range values (e.g., Fig. 9a, d; Parard et al., 2016). A mapping approach of the first category such as the one presented here, which uses the observations directly, is not affected by external-source data quality (Fig. 9i–l).

4.3 Long-term pCO_2 trend

The long-term trend of surface pCO_2 in Baltic Sea surface waters has been studied before (Table 1): Wesslander et al. (2010) describe an increase in monthly pCO_2 (ca. +20 μatm yr^{-1}) for the 1993–1998 period in the Eastern Gotland basin, which seems mostly driven by less intense summer pCO_2 minima (from ca. 50 μatm in 1993 to ca. 250 μatm in 1998). For the longer period 1993–2009, they do not detect a significant trend. While Wesslander et al. (2010) use pCO_2 calculated from pH and alkalinity, all further studies are based on the same surface pCO_2 observations archived in SOCAT (Bakker et al., 2016), albeit using different methods and time extents:

Laruelle et al. (2018) found an increase of +2.9$\pm$2.4 μatm yr^{-1} (1 σ) for winter-time pCO_2 from 1995–2011 in the Southern and Central Baltic Sea. At the same time, they see a similar spatial gradient as in our work (Fig. 7) with stronger increase in the South-west and zero or even negative trend in the Northern Gotland basin.

Schneider and Müller (2018) describe an increase of +4.6 to +6.1 μatm yr^{-1} (1 σ between 0.6−1.5 μatm yr^{-1}) for different areas for the 2008–2015 period. However, their analysis did not deseasonalize the observations prior to linear trend analysis. During their analyzed period, there is an increase in observations during autumn and winter (with typically high pCO_2) and a decrease in early spring observations (with typically low pCO_2), while late-spring and summer observations have a similar data coverage over the years. Their relatively high pCO_2 trend estimate therefore seems to be partially caused by a seasonal shift in data availability that was left unaccounted for in the analysis.

Becker et al. (2021) derived a trend of +2.05$\pm$0.12 μatm yr^{-1} for the Southern Baltic Sea (South of 56° N), and of +1.84$\pm$0.21 μatm yr^{-1} for the Central Baltic Sea (between 56° N and 61° N) for the period 1995–2016. However, they observe a stronger trend in earlier years (starting in the 90's) than for later periods (starting in the mid-2000's).

Our analysis covers the more recent period 2003–2021 and gives a significant trend of +1.4$\pm$0.5 μatm yr^{-1} (1 σ) in the Southern Baltic Sea (South of 56.5° N) and of +1.5$\pm$0.7 μatm yr^{-1} in the Åland Sea, parts of the Northern Baltic Proper, and the Gulf of Finland (between 59° N and 61° N). The Central Baltic Sea as well the as the Northern basins themselves show no significant trend. The positive trend (+1.2$\pm$0.6 μatm yr^{-1}) in coastal waters of the Northern basins along the Finnish coast as well as in the Gulf of Riga (Fig. 7) has currently no support by direct observational constraints in those areas (Fig. 2). In contrast, it likely originates from high similarity to other coastal waters (e.g., along the Southern Baltic shore) in the model

Table 1. Summary of long-term pCO_2 trends for different areas and time periods in the Baltic Sea as obtained from different studies.

Study	Time period	Trend $\pm 1\,\sigma$ in μatm yr^{-1}	Area	Note
Wesslander et al. (2010)	1993–1998	+20	Eastern Gotland basin	pCO_2 calculated from pH and alkalinity
Wesslander et al. (2010)	1993–2009	not significant	Eastern Gotland basin	pCO_2 calculated from pH and alkalinity
Laruelle et al. (2018)	1995–2011	+2.9±2.4	Southern and Central Baltic Sea	on winter-time pCO_2
Schneider and Müller (2018)	2008–2015	+4.6 to +6.1 (1 σ 0.6−1.5)	Southern and Central Baltic Sea	shift in seasonal data coverage not accounted for in trend analysis
Becker et al. (2021)	1995–2016	+2.05±0.12	Southern Baltic Sea (South of 56° N)	
Becker et al. (2021)	1995–2016	+1.84±0.21	Central Baltic Sea (56° N – 61° N)	
this work (Fig. 7)	2003–2021	+1.4±0.5	Southern Baltic Sea (South of 56.5° N)	
this work (Fig. 7)	2003–2021	not significant	Central Baltic See; Northern basins	
this work (Fig. 7)	2003–2021	+1.5±0.7	Åland Sea, Northern Baltic Proper, Gulf of Finland (59° N – 61° N)	
this work (Fig. 7)	2003–2021	+1.2±0.6	Coastal waters in Northern basins and Gulf of Riga	without direct observational support

data variability analysis and thus in the variability patterns e_i used for mapping. As such, the pCO_2 increase may be realistic, but lacks field data support.

Together with the literature, our results seem to indicate a reduction in overall surface pCO_2 increase in the Baltic Sea during the past decades, or even its complete absence like in the Central Baltic Sea (Fig. 7) in recent periods. While atmospheric pCO_2 levels are still rising (ca. +2.4 μatm yr^{-1} in the past decade; Lan et al., 2022), this has implications for the CO$_2$ balance between atmosphere and Baltic Sea. It supports previous claims of coastal seas to become a less intense source of CO$_2$ or eventually to turn into (an increasing) CO$_2$ sink (Laruelle et al., 2018).

5 Conclusions

In this work, we developed an extrapolation approach that combines two worlds: Models, specifically the distribution and connectivity that exists in model data variability, and observations in that they provide constraints of the real world picture.

Most notable features of the approach are that it does not tend to give extreme, out-of-range values even with few data constraints and that it provides local error estimates, which reflect both underlying variability, e.g., coast-basin gradients, as well as observational data constraints. We consider of particular merit that the extrapolation scheme adapts its spatial scales to the amount of observations in a certain area, leading to a sound representation of less uncertainty where more data are available.

Used together with high-quality surface pCO_2 data from SOCAT, we established a climatology that covers the entire Baltic Sea. Given the present data scarcity in the Northern basins of the Baltic Sea, a mean pCO_2 climatology is what is reliably achievable today. It can serve as a seasonal baseline of regional pCO_2 evolution that enables assessment of interannual variations, e.g., with respect to timing or amplitude. With sustained and/or enhanced observations in such data poor regions, a fully monthly-resolved pCO_2 dataset will become realistic in the future. To this end, the recently ICOS-adopted SOOP *Tavastland* as well as SOOP *Silja Serenade*, crossing between Stockholm and Helsinki, provide a positive outlook for uncertainty reduction.

Finally, our extrapolation approach as well as the method to establish a climatology is neither limited to pCO_2 nor to the Baltic Sea. Instead, it is transferable to other areas and parameters where the present work can serve as a template.

6 Data availability

Surface pCO_2 data are available from SOCAT (https://www.socat.info, Bakker et al., 2016) and Rehder et al. (2021). ERGOM model output data are available at https://thredds-iow.io-warnemuende.de/thredds/catalogs/projects/integral/catalog_pocNP_V04R25_3nm_agg_time.html?dataset=IOW-THREDDS-Baltic_pocNP_V04R25_3nm_agg_time_2020-11-20-12. The climatology is available from Bittig et al. (2023): https://doi.org/10.1594/PANGAEA.961119.

Appendix A: Extrapolation approach

A1 Notation and mathematical background

To represent a spatial dataset at a given time t with m spatial points, we use the data vector x_t with size $m \times 1$. For a spatial time series of n times, we use the data matrix $\mathbf{X}$ with size $m \times n$, where the n columns correspond to n data vectors x_t. Data in x_t and $\mathbf{X}$ are the deviation from the space-dependent temporal mean $\overline{x}_m$. The empirical data covariance matrix $\mathbf{Q_{XX}}$ with size $m \times m$ is given by

$$\mathbf{Q_{XX}} = \frac{1}{n-1}\mathbf{XX}^{\mathrm{T}} \,. \tag{A1}$$

The singular value decomposition (SVD) or empirical orthogonal function (EOF) decomposition of the data matrix $\mathbf{X}$ decomposes $\mathbf{X}$ into a series of orthonormal factors or principal components according to

$$\mathbf{X} = \mathbf{E}\boldsymbol{\Sigma}\mathbf{A}^{\mathrm{T}} , \tag{A2}$$

where $\mathbf{E}$ is a $m \times m$ orthonormal matrix, $\boldsymbol{\Sigma}$ a $m \times n$ rectangular diagonal matrix, and $\mathbf{A}$ a $n \times n$ orthonormal matrix. With the above convention on m and n, the column vectors e_i (with size $m \times 1$) in $\mathbf{E}$ represent spatial patterns while the column vectors a_i (with size $n \times 1$) in $\mathbf{A}$ represent amplitude time series. They are also called left-singular vectors and right-singular vectors, respectively. The diagonal elements of $\boldsymbol{\Sigma}$ are the so-called singular values s_i of $\mathbf{X}$. Eq. A2 can be written in vector form as

$$x_t = \mathbf{E}\boldsymbol{\Sigma}a_t = \mathbf{E}\alpha_t , \tag{A3}$$

where $\alpha_t = \boldsymbol{\Sigma}a_t$ is the so-called dimensional amplitude at a given time t.

Based on a SVD of $\mathbf{X}$ (Eq.A2), the $m \times m$ matrix $\mathbf{B} = \mathbf{X}\mathbf{X}^{\mathrm{T}}$ can be expressed as

$$\mathbf{B} = \mathbf{X}\mathbf{X}^{\mathrm{T}} = \mathbf{E}\boldsymbol{\Sigma}\mathbf{A}^{\mathrm{T}}\mathbf{A}\boldsymbol{\Sigma}^{\mathrm{T}}\mathbf{E}^{\mathrm{T}} = \mathbf{E}\boldsymbol{\Sigma}\boldsymbol{\Sigma}^{\mathrm{T}}\mathbf{E}^{\mathrm{T}} = \mathbf{E}\tilde{\boldsymbol{\Lambda}}\mathbf{E}^{\mathrm{T}} , \tag{A4}$$

where $\tilde{\boldsymbol{\Lambda}}$ is a diagonal matrix whose diagonal elements are $\tilde{\lambda}_i = s_i^2$. Eq. A4 states the eigendecomposition of $\mathbf{B}$. Since matrix $\mathbf{B}$ is proportional to the covariance matrix $\mathbf{Q}$ (Eq. A1), we can state the eigendecomposition of the data covariance matrix $\mathbf{Q}$ as

$$\mathbf{Q} = \mathbf{E}\boldsymbol{\Lambda}\mathbf{E}^{\mathrm{T}} \tag{A5}$$

with corresponding eigenvalue problem

$$\mathbf{Q}\mathbf{E} = \boldsymbol{\Lambda}\mathbf{E} \tag{A6}$$

and

$$\boldsymbol{\Lambda} = \frac{1}{n-1}\tilde{\boldsymbol{\Lambda}} . \tag{A7}$$

The spatial patterns e_i with size $m \times 1$ are eigenvectors of the data covariance matrix, and the diagonal elements λ_i of $\boldsymbol{\Lambda}$ the corresponding eigenvalues λ_i, which give the amount of variance associated to each e_i. From the set of eigenvectors e_i and their corresponding amount of variance λ_i, the spatial distribution x_t at a given time t can be reconstructed by determination of a suitable amplitude vector a_t (Eq. A3) (see textbooks of linear algebra or statistical data analysis, e.g., Dommenget, 2015).

A2   Truncation of eigenvalue modes

For practical purposes, reconstruction often uses only the first l leading instead of all m eigenvectors e_i ($1 \leq l \leq m$), i.e., $\mathbf{E}$, $\boldsymbol{\Lambda}$, and $\mathbf{A}$ are split into a matrix $\mathbf{E}$, $\boldsymbol{\Lambda}$, and $\mathbf{A}$ of size $m \times l$, $l \times l$, and $n \times l$, respectively, which contain the first l leading

440 eigenvector modes, and a matrix $\mathbf{E}'$, $\mathbf{\Lambda}'$, and $\mathbf{A}'$, which contain the remaining $m - l$ eigenvector modes. Eqs. A2, A3, and A5 thus become

$$\mathbf{X} = \mathbf{E\Sigma A}^{\mathrm{T}} + \mathbf{E}'\mathbf{\Sigma}'\mathbf{A}'^{\mathrm{T}} \ , \tag{A8}$$

$$x_t = \mathbf{E\Sigma} a_t + \mathbf{E}'\mathbf{\Sigma}' a'_t \ , \text{ and} \tag{A9}$$

$$\mathbf{Q} = \mathbf{E\Lambda E}^{\mathrm{T}} + \mathbf{E}'\mathbf{\Lambda}'\mathbf{E}'^{\mathrm{T}} = \mathbf{P} + \mathbf{P}' \ . \tag{A10}$$

445 The leading eigenvector modes e_i cover most part of the data variance and often represent more "large-scale" spatial patterns, while the higher modes than l contain only a small amount of the data variance and can be seen as "small-scale" spatial pattern (Lorenz, 1956; Kaplan et al., 2000; Dommenget, 2015). Correspondingly, the first and second term in Eq. A10 give the large scale and small scale variance $\mathbf{P}$ and $\mathbf{P}'$, respectively, whereas in Eq. A8 and its vector form Eq. A9 they give the large scale and small scale contribution to the spatial data vector x_t, respectively.

450   This split can also be interpreted as decomposition into a "signal" and a "noise" part. Eqs. A8 - A10 with only the l leading modes (i.e., with only the first term) is called a truncated EOF reconstruction, in which dimensionality is reduced from m to l modes. Higher order modes (in $\mathbf{E}'$ and $\mathbf{\Lambda}'$, i.e., the second term) are assumed to be dominated by noise and error and discarded in a truncated eigenvector or EOF reconstruction (Lorenz, 1956; Kaplan et al., 2000).

A3 Extrapolation from observational data

455 To represent a set of k observations at a given time t, we use the observational data vector y_t and the observational error σ_t, both with size $k \times 1$. The transfer operator $\mathbf{H}_t$ is then a "sampling" or observation function that depends on the spatial configuration of the observation points and samples from the data vector x_t of size $m \times 1$ so that the result $\hat{x}_t$,

$$\hat{x}_t = \mathbf{H}_t x_t \ , \tag{A11}$$

has the same size $k \times 1$ as the observations. To be comparable with $\hat{x}_t$, the observational data y_t are expressed as deviation
460 from the space-dependent temporal mean $\overline{x}_m$, too (Elken et al., 2019).

    The eigenvalue reconstruction in truncated form (Eq. A9) then becomes:

$$\mathbf{H}_t x_t = \mathbf{H}_t \mathbf{E\Sigma} a_t \ . \tag{A12}$$

Minimization of a suitable cost function Q, e.g., for least-squares optimization as in Elken et al. (2019),

$$Q(\alpha_t) = (\mathbf{H}_t \mathbf{E} \alpha_t - y_t)^{\mathrm{T}} (\mathbf{H}_t \mathbf{E} \alpha_t - y_t) \ , \text{with} \tag{A13}$$

465     $$\alpha_t = \mathbf{\Sigma} a_t \ , \tag{A14}$$

yields a system of l linear equations with l unknowns (Elken et al., 2019):

$$\mathbf{D}\alpha_t = \mathrm{h} \ , \text{with} \tag{A15}$$

$$\mathbf{D} = \mathbf{E}^{\mathrm{T}} \mathbf{H}_t^{\mathrm{T}} \mathbf{H}_t \mathbf{E} \ , \text{ and} \tag{A16}$$

$$\mathrm{h} = \mathbf{E}^{\mathrm{T}} \mathbf{H}_t^{\mathrm{T}} y_t \ , \tag{A17}$$

470   which provides the observation-based eigenvector amplitudes α_t or a_t (Eq. A14), respectively.

With Eq. A9 in truncated form and Eq. A14, the data vector x_t can be obtained, i.e., an extrapolation from $k \times 1$ observational data points y_t to the entire spatial domain of $m \times 1$ data points x_t with help of the truncated eigenvalue decomposition of $m \times l$ eigenvectors and l eigenvalues e_i and λ_i, or $\mathbf{E}$ and $\mathbf{\Lambda}$, respectively.

A4   Error considerations

475   Both "observational error" and "representational error" impact the determination of the eigenvector amplitudes a_t. Observational error σ_t includes both instrumental and sampling error and can be used to limit the impact of observational data constraints y_k (Kaplan et al., 2000). Representational error is the error made by truncation, i.e., by using only the l largest, leading eigenvectors and neglecting the remainder of the spectrum, which can be derived from the "small-scale" covariance $\mathbf{P}'$ contribution (Kaplan et al., 2000).

480   The error covariance matrix $\mathcal{R}$ is the sum of the observational data error covariance $\mathbf{S}$ and a term that accounts for the covariance created in the truncated modes $\mathbf{E}'$ not resolved by the analysis:

$$\mathcal{R} = \mathbf{S} + \mathbf{H}_t \mathbf{E}' \mathbf{\Lambda}' \mathbf{E}'^T \mathbf{H}_t'^T = \mathbf{S} + \mathbf{H}_t \mathbf{P}' \mathbf{H}_t'^T \ , \tag{A18}$$

where $\mathbf{S}$ is a diagonal matrix with the observations' variance σ_t^2 on the diagonal and $\mathbf{H}_t$ the aforementioned sampling operator (Kaplan et al., 2000).

485   By addition of constraints on the cost function Q (a) to limit the estimated eigenvector amplitudes based on the amount of variance they explain in the original eigenvalue decomposition, and (b) that a_t determination is limited by the uncertainty of observations and from truncation (see above), Eq. A13 is modified to (Kaplan et al., 2000):

$$Q(\alpha_t) = (\mathbf{H}_t \mathbf{E} \alpha_t - y_t)^T \mathcal{R}^{-1} (\mathbf{H}_t \mathbf{E} \alpha_t - y_t) + \alpha_t^T \mathbf{\Lambda}^{-1} \alpha_t \ , \tag{A19}$$

and the solution Eqs. A15-A17 thus becomes (Kaplan et al., 2000):

$$490 \quad \mathbf{D} \alpha_t = \mathrm{h} \ , \text{with} \tag{A20}$$

$$\mathbf{D} = \mathbf{E}^T \mathbf{H}_t^T \mathcal{R}^{-1} \mathbf{H}_t \mathbf{E} + \mathbf{\Lambda}^{-1} \ , \text{ and} \tag{A21}$$

$$\mathrm{h} = \mathbf{E}^T \mathbf{H}_t^T \mathcal{R}^{-1} y_t \ . \tag{A22}$$

On the other hand, the large scale portion of the data covariance $\mathbf{Q}$ (Eq. A10) can be obtained from this solution according to (Kaplan et al., 2000):

$$495 \quad \mathbf{P} = \mathbf{E} \mathbf{D}^{-1} \mathbf{E}^T \ . \tag{A23}$$

$\mathbf{P}$ can be seen as the mapping uncertainty of the extrapolation.

Note that the calculation of $\mathbf{P}$ only requires the sampling operator $\mathbf{H}_t$, i.e., where samples are present, as well as an observational error estimate $\mathbf{S}$, but not the actual observations or amplitudes at these locations. In case of absence of any observation,

$\mathbf{H}_t$ contains only zeros and eqs. A21 and A23 then simplify to $\mathbf{D} = \mathbf{\Lambda}^{-1}$ and $\mathbf{P} = \mathbf{E}\mathbf{\Lambda}\mathbf{E}^{\mathrm{T}}$ (compare Eq. A10), respectively. Addition of observational constraints thus reduces the mapping uncertainty $\mathbf{P}$.

For our purposes, we assume that *off-diagonal* elements in the covariance $\mathbf{P}'$ are negligible, i.e., that the truncated eigenvector modes $\mathbf{E}'$ are sufficiently small scale and their variances $\mathbf{\Lambda}'$ are small enough that they do not show a noticeable covariance contribution (Eq. A18). We therefore approximate $\mathbf{P}'$ by a diagonal matrix whose diagonal elements are obtained from rearrangement of Eq. A10:

$$\mathrm{diag}(\mathbf{P}') = \mathrm{diag}(\mathbf{Q}) - \mathrm{diag}(\mathbf{E}\mathbf{\Lambda}\mathbf{E}^{\mathrm{T}}) \,, \tag{A24}$$

where $\mathbf{Q}$ is accessible from the data $\mathbf{X}$ (Eq. A1) and the second term from the truncated eigenvalue decomposition.

A5 Number of significant modes

A critical aspect before any extrapolation from observations is how many modes e_i to use, or – in other words – where to truncate reconstruction, i.e., how to distinguish between modes representing desired variability and modes representing "noise". Often, an arbitrary threshold of the total variance covered by the l leading modes is chosen (e.g., Kaplan et al., 2000).

Here, we apply the DINEOF variant of SVD or EOF decomposition of the dataset $\mathbf{X}$ to find the l_{max} leading eigenvectors e_i. The number l_{max} of significant modes is determined by a cross-validation procedure from the data $\mathbf{X}$ (Beckers and Rixen, 2003) and we use this l_{max} as the upper bound for l in our ensemble approach (see below).

A6 Ensemble approach for robustness and locality

Depending on the spatial distribution or clustering of observations y_t, not all amplitudes of the l_{max} spatial eigenvectors e_i may be well-constrained. In some configurations, e.g., with few or clustered observations, where $\mathbf{H}_t$ selects only few of the m spatial data points, a reconstruction with fewer modes than l_{max} may give a solution with a smaller mapping uncertainty $\mathbf{P}$ than the truncated reconstruction with all l_{max} modes e_i.

We therefore use an ensemble approach over the truncated reconstructions where we vary l from just 1 mode to l_{max} modes,

$$\overline{\mathcal{X}} = \frac{\sum_{l=1}^{l_{\mathrm{max}}} w_l \cdot \mathcal{X}_l}{\sum_{l=1}^{l_{\mathrm{max}}} w_l} \,, \tag{A25}$$

where the weights w_l (with size $m \times 1$) are based on the diagonal elements of $\mathbf{P}$, i.e., the variance $\sigma_{\mathbf{P},t}^2$ or mapping uncertainty of the extrapolation:

$$w_l = 1 \left/ \frac{\sigma_{\mathbf{P},t}^2}{\sum^m \sigma_{\mathbf{P},t}^2} \right. \,. \tag{A26}$$

As the mapped variance $\mathrm{diag}(\mathbf{P})$ varies in magnitude with the number of eigenvectors included, the weights w_l for a given number of modes l are normalized by the total variance over all m data points, which gives a normalized spatial weight vector w_l (Eq. A26). For a given spatial data point m, preference is thus given to reconstructions where it is among the better constrained ones for the given number of modes l.

For $\mathcal{X}_l$, each using only the first l ($\leq l_{\mathrm{max}}$) eigenvector modes (Eq. A25), we insert:

- the reconstructed data vector x_t (from Eq. A9 in truncated form) to yield as $\overline{\mathcal{X}}$ the ensemble mean $\overline{x_t}$,

- the term $(\overline{x_t} - x_t)^2$ to yield as $\overline{\mathcal{X}}$ the biased weighted sample variance about the ensemble mean $\sigma_{t,\mathrm{mean}}^2$,

- the mapping variance $\sigma_{\mathbf{P},t}^2$ (i.e., the diagonal of $\mathbf{P}$; Eq. A23) to yield as $\overline{\mathcal{X}}$ the remaining mean "large-scale" variance $\overline{\sigma_{\mathbf{P},t}^2}$,

- the approximation of the truncated variance $\sigma_{\mathbf{P}',t}^2$ (i.e., the diagonal of $\mathbf{P}'$; Eq. A24) to yield as $\overline{\mathcal{X}}$ the mean "small-scale" variance $\overline{\sigma_{\mathbf{P}',t}^2}$, and

- the number of modes l itself to yield as $\overline{\mathcal{X}}$ the average number of modes $\overline{l}$ used in the reconstruction

as a spatial vector of size $m \times 1$ each, i.e., on the full spatial domain. The reconstructed data vector $x_{t,\mathrm{reconstr}}$ and the total variance of reconstruction $\sigma_{t,\mathrm{reconstr}}^2$ are given by

$$x_{t,\mathrm{reconstr}} = \overline{x_t} \tag{A27}$$

$$\sigma_{t,\mathrm{reconstr}}^2 = \sigma_{t,\mathrm{mean}}^2 + \overline{\sigma_{\mathbf{P},t}^2} + \overline{\sigma_{\mathbf{P}',t}^2} \tag{A28}$$

A7 Temporal coherence

So far, we considered the observations y_t and the reconstructed data vector x_t to originate and be valid for a given time t, respectively. However, in practice, observations y will spread over a certain time extent Δt, e.g., days for a single SOOP transect to weeks for a basin-covering cruise. If this time extent (e.g., duration of a cruise) is comparable to the time scale of the system's dynamics (e.g., spring surface warming or bloom onset), distortions in the reconstructed fields x_t may occur (Elken et al., 2019) as different "states" of the system could be sampled at different space-time locations.

To collate temporally extended observations into a common synoptic reconstruction without artifacts, Elken et al. (2019) add a linear temporal (short-term) trend for each eigenvector mode to the optimization, thus collating observations made at different observation times t_p to a common reference time instance $t_\circ$.

To this end,

- the time difference Δt_p between observation and reference time is introduced:

$$\Delta t_p = t_p - t_\circ . \tag{A29}$$

- The sampling operator $\mathbf{H}_t$ is extended to not only sample from the eigenvector e_i the value, χ, corresponding to the observation, but also the value times the time difference, $\chi \cdot \Delta t_p$, corresponding to a (short-term) time gradient. $\mathbf{H}_t\mathbf{E}$ thus becomes a matrix of size $k \times 2l$.

- The l eigenvalues are replicated with a constant scaling factor, so that $\mathbf{\Lambda}$ becomes a $2l \times 2l$ diagonal matrix. I.e., both the value (first l eigenvalues) and its time difference (second l eigenvalues times scaling factor) follow the same eigenvectors e_i order and importance with the scaling factor to determine the balance between between both. Based on preliminary
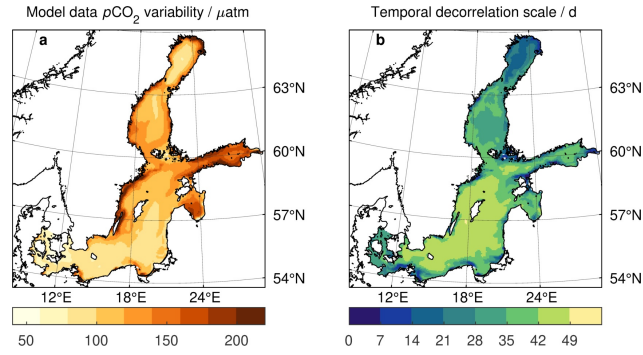
Figure A1. Model data $\mathbf{X}$ characteristics: (a) $p\text{CO}_2$ variability shown by the square-root of the model data covariance matrix $\mathbf{Q}$'s diagonal elements, i.e., the standard deviation of the $p\text{CO}_2$ data $\mathbf{X}$ at each location. (b) $p\text{CO}_2$ variability shown by the temporal decorrelation time scale, i.e., the time (in days) at which the lagged autocorrelation drops below a threshold of 0.63 correlation. Less than 1 % of locations have a temporal decorrelation scale of ≤ 7 d, while about 25 % are within ≤ 30 d. To adequately reflect the $p\text{CO}_2$ data dynamics in the variability pattern extraction (section 2.2.1), a weekly aggregation of the model data $\mathbf{X}$ was therefore chosen compared to, e.g., daily or monthly model output.

tests, we used an empirical scaling between spatial value pattern and temporal trend pattern of $9 \cdot 10^{-4}$, equal to a ratio of approx. 1 μatm per 33 days.

560   – The eigenvalue amplitude vector a_t is doubled in size to $2l \times 1$, where the first l values continue to represent the eigenvectors' e_i amplitudes, while the second l values represent their temporal derivative.

Thus, the system of linear equations (Eqs. A20-A22) becomes a system of $2l$ equations with $2l$ unknowns, and the reconstruction (Eq. A9) provides both an extrapolation to the entire spatial domain of $m \times 1$ data locations at reference time $t_\circ$ as well as a temporal trend of change on the $m \times 1$ data locations at reference time $t_\circ$ (Elken et al., 2019).

565 Appendix B: Seasonal $p\text{CO}_2$ from value and linear trend climatology by cubic Hermite spline calculation

With a $p\text{CO}_2$ value x and linear $p\text{CO}_2$ trend d given for each month of the climatology, the seasonal evolution of $p\text{CO}_2$ at a given location m can be calculated as a cubic Hermite spline according to:

$$
\begin{aligned}
x_t = h_{00}(\gamma) \cdot x_k \quad &+ h_{10}(\gamma) \cdot d_k \quad \cdot (t_{k+1} - t_k) + \ldots \\
h_{01}(\gamma) \cdot x_{k+1} &+ h_{11}(\gamma) \cdot d_{k+1} \cdot (t_{k+1} - t_k) \,, \text{ with}
\end{aligned}
\tag{B1}
$$
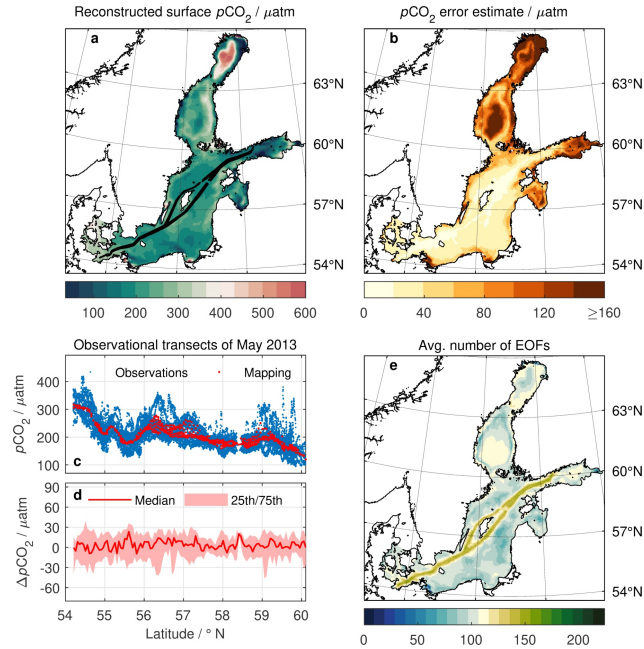
Figure A2. Same as Fig. 3 but without temporally collating the observations to the middle of the month (details in section A7). The general picture of (a) reconstructed pCO_2 $x_{t,\mathrm{reconstr}}$, (b) pCO_2 error estimate $\sigma_{t,\mathrm{reconstr}}$, and (e) average number of patterns $\bar{l}$ of the reconstruction is comparable to the temporally coherent reconstruction (Fig. 3a, b, g, respectively), but (c) mapped pCO_2 (red) gives only one uniform value throughout the month and (d) differences to observations are therefore increased (compare Fig. 3e, f).

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$$h_{00}(\gamma) = 2\gamma^3 - 3\gamma^2 + 1 \ , \tag{B2}$$

$$h_{10}(\gamma) = \ \gamma^3 - 2\gamma^2 + \gamma \ , \tag{B3}$$

$$h_{01}(\gamma) = -2\gamma^3 + 3\gamma^2 \ , \tag{B4}$$

$$h_{11}(\gamma) = \ \gamma^3 - \gamma^2 \ , \text{ and} \tag{B5}$$

575
$$\gamma = \frac{t - t_k}{t_{k+1} - t_k} \ . \tag{B6}$$

Here, t_k and t_{k+1} are the times of the climatological month before and after the time t of interest, and γ gives the normalized time. $h(\gamma)$ are Hermite basis functions and x_k and x_{k+1} as well as d_k and d_{k+1} are the associated monthly pCO_2 value and pCO_2 trend, respectively, which determine the seasonal pCO_2 x_t at time t.

Author contributions. HCB and GR conceived the study. The method was developed by HCB with important input by EJ and GR. TN
580   performed the model simulations and HCB the analysis. HCB lead the manuscript writing with contributions by all co-authors.
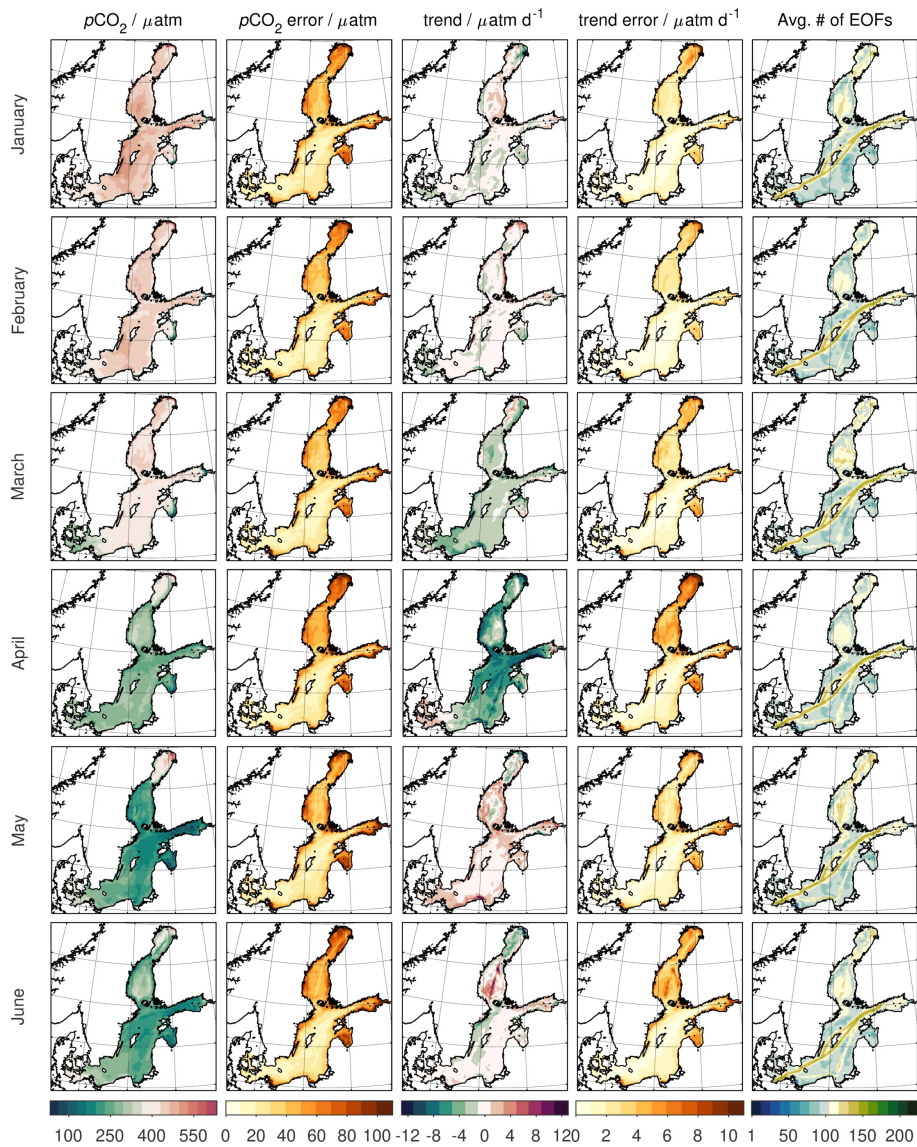
Figure A3. Monthly climatology **Y** of surface pCO_2, pCO_2 error estimate, pCO_2 trend, pCO_2 trend error estimate, and average number of EOF patterns in the ensemble (left to right) for the months Jan. – June (top to bottom).

Competing interests. The authors declare that they have no conflict of interest.

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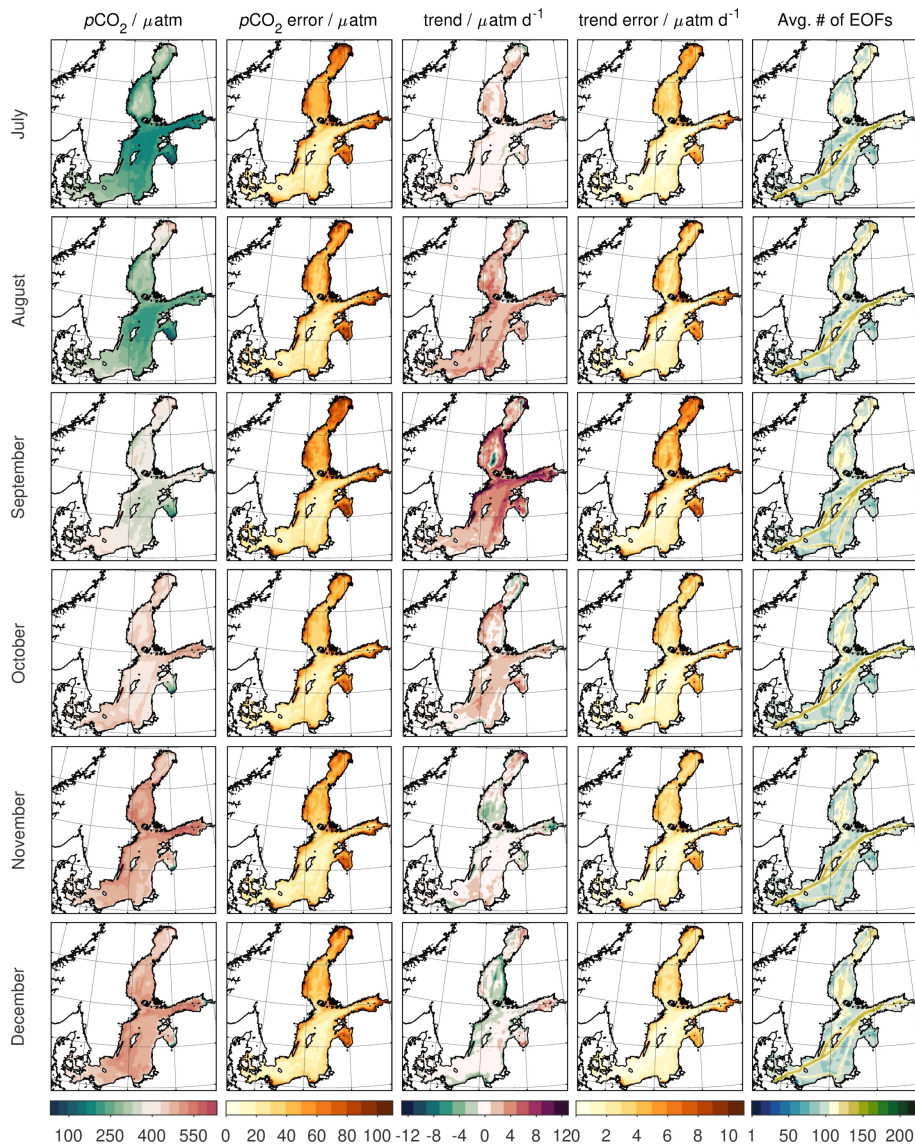
Figure A4. Same as Fig. A3 but for July – Dec.

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