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4 # The ULR-repro3 GPS data reanalysis and its estimates of
5 # vertical land motion at tide gauges for sea level science

7 *Médéric Gravelle[1], Guy Wöppelmann[1], Kévin Gobron[1,2],*

8 *Zuheir Altamimi[3,4], Mikaël Guichard[1], Thomas Herring[5], Paul Rebischung[3,4]*

10 [1] LIENSs, CNRS – La Rochelle University, 17000 La Rochelle, France
11 [2] Royal Observatory of Belgium, Uccle, Belgium
12 [3] Université de Paris, Institut de physique du globe de Paris, CNRS, IGN, F-75005
13 Paris, France
14 [4] ENSG-Géomatique, IGN, F-77455 Marne-la-Vallée, France
15 [5] MIT, Cambridge, MA, USA

17 *Correspondence to*: Médéric Gravelle (mederic.gravelle@univ-lr.fr)

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Abstract

A new reanalysis of Global Navigation Satellite System (GNSS) data at or near tide gauges worldwide was produced by the University of La Rochelle (ULR) group within the 3rd International GNSS Service (IGS) reprocessing campaign (repro3). The new solution, called ULR-repro3, complies with the IGS standards adopted for repro3, implementing advances in data modelling and corrections since the previous reanalysis campaign, and extending the average record length by about 7 years. The results presented here focus on the main products of interest for sea level science, that is, the station position time series and associated velocities on the vertical component at tide gauges. These products are useful to estimate accurate vertical land motion at the coast and supplement data from satellite altimetry or tide gauges for an improved understanding of sea level changes and their impacts along coastal areas. To provide realistic velocity uncertainty estimates, the noise content in the position time series was investigated considering the impact of non-tidal atmospheric loading. Overall, the ULR-repro3 position time series show reduced white noise and power-law amplitudes and station velocity uncertainties compared to the previous reanalysis. The products are available via SONEL (https://doi.org/10.26166/sonel_ulr7a; Gravelle et al., 2022).

1 Introduction

Vertical land motion plays a crucial role in understanding sea level changes and its spatial variability (Wöppelmann & Marcos, 2016; Frederikse *et al*., 2020; Hamligton *et al*., 2020; for recent reviews and references therein). This is especially true along the coasts, where its monitoring is often an essential requirement to assess the extent of the environmental and socio-economic threats posed by changing sea levels in a warming climate at regional or local scales (Magnan *et al*., 2020). Changes in sea level can be measured relative to the land by tide gauges, or relative to the Earth's center of mass by satellite altimeters (e.g., Marcos *et al*., 2019). In both relative (tide gauge) and geocentric (satellite) measuring systems, accurate estimates of vertical land motion are essential, either to disentangle the solid Earth contribution from other factors in tide gauge records (Woodworth *et al*., 2019), or to supplement satellite altimetry data to assess relative sea level change for coastal studies and planning (Poitevin *et al*., 2019).

In the last decades, significant efforts have been undertaken to produce accurate estimates of vertical land motion at tide gauges using Global Navigation Satellite System (GNSS) data (e.g., Sanli and Blewitt, 2001; Wöppelmann *et al*., 2007; Hammond *et al*., 2021). Wöppelmann *et al*. (2007) showed the importance of applying a homogeneous GNSS data reanalysis strategy across the entire data span, that is, using the same modelling, corrections and parameterization, to address the demand of accurate position time series and velocities for sea level studies. This conclusion was reached independently by Steigenberger *et al*. (2006) within the International GNSS Service (IGS; Johnston *et al*., 2017). Since then, the IGS has conducted several data reanalysis campaigns, stimulated by progress in modelling and corrections, lengthening of measurement records and updates of the International Terrestrial Reference Frame (ITRF) realizations (Rebischung *et al*., 2016).

In 2019, the IGS launched a third reprocessing campaign, designated as 'repro3', involving the international GNSS community (Rebischung, 2021). The University of La Rochelle (ULR) group contributed to this effort with a solution (ULR-repro3), which specifically includes a large selection of reliable GNSS stations near tide gauges. This paper describes the latest ULR solution in a series, succeeding previous releases described in Wöppelmann *et al*. (2009) and Santamaria-Gomez *et al*. (2017). This solution complies with the modelling and corrections adopted for 'repro3' (Rebischung, 2021; http://acc.igs.org/repro3/repro3.html), for example, corrections are made for antenna phase centre and solid Earth tides (see Section 2.2.1) . It

72 specifically highlights the time series of station positions and their vertical velocities, which are

73 the main products of interest for the sea level community. A crucial piece of information for

74 the practical use of these products is their uncertainties, which must account for the presence of

75 time-correlated stochastic variations (or noise) in the position time series (Williams *et al*.,

76 2004). Consequently, this paper also presents the statistical modelling strategies employed to

77 derive realistic uncertainty estimates. These results are presented together with a comparison

78 with respect to the previous ULR solution to appraise the progress accomplished over the past

79 seven years.

80

2 The ULR-repro3 products

2.1 Input data

83 Although the term GNSS is employed throughout the manuscript, the ULR-repro3 reanalysis

84 considered Global Positioning System (GPS) observations only. The GNSS measurements were

85 retrieved from the SONEL archive (www.sonel.org) in the form of station-specific daily files

86 in the international standard RINEX format (https://igs.org/wg/rinex/). These contain dual-

87 frequency carrier phase and pseudo-range measurements with a typical sampling of 30s.

88 SONEL holdings include data from over 1,200 stations around the world, amounting to over

89 6,300,000 daily files. A station selection was applied with the criteria of targeting time series

90 with over three years of continuous GNSS measurements and 70% completeness, located at or

91 near a tide gauge (within 15km). The term "continuous" denotes that no offset discontinuity in

92 the station position was anticipated from the metadata available, that is, from the station

93 operation logfiles, which should report changes in instrumentation, or from the co-seismic

94 displacements predicted using the earthquakes database and modelling described by Métivier

95 *et al*. (2014), updated to 2020. Some exceptions to these selection criteria concerned the French

96 GNSS stations at tide gauges, as part of the ULR commitment for France to the global sea level

97 observing (GLOSS) programme of the Intergovernmental Oceanographic Commission. This

98 programme was initiated in 1985 to establish a well-designed, high-quality *in situ* sea level

99 observing network to support a broad research and operational user base. Its primary products

100 are sea levels from permanent tide gauges provided with different sampling rates, data latencies

101 and averaging periods (IOC, 2012). SONEL is one of the five global data centres of GLOSS,

102 dedicated to assembling raw measurements from permanent GNSS stations at or near tide

103 gauges, as well as products of their analysis (GNSS position time series and velocities).

104

105 The spatial distribution of the GNSS stations considered in ULR-repro3 is shown in Figure 1

106 with symbols coloured according to the record length, ranging from 3 months to 21 years. The

107 last year processed is 2020, instead of 2013 for the previous ULR reanalysis (Santamaria-

108 Gomez et al., 2017), reaching an overall extension of seven years with a median station record

109 length of 13.1 years. The station network shows a global distribution (Figure 1) with stations

110 that are obviously far from coastlines: they were added from the IGS repro3 station priority list

111 as reference frame stations to ensure an optimal alignment to the International Terrestrial

112 Reference Frame (ITRF) and estimation of the satellite orbits. The ULR-repro3 station network

113 ultimately consists of 601 GNSS stations (Figure 1), among which 176 are reference stations.

114

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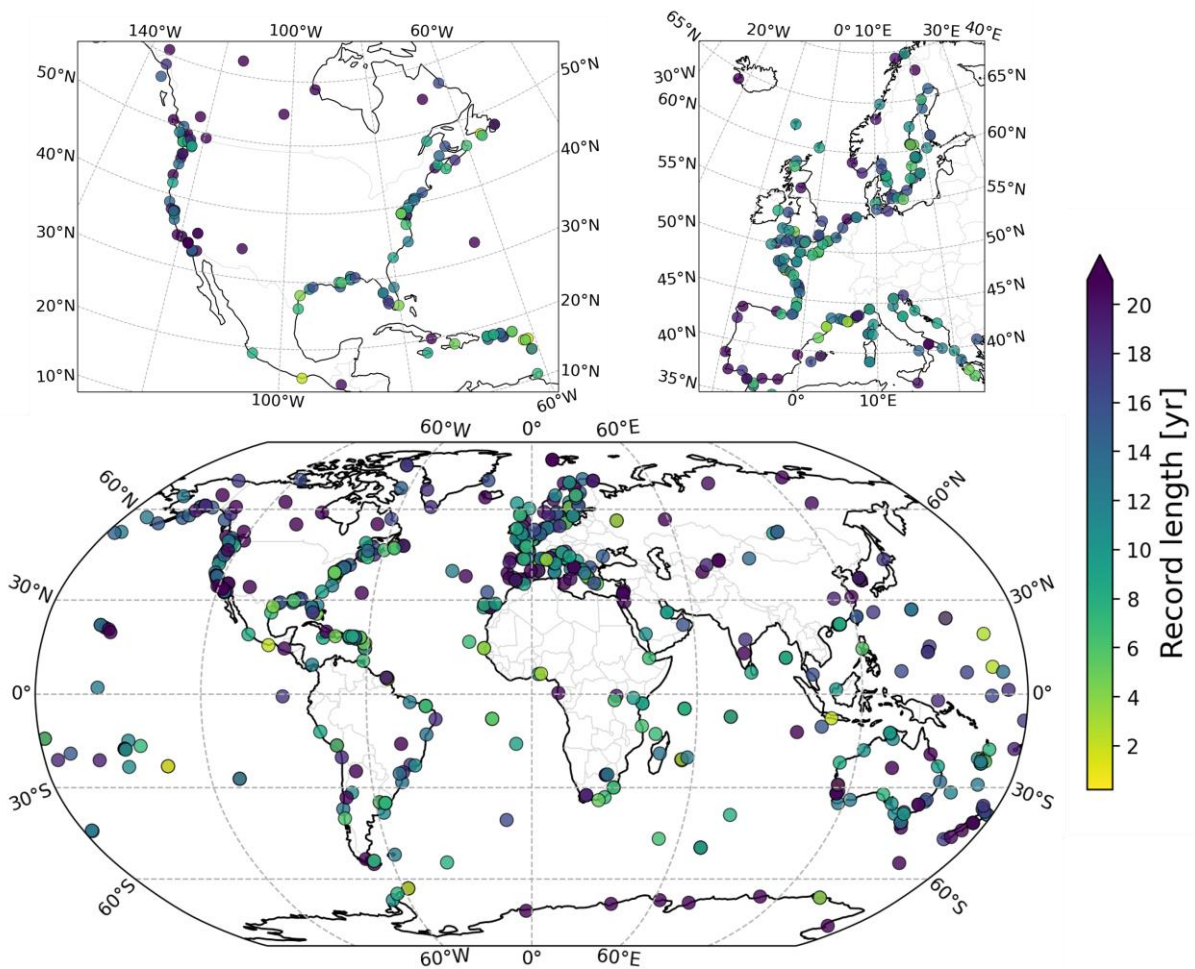

116 **Figure 1**: Spatial distribution of the 601 GNSS stations in ULR-repro3 and record length (colour bar),

117 whose median is 13.1 years, spanning the 2000.0-2021.0 period.

118

2.2 GNSS processing

120 Estimating accurate vertical land motion from GNSS measurements involves several essential

121 steps, such as computing daily station positions or deriving trends from the position time series.

122 In the first step, many corrections are applied, and other parameters such as satellite orbits or
123 atmospheric delays are adjusted along with the station positions (details in Section 2.2.1). It
124 requires advanced modelling and corrections and is usually best performed in a free-network
125 approach or loosely constrained strategy (Heflin *et al*., 1992; Altamimi *et al*., 2002), whose
126 major output is a global set of daily station positions expressed in an undetermined terrestrial
127 frame. The next step is to align these global solutions of daily station positions to a stable and
128 well-defined terrestrial frame such as the ITRF2014 (Altamimi *et al*., 2017). The last step
129 involves modelling the kinematics described by the position time series, to obtain the quantity
130 of interest (trends, periodic oscillations, step discontinuities, etc.). Each step involves analyst
131 choices that can affect the estimated quantity of interest, and subsequently the geophysical
132 interpretation. The details below can thus be crucial to understand the results and their
133 uncertainties.
134
135 *2.2.1 Modelling & Corrections*
136 The ULR-repro3 processing considered the advances that occurred over the past seven years,
137 since the second IGS reanalysis campaign (Rebischung *et al*., 2016). It complies with the
138 highest international standards, which were adopted by the IGS for the third reprocessing
139 campaign (http://acc.igs.org/repro3/repro3.html). The new modelling and corrections were
140 implemented in the GAMIT/GLOBK software packages (Herring et al., 2015; 2018) used here,
141 in particular the International Earth Rotation and Reference Systems Service (IERS) linear pole
142 model adopted in 2018 and the high-frequency (subdaily) Earth Orientation Parameters (EOP)
143 tide model from Desai and Sibois (2016). Table 1 provides a summary of the main modelling
144 features and corrections applied in the ULR-repro3 reanalysis.
145

146

ULR-repro3 modelling and corrections	
Observations	double-differenced phase observations (GPS only, L1 & L2)
Sessions and sampling	24-hr sessions; 2 min. sampling (30s in the data cleaning)
Elevation cut-off angle	10 degrees
Antenna phase center	igsR3_2135.atx (IGS Mail by A. Villiger, Dec. 2020)
Ionosphere refraction	ionosphere-free linear combination (1st order effect); 2nd and 3rd order corrections using IGRF13 (Alken *et al.*, 2021) and IGS combined IONEX files.
Troposphere refraction	A priori zenith delays from Saastamoinen model, mapped with VMF1 functions (Böhm *et al.*, 2006); zenith wet delays estimated at 1-hr intervals and gradients in north-south and east-west directions at 24-hr intervals.
Gravity field model	EGM2008 up to degree and order 12 (Pavlis *et al.*, 2012)
Solid Earth tides	IERS conventions (Petit & Luzum, 2010)
Ocean tide model	FES2014b (Lyard *et al.*, 2021)
Mean pole	linear mean pole as adopted by IERS in 2018
Subdaily EOP model	Earth Orientation Parameters tide model from Desai and Sibois (2016)
Ocean tide loading	Provided by the EOST loading service (J.P. Boy; http://loading.u-strasbg.fr) using the ocean tide model FES2014b (Lyard *et al.*, 2021)

147 **Table 1**: Main features of the GNSS data analysis strategy adopted for ULR-repro3 following

148 the IGS recommendations (http://acc.igs.org/repro3/repro3.html).

149

150 The remaining aspects of the ULR-repro3 data analysis strategy align with the approach used

151 in Santamaria-Gomez *et al.* (2017), so the following only briefly outlines them to understand

152 the analyst choices for geophysical application and interpretation. For each network of stations,

153 double-differenced GPS phase observations were processed in the ionosphere-free L1/L2 linear

154 combination. To minimize the impact of mismodeled low-elevation tropospheric delays,

155 satellite observations below 10 degrees were not considered. This cut-off angle aims to mitigate

156 the limitation due to ground antennas without absolute calibration (13% of the antennas in the

157 ULR-repro3 network). These antennas have a relative calibration (with respect to an antenna

158 with absolute calibration) converted to absolute considering only elevation-dependent phase

159 centre variation (PCV) down to 10 degrees. For the other (calibrated) GNSS antennas, phase

160 centre offsets with azimuth-dependent and elevation-dependent absolute PCV corrections were

161 applied (igsR3_2135.atx; IGS Mail by A. Villiger, 2020). Satellite-specific antenna phase

162 centre offsets and block-specific nadir angle-dependent absolute PCV were applied for the

163 transmitting antennas.

164

165   The first-order ionospheric delays were removed using the ionosphere-free linear combination

166   observations, whereas the second and third orders were corrected using the International

167   Geomagnetic Reference Field model (Alken *et al*., 2021) and total electron content maps from

168   the IGS IONEX files. For the tropospheric delays, a priori hydrostatic zenith delays at the

169   ellipsoidal surface were obtained for each station from the VMF1 grids (Böhm *et al*., 2006).

170   They were then reduced to the station heights using the GPT2 model (Lagler *et al*., 2013). The

171   residual zenith tropospheric delays were adjusted at 1-hr intervals (i.e., 25 parameters per day)

172   for every station using a piecewise linear model, assuming the unmodeled wet component

173   dominates. Both the hydrostatic and wet zenith tropospheric delays were mapped to the

174   observation elevations using the VMF1 functions. The azimuthal asymmetry in the tropospheric

175   delay was accounted for by estimating a linear change in gradients (north-south and east-west)

176   over each day and station using the mapping function from Chen and Herring (1997).

177

178   The phase observations were weighted by elevation angle in the first iteration, and then by

179   elevation angle and station-dependent scatter of the phase residuals obtained from the first

180   iteration. The double-differenced phase ambiguities were adjusted to real values except when

181   they could be confidently fixed to integer values (more than 85% fixed). Within the same

182   inversion, GNSS satellite orbital parameters were adjusted using 24-hr arcs, IGS orbits as a

183   priori values and loose constraints consistent with the station position constraints (free-network

184   approach). Non-gravitational constant and once-per-revolution accelerations on the satellites

185   were adjusted too, using the ECOMC model. This model is a combination of the ECOM1 and

186   ECOM2 models (Springer *et al.*, 1999; Arnold *et al.*, 2015) with specific parameters

187   constrained in post-processing. Nominal satellite attitude corrections were applied, except

188   during eclipse periods where yaw rates were modelled (Kouba, 2009). Phase rotations due to

189   changes in the satellite antenna orientation away from the Earth-pointing direction were also

190   applied (Wu *et al*., 1993). Regarding the Earth orientation parameters (pole position, rate and

191   length of day), these were estimated daily with a priori values from the IERS Bulletin A.

192   Modelled diurnal and semi-diurnal terms were added to the a priori pole and UT1 values

193   following the IERS Conventions (Petit and Luzum, 2010).

194

195   Note that neither loading displacements due to atmospheric tides nor non-tidal (atmospheric,

196   oceanic, hydrologic) loading displacements were corrected during the first step, which aimed

197   at estimating daily station positions from the GNSS measurements. By contrast, the

198   displacements of the crust due to solid-Earth and pole tides (solid Earth and ocean) were

199   corrected following the IERS Conventions (Petit and Luzum, 2010). Crustal motion due to the

200   ocean tide loading was corrected too, using the tidal constituents computed by EOST loading

201   service at each station from the FES2014b model (Lyard *et al.*, 2021).

202

2.2.2. Offset detection & terrestrial frame alignment

204   Figure 2 shows the number of stations selected for ULR-repro3 with GNSS observations

205   available each day over the time period considered (2000.0-2021.0), ranging from 110+ to

206   nearly 500 stations. For computational efficiency, the stations were split into several (up to 10)

207   regional subnetworks, each having between 29 and 70 stations processed independently. For

208   the reader interested in this technicality, Figure S1 shows the regional subnetworks distribution

209   for the day 2018-01-01. An additional subnetwork of globally distributed stations was

210   considered to allow the daily combination of the regional subnetwork results in a unique daily

211   global solution. This global subnetwork was made up of IGS reference frame stations, each of

212   which also appeared in one – and only one – of the regional subnetworks. In turn, one regional

213   subnetwork included one IGS reference frame station at least, but could include more depending

214   on the total number of subnetworks. Moreover, to strengthen the physical link between regional

215   subnetworks, two stations from adjacent regional subnetworks were also included, that is, one

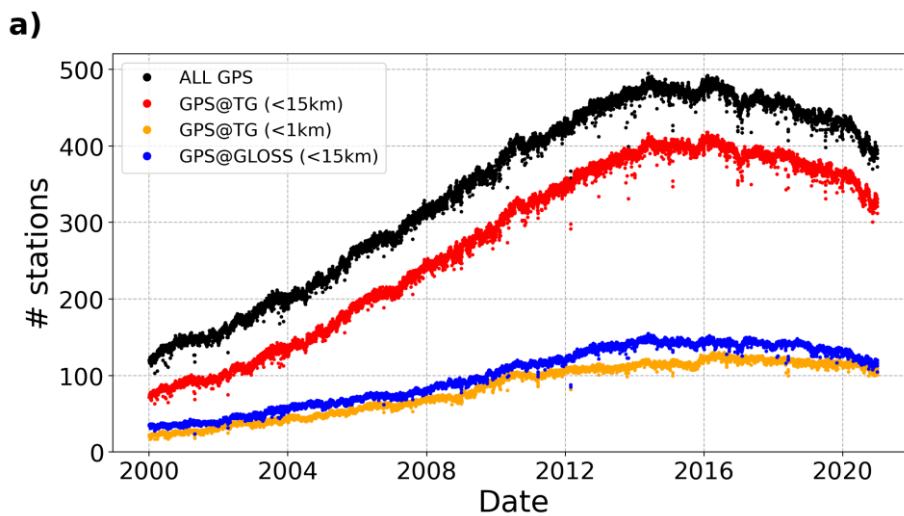
216   station from one nearby subnetwork and another from another nearby subnetwork, exclusive of

217   the stations in the global subnetwork. All the subnetworks vary day by day depending on the

218   station data actually available for the day considered. This network strategy has changed

219   compared to past ULR reanalyses, benefitting from the experience of the Massachusetts

220   Institute of Technology (MIT) IGS analysis centre.

221

b)

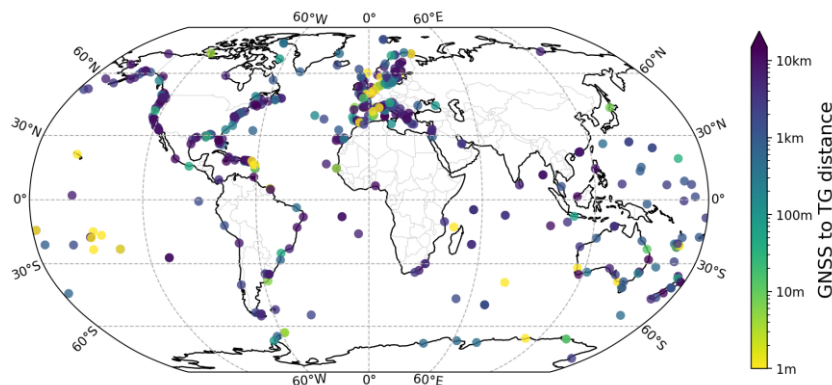



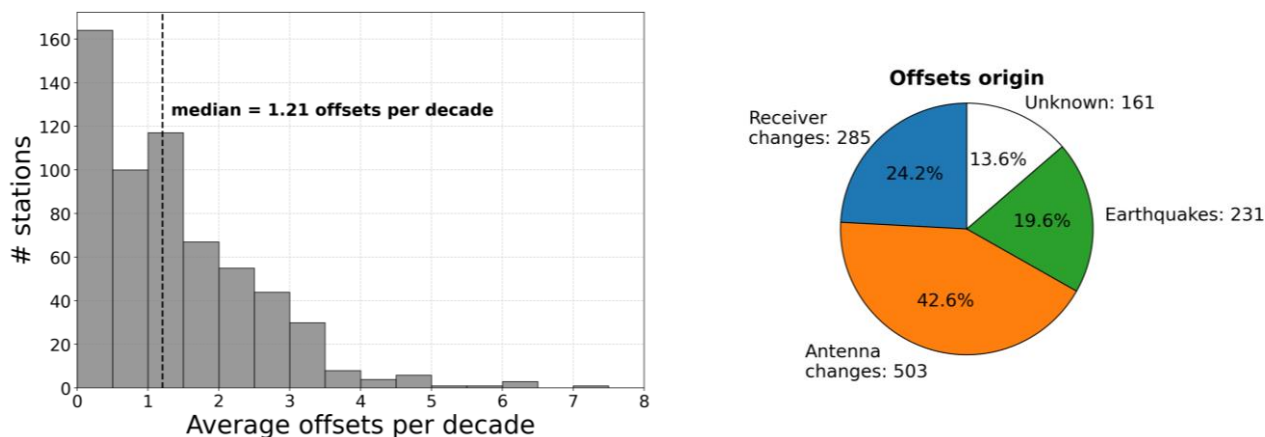
Figure 2: a) Evolution of station availability in ULR-repro3 (all in black), within 15 km and 1 km distance from a tide gauge (red and orange, respectively), and GLOSS tide gauge site (blue); b) Spatial distribution of GNSS stations and their distance to tide gauges considered in this study.

The loosely-constrained station positions and tropospheric delays for the common stations and the satellite orbital and Earth rotation parameters estimated from the subnetwork data analyses were combined using GLOBK (Herring *et al*., 2015) to obtain the daily global solutions, which include all stations available each day with their positions expressed in a common but yet undetermined terrestrial frame. These daily global solutions were then stacked into a long-term solution using the CATREF software package (Altamimi *et al*., 2018) with a time-dependent functional model that included translation, rotation and scale transformation parameters between daily and long-term frames, estimated simultaneously with the mean station positions (at the reference epoch 2010.5), annual and semi-annual signals and velocities. The scale parameters, that represent the mean height changes of all the sites, are available upon request, especially for users interested in global sea level rise.

Note that position offset discontinuities (mostly due to equipment changes and earthquakes), as well as station velocity changes and post-seismic displacements, were added to the above modelling, where appropriate. Since experienced analysts still tend to perform better than automatic methods (Gazeaux *et al*., 2013), the position offsets were identified and adopted by expert eyeball using all positioning components (i.e., including north and east components). To facilitate this task, the equipment changes reported in the GNSS station logs were considered, as well as the co-seismic displacements larger than 2 mm predicted with the earthquakes database and modelling by Métivier *et al*. (2014). When a position discontinuity was detected in a time series, the station position was estimated separately before and after the discontinuity together with the offset amplitude. The velocities before and after each position discontinuity

249 were tightly constrained (0.01 mm/yr), unless a velocity discontinuity was suspected. In the

250 latter case (less than 2% of the GNSS stations considered in ULR-repro3), no constraint was

251 applied and different velocities were estimated for each period of data around the discontinuity.

252 **Figure 3**: Average station position offsets per decade (histogram) and offsets origin (piechart)

253

254 The above procedure also included manual editing to identify (and remove) outliers as well as

255 additional non-documented position offset discontinuities. It was iterated until convergence

256 (expert eyeball). Overall, 1.2 offset discontinuities were detected per decade and per station,

257 mostly caused by equipment changes (66.8%) and earthquakes (19.6%), whereas the remaining

258 13.6% were flagged as unknown (Figure 3) due to the lack of available metadata.

259

260 The long-term terrestrial frame, in which the estimated velocities are ultimately expressed, was

261 finally aligned to the ITRF2014 (Altamimi *et al.*, 2017) by applying minimal constraints to all

262 the transformation parameters (translation, rotation, scale, and their rates) with respect to the

263 positions and velocities of a stable subset of about 35 well-distributed reference frame stations.

264 This step resulted in daily position time series expressed in the ITRF2014 frame for all (601)

265 stations considered in ULR-repro3. From this set of position time series, only stations having

266 more than three years between two consecutive position discontinuities and with data gaps not

267 exceeding 30% were retained for the next step as input (546 stations, among which 161 are

268 reference stations and 457 are nearby a tide gauge).

269

270 *2.2.3. Stochastic modelling and time-correlated noise*

271 The last step was the estimation of the parameters of interest (primarily here station velocities)

272 and their uncertainties, where both a functional and a stochastic model were adjusted to each of

273 the position time series found using the procedure described in Section 2.2.1 on a station by

274 station basis, following the equation (E1):

$$x(t) = x_{ref} + v_x(t - t_{ref}) + \sum_{i=1}^{N_0} a_i H(t - t_i) + \sum_{j=1}^{3}\left[s_j\sin\left(\frac{2\pi}{\tau_j}t\right) + c_j\cos\left(\frac{2\pi}{\tau_j}t\right)\right]$$

$$+ \sum_{d=1}^{8}\left[s_d\sin\left(\frac{2\pi}{\tau_d}t\right) + c_d\cos\left(\frac{2\pi}{\tau_d}t\right)\right] \quad\quad (E1)$$

$$+ \sum_{f=1}^{3}\left[s_f\sin\left(\frac{2\pi}{\tau_f}t\right) + c_f\cos\left(\frac{2\pi}{\tau_f}t\right)\right] + \sum_{k=1}^{N_{PSD}} PSD_k(t)$$

275 where x_{ref} is the position at the reference epoch t_{ref}, defined arbitrarily as the mid of the

276 observation period considered (2000.0-2021.0),

277 v_x is the linear velocity,

278 $H(t - t_i) = \begin{cases} 0 \ if \ t < \ t_i \\ 1 \ if \ t \geq \ t_i \end{cases}$ is the Heaviside function that multiplies the position offset a_i

279 $\tau_j = \frac{1}{j}$ is the period in years of the seasonal term j (annual, semi-annual and ter-annual),

280 $\tau_d = \frac{P_D}{365.25}$ is the period in years (P_D in days) of the draconitic signals,

281 $\tau_f = \frac{P_F}{365.25}$ is the period in years (P_F in days) of the fortnightly signals.

282
$$PSD_k(t) = \begin{cases} a_k\log\left(1 + \frac{t - t_k}{\tau_k}\right) if \ PSD \ model \ is \ log \\ a_k\left(1 - e^{-\frac{t-t_k}{\tau_k}}\right) if \ PSD \ model \ is \ exp \\ a_{1k}\log\left(1 + \frac{t - t_k}{\tau_{1k}}\right) + a_{2k}\left(1 - e^{-\frac{t-t_k}{\tau_{2k}}}\right) if \ PSD \ model \ is \ log + exp \\ a_{1k}\log\left(1 + \frac{t - t_k}{\tau_{1k}}\right) + a_{2k}\log\left(1 + \frac{t - t_k}{\tau_{2k}}\right) if \ PSD \ model \ is \ log + log \\ a_{1k}\left(1 - e^{-\frac{t-t_k}{\tau_{1k}}}\right) + a_{2k}\left(1 - e^{-\frac{t-t_k}{\tau_{2k}}}\right) if \ PSD \ model \ is \ exp + exp \end{cases}$$

283 In this step, an additional and independent time series editing was considered to eliminate

284 possibly remaining unreliable estimates from the previous step. The position estimates were

285 compared to a running monthly median. Any epoch with a position showing a difference from

286 the median exceeding five times the median absolute deviation in at least one component was

287 discarded.

288

289   The stochastic model considered a linear combination of white noise and power law process
290   (WN+PL), whose parameters (the stochastic process amplitudes and the spectral index of the
291   power-law process) were estimated using the Restricted Maximum Likelihood Estimation
292   method (Patterson & Thompson, 1971; Koch, 1986; Gobron *et al*., 2022). To obtain realistic
293   stochastic parameter estimates, non-tidal atmospheric loading (NTAL) displacements were also
294   subtracted from the position time series prior to this adjustment, following the recommendation
295   of Gobron *et al*. (2021). These NTAL displacements were obtained from the Earth System
296   Modelling team of the German Research Center for Geosciences in Potsdam (Dill and Dobslaw,
297   2013).

298

299   The functional model included an intercept, a linear trend (velocity), the position offsets
300   identified in the previous step, three seasonal terms (annual, semiannual, and terannual),
301   periodic terms at the first eight harmonics of the GPS draconitic year (351.4 days; Ray et al.,
302   2008), and three fortnightly terms with periods of 13.62, 14.19 and 14.76 days (Penna and
303   Stewart, 2003; Amiri-Simkooei, 2013). The parameters of this functional model, and their
304   uncertainties, were estimated using the weighted least squares estimator with the inverse of the
305   estimated WN+PL model covariance matrix as weight matrix. During the observation time
306   span, some stations (44) recorded significant co-seismic offsets and transient post-seismic
307   signals, in which case the modeling was further extended to include velocity changes, and
308   logarithmic or exponential decay functions according to the observed time evolution.

309

2.3 Estimates of vertical land motion

2.3.1 Position time series & Vertical velocities

312   The GNSS products of primary interest for sea level studies are the station position time series
313   and vertical velocity estimates as underlined in the founding charter of the IGS working group
314   "GNSS Tide Gauge Benchmark Monitoring" (Schöne *et al*., 2009) and later on in the
315   implementation plan of the GLOSS programme (IOC, 2012). In the following, we focus on the
316   vertical positioning component. However, the horizontal components are made available too,
317   and can be useful for other geophysical applications. Figure 4 shows the ULR-repro3 vertical
318   velocity field, and the corresponding uncertainties. This GNSS velocity field ultimately consists
319   of 546 stations, among which 457 are within 15 km from a tide gauge. This number decreases
320   to 135 for stations less than 1 km from a tide gauge. Note that the stations inland are IGS
321   reference frame stations (section 2.1).

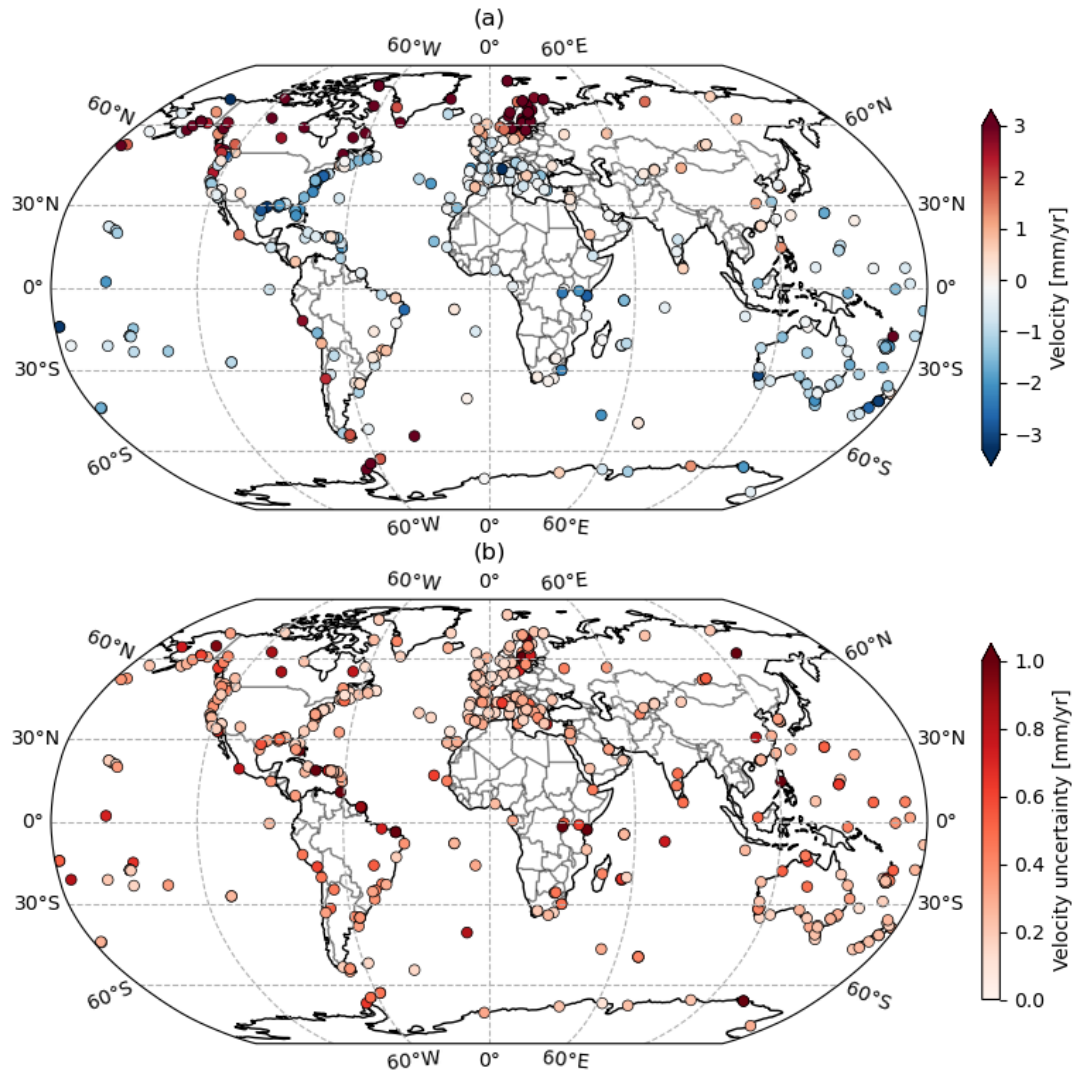



Figure 4: Vertical velocities (a), and associated uncertainties (b), estimated for the stations with at least 3 years of continuous measurement (see text).

Overall, the geographical patterns observed in Figure 4.a are consistent with known geophysical processes such as uplift in the northern latitudes of Europe and North America due to Glacial Isostatic Adjustment (GIA), or subsidence along the northern coastlines of the Gulf of Mexico primarily driven by ground water depletion and sediment compaction, also observed in previous and independent GNSS analysis results (e.g., Blewitt *et al*., 2018; Hammond *et al*., 2021). The eight stations with velocity discontinuities are not plotted in Figure 4.

2.3.2 Data availability

The ULR-repro3 products are available from the online Digital Object Identifier (DOI) landing page (https://doi.org/10.26166/sonel_ulr7a; Gravelle et al., 2022). That is, the station position

336 time series together with the estimated velocities for all positioning components (north, east,
337 and up). These products are hosted at the SONEL scientific service, which serves as data
338 assembly centre dedicated to GNSS data at tide gauges (Wöppelmann *et al.*, 2021) for the
339 international GLOSS programme (IOC, 2012). As a UNESCO-related programme, the service
340 complies with the UNESCO open access data policy (i.e., the data sets are available free of
341 charge without any barriers) and strives towards providing the highest international standards,
342 in particular in terms of long-term availability and permanent access. Note that the ULR-repro3
343 reanalysis yielded other parameter estimates, which can be of interest to other geophysical
344 applications (e.g., station position offsets related to earthquakes and seasonal signals). These
345 are also made available via SONEL.

346

347 ## 3 Products quality

348 ## 3.1 Average time correlation properties

349 Previous studies have documented the presence of both power-law noise (PL) and white noise
350 (WN) in GNSS station position time series (e.g., Williams *et al.*, 2004; Santamaria-Gomez *et*
351 *al.*, 2011; Gobron *et al.*, 2021; Santamaria-Gomez & Ray, 2021). Such time-correlated
352 properties are also evidenced by Figure 5 for ULR-repro3, where Lomb-Scargle periodograms
353 of all detrended station position time series were averaged. As highlighted by the red curve in
354 Figure 5 (in logarithmic scales), the power-law process induces the negative trend at low
355 frequencies (that is, a spectral power $\propto 1/f^{\alpha}$), whereas the white noise causes the flattening at
356 high frequencies. This flattening is especially visible above 22.8 cpy, where the power of the
357 white noise exceeds that of the power-law process. Note that, on the one hand, the background
358 shape of the average periodogram (Figure 5) is accounted for by the WN+PL stochastic model,
359 presented in section 2.2.3, and adjusted to each position time series. On the other hand, the
360 functional model accounts for the spectral peaks marked by coloured vertical lines, which
361 correspond to well-identified periodic oscillations common to most GPS solutions (Ray *et al.*,
362 2008).

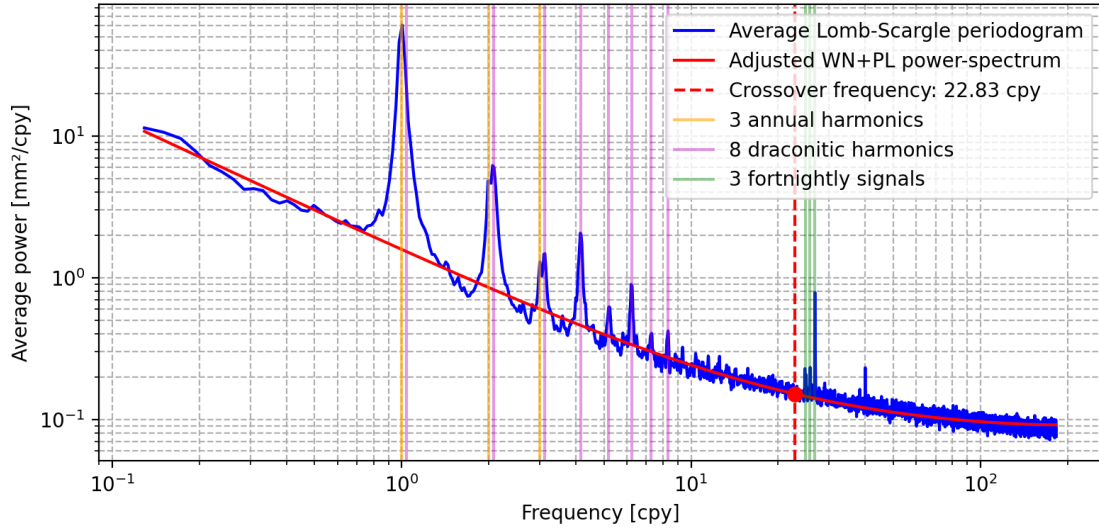



Figure 5: Average Lomb-Scargle periodogram for the ULR-repro3 detrended vertical position time series corrected for NTAL displacements (frequency unit is cycles per year or cpy).

3.2 Stochastic properties of position time series

The periodogram in Figure 5 does not provide information about the properties of individual stations. By contrast, Figure 6 highlights the stochastic process amplitudes and the spectral index of the WN+PL stochastic models adjusted to the individual vertical position time series.

The median value of the spectral indices is -0.93, that is, close to -1.00, which confirms the prevalence of a flicker-like noise in the low frequency band. The spectral indices show no clear latitudinal dependency (Figure 6.g-h). Since power-law amplitudes depend on the spectral index values, they were transformed into a modified empirical standard deviation (Gobron *et al.*, 2021), expressed in mm, enabling a more rigorous comparison between noise amplitudes and Root Mean Squared Errors (RMSE) values. No latitudinal dependency is revealed in Figure 6.e. By contrast, the white noise amplitudes show largest values within the tropical band (Figure 6.c), and lower values at high latitude, but are mostly non-zero thanks to the NTAL corrections (Gobron *et al.*, 2021). Logically, this pattern also appears in the RMSE (Figure 6.a), as it quantifies the combined influence of the white noise and power-law processes.

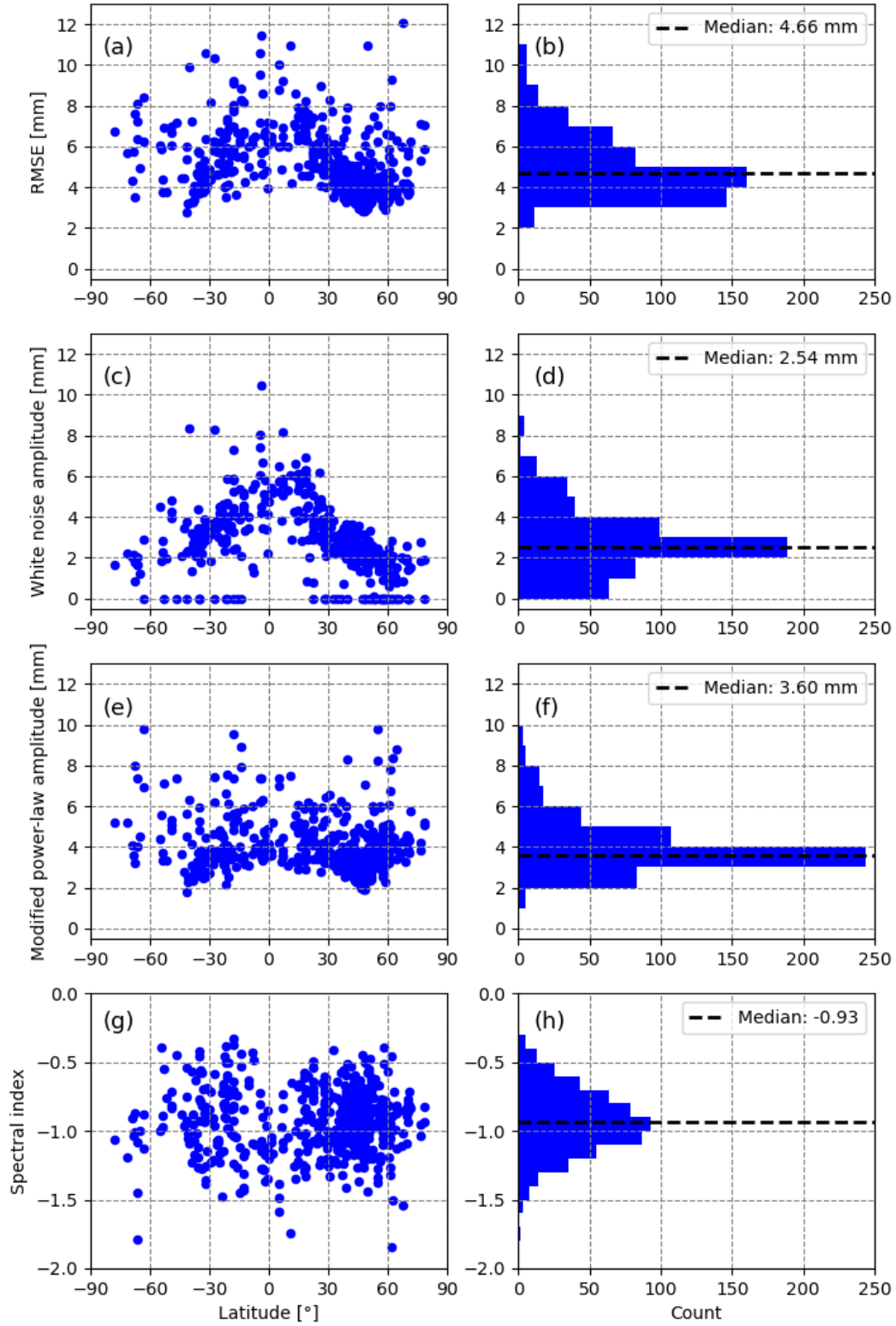



Figure 6: Vertical position time series RMSE (a) and (b), white noise amplitudes (c) and (d); modified power-law amplitudes (e) and (f); and spectral indices (g) and (h). See text for details.

3.3 Vertical velocity uncertainties

An important consequence of temporally correlated noise in time series of GNSS positions is its impact on the uncertainties of GNSS-derived velocities, which can be largely underestimated, up to a factor of ten (Williams *et al*., 2004), if the temporal correlations are ignored. Figure 7 shows the distribution of the vertical velocity uncertainties obtained for the ULR-repro3 stations considering the stochastic properties estimated above. Their median value is 0.27 mm/yr with 83% of the stations displaying a vertical velocity uncertainty below 0.5 mm/yr. The colouring in Figure 7.a indicates that the largest velocity uncertainties typically correspond to the stations with the shortest records.

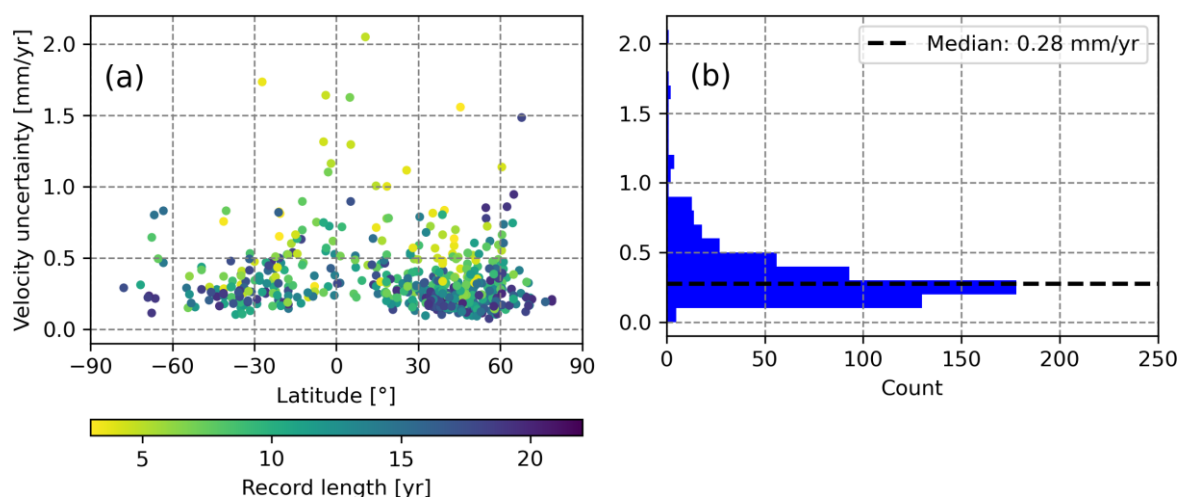



Figure 7: Vertical velocity uncertainties as a function of the geographical latitude with colour corresponding to the record length (a) and histogram (b).

3.4 Highlights *wrt* previous ULR reanalysis

To appraise the progress accomplished with the ULR-repro3 reanalysis, the position time series from the previous reanalysis (Santamaria-Gomez *et al*., 2017) were retrieved at SONEL, and the same processing (last step in section 2) was applied for a rigorous comparison (same non-tidal atmospheric loading corrections, and same functional and stochastic models). This comparison involved the 251 common stations. Figure 8 indicates a substantial reduction of 28% in the median vertical velocity uncertainties, from 0.35 mm/yr down to 0.25 mm/yr (ULR-repro3), which is below the uncertainty threshold reported by Griffiths and Ray (2016) using simulations to investigate the effect of position offsets and record lengthening. However, it is worth noting that the community interested in monitoring vertical land motion at tide gauges tend to limit changes in GNSS equipment to the strictly unavoidable (failure, destruction, etc.)

as recommended by the IGS-related working group (Schöne *et al.*, 2009). As a result, the average return period of offsets is about four years longer here (Figure 3) than observed for the entire set of stations contributing to the IGS repro3 campaign (Rebischung *et al.*, 2021), hence partly explaining the improved velocity uncertainties observed with ULR-repro3 reanalysis.

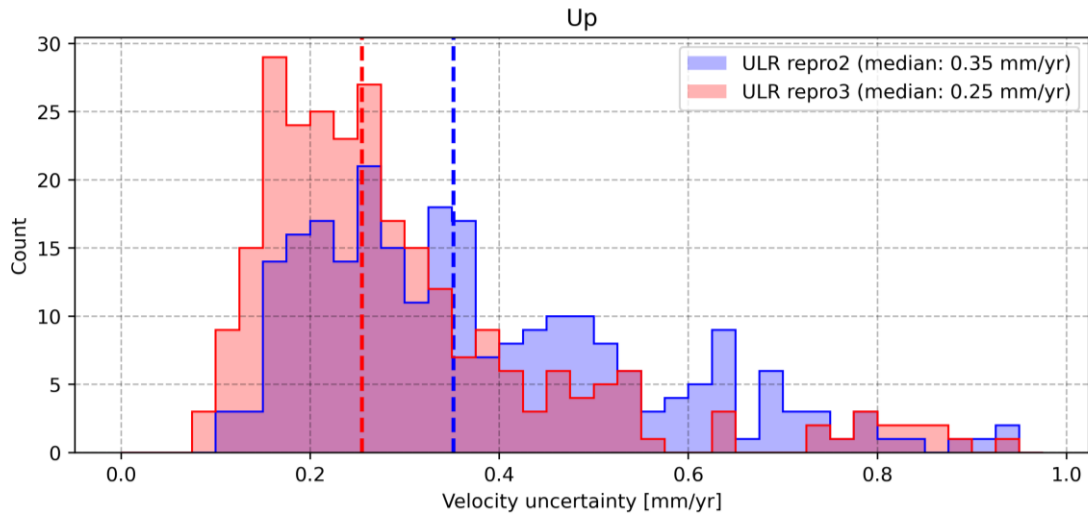



Figure 8: Vertical velocity uncertainties for ULR-repro3 wrt the previous ULR solution based on the 251 common stations. The vertical dashed lines correspond to the medians.

The marked improvement in the quality of ULR-repro3 products can also be appraised from the RMSE position residuals (median value of 5.3 mm down to 4.9 mm now) and the amplitude of white noise (from 3.4 mm to 2.8 mm), whereas the power-law amplitude and spectral index remained equivalent (3.8 mm and -0.93, respectively).

In addition to the progress achieved over the previous ULR solution, the quality of the ULR-repro3 solution was also confirmed by the comparisons undertaken within the IGS reanalysis campaign, showing that the noise content in ULR-repro3 is comparable to that of most of the other contributing solutions and analysis centres (Rebischung *et al*., 2021).

4 Concluding remarks

This paper has presented the latest GNSS data reanalysis carried out by the ULR group within the international IGS framework, yielding time series of position estimates to measure the vertical land motion nearby tide gauges. It includes an increased number of GNSS stations with an extended time span. Along with the velocity estimates, their uncertainties were obtained by modelling the temporally correlated noise processes inherent in the data, after correcting the position time series for non-tidal atmospheric loading displacements, as recommended by Gobron *et al*. (2021). Overall, the comparisons indicate that ULR-repro3 represents a marked

437 improvement in its product quality over the previous reanalysis, with a notable reduction in

438 median vertical velocity uncertainty by 28% (Figure 8).

439 An interesting perspective will be to examine the differences with global reanalyses obtained

440 by other groups complying with the latest IGS standards, but using different analyst choices at

441 any of the major GNSS processing steps described in section 2 (e.g., Blewitt *et al.*, 2016;

442 Männel *et al.*, 2022). A related perspective will be to address the issue of which reanalysis is

443 best for the non-expert sea level user, if any (Ballu *et al.*, 2019). In this respect, the Commission

444 on Mean Sea Level and Tides from the International Association for the Physical Sciences of

445 the Oceans (IAPSO) could provide a stimulating framework to gather experts and users

446 worldwide, and reflect on the issue posed by multiple high-quality GNSS reanalyses, as IAPSO

447 did nearly thirty years ago when the issue of geodetic fixing of tide gauge benchmarks was

448 considered with the advances of space geodesy (Carter *et al.*, 1994).

449

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459

460 **Author contributions**

461 The project was defined by MGr and GW as a contribution to the third reprocessing ('repro3')

462 campaign of the International GNSS Service (IGS). MGr processed the GPS data with support

463 from TH (GAMIT/GLOBK software packages, network design, and strategy for subnetwork

464 design and orbit adjustment), ZA (CATREF software and reference frame alignment), PR

465 (product quality assessment within 'repro3'), and MGu (strategic use of the high-performance

466 computing center). KG prepared the NTAL corrections, assessed the stochastic properties of

467 the time series and produced the final velocity field. All authors contributed to the analysis and

468 discussion of the results. The first manuscript draft was written by GW. All authors contributed

469 to the subsequent versions, and approved the final manuscript.

470

Competing interests

The contact author has declared that none of the authors has any competing interests.

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