Answers to Reviewer #2:

The paper describes the updated SSS- SMOS derived data set. Inversion algorithm, comparison with other products, including the one previously developed by the same consortium, and partial data validation are described. The paper is clear and the description of process used to move from data to product is appropriate. The main advantage of the new product is its finer resolution which could be relevant for oceanographic processes description. The paper is almost ready for publication except for some minor suggestions which can improve its readability.

Thank you very much for all your comments and suggestions. We think the paper has improved a lot after integrating them in the manuscript.

Lines 14-15 : there is a repetition here. Please check.

Corrected.

Line 16.19 : you can improve the readability of manuscript here by merging/reformulating the different short sentences.

The sentence has been changed to:

"The number of in situ surface salinity measurements is, therefore, very scarce, and especially in the central Arctic Ocean, since it is a region with extreme weather conditions and sea ice forces are strong enough to destroy the in situ measurements infrastructures (like Argo floats, moorings, or gliders). "

Lines 20-21: sentence "...better monitoring the observed changes in the freshwater fluxes". Please add reference for the observed changes which, in my understanding, differs from L-band radiometry.

### Changed to:

"The use of L-band radiometry to fill the observational salinity gaps at high latitudes could be very useful to better monitor the observed changes in the freshwater fluxes (Fournier et al. 2020)."

The reference is also added.

Fournier, S., et al., (2020). Sea surface salinity as a proxy for arctic ocean freshwater changes. JGR: Oceans

-Line 28-29 : "Whilst L-band frequency is the region of the electromagnetic spectrum offering the most sensitivity to salinity variations, it decreases rapidly in cold waters " this is not true. Recent paper (e.g. 10.1109/TGRS.2021.3101962) proves that other frequencies work better and efforts are made to promote it from space ( DOI: 10.1109/JSTARS.2021.3073286)

Yes we added the following sentence:

"The SMOS frequency band (1.43GHz, L-band) is an optimum band to measure salinity, since this electromagnetic region is protected against human electromagnetic emissions, while the sensitivity to salinity is high."

And modified the cited one by this one:

"Whilst the sensitivity to salinity is high at L-band, the sensitivity decreases rapidly in cold waters."

-Line 31-32 – LSC: you can simply mention that the problem is due to the large footprint on the ground (interferometer is obviously worst).

We have changed the sentence accordingly.

-Line 58 : could you provide an estimate of error introduced by the interpolation process?

This is not possible in this case. The reliability of the nearest-neighbor interpolation depends on the spatial variability of the original ECMWF data.

-Line 67 – the sentence "The SSS and SST are converted to TB "sounds a bit strange, I guess that you meant that SSS and SST are used as inputs in an e.m model to generate simulated Tb values.

Yes, the referee is right. The sentence has been changed.

"The SSS and SST are used as inputs of the Meissner and Wentz dielectric constant model to obtain TB (Meissner & Wentz, 2004, 2012). The TB obtained is considered the reference value to perform the spatial bias correction of the measured TB."

-Line 69\_ you mention that data "generated from measurements of the 2005-2017 period" are used as reference but SMOS data refers to 2011-2019 period. Did you evaluate if there is an impact on the obtained the results if the same overlapping period is used?

It is not possible to have the same overlapping period because WOA is generated only for the complete 2005-2017 period while SMOS has no data prior to 2010 (2011 in our case).

### -Line 90: could you add an accuracy estimate for Tara data?

The Tara expedition in the Arctic used a thermosalinograph (TSG) Seabird SB45 to measure the conductivity and temperature and then the salinity is computed. This sensor has an accuracy of the conductivity of  $\pm$  0.0003 S/m, which represents the same magnitude of salinity accuracy of 0.0003 PSU.

Reference: https://www.seabird.com/sbe45-microtsg-thermosalinograph/product?id=54627900541

# -Line 104-105: could you estimate/quantifying the differences in considering 64x64 instead of 128x128 point? You mention "without loss of information/resolution ".

A division of the antenna hexagonal grid in 64x64 cells provides 4096 grid points. This is enough to provide the Tb values because the number of visibilities from which snapshots are derived by a linear transformation is 2791. The hexagonal grid must be constructed as 2nx2n grid and n<6 undersamples the image. This fact has been explained in the new text:

"This resolution in the antenna level results in 4096 grid points being enough to provide the TB values because the number of visibilities from which snapshots are derived by a linear transformation is 2791. This choice allows us to reduce the computational time without loss of information/resolution."

# -Line 119-120; is not clear if the ionosphere correction is applied. Since 1st Stokes parameter is used for the inversion

Yes. It is applied. This contribution is accounted for in figure 1.

-Line 133-135: if I understood correctly you use, as reference, the SSS value obtained from the WOA instead to the one obtained from SMOS (average value). If so, which is the estimated differences between these values? Could you provide an example for some specific regions where the coast contamination is /or isn't relevant?

In this new version of the Arctic salinity product, the bias is corrected in TB and not in SSS. In this case the reference is the TB obtained from SSS and SST from WOA. The reference TB is computed from WOA SSS and SST using the Meissner and Wentz dielectric model. Then, we obtain TB values for each latitude, longitude, satellite orientation and position in the antenna reference frame (the new reference). The correction depends of a wide variety of factors but can attain values as high as 10K depending on the position in the antenna reference frame or the distance to the coast. Figures 19 and 20 from ATBD document (http://dx.doi.org/10.13140/RG.2.2.12195.58401) show the differences for 4 points of the field of view for ascending and descending cases (reproduced here).

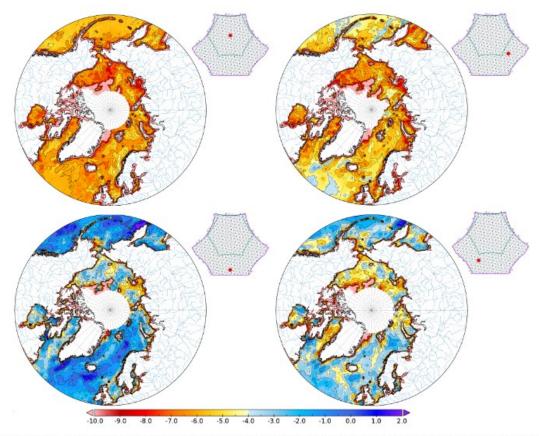


Figure 19: Correction to be applied to measured half first Stokes parameter in 4 difference FOV positions for ascending passes (equation 20)

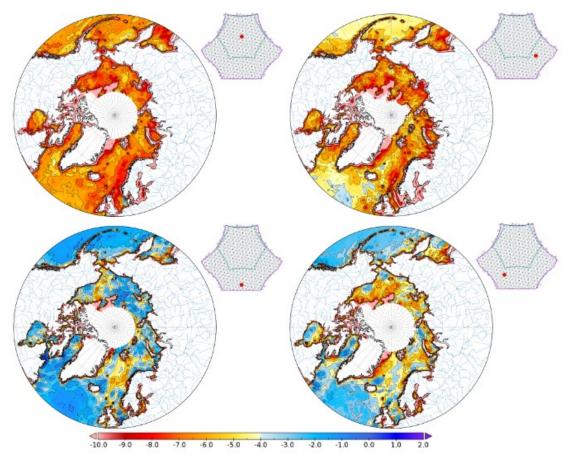


Figure 20: Correction to be applied to measured half first Stokes parameter in 4 difference FOV positions for descending passes (equation 20)

-Line 173 : the sentence "Only latitudes above 50â¦N are considered" can be eliminated since it is repetition of line 159.

The sentence has been eliminated.

-Line 189- For the minimization did you use different approaches? For instance, did you check if the introduction of a regularization term could be beneficial?

The minimization used is a non bayesian method and therefore it doesn' have any regularization term. We haven't tested any other minimization algorithm for this Arctic product.

# -Line 203 – 206 why using 100 , 7 and 2 as criteria? Could you better justify it? (i.e. Why not 90 or 110?)

The number of the minimum number of measures to create the SMOS-based climatology was taken to 100 by simply testing different values. No significant differences are obtained using 90 or 110... The value is based on the minimum required measures to obtain a statistically significant TB distribution

without holes. The resulting distributions should be adequate to obtain their moments and this is not reliable with a low number of measures. Moreover, points with a low number of TB measures in 9 years are not certainly reliables.

The values adopted for the maximum absolute kurtosis (7) and absolute skewness (2) may be used as reference values for determining substantial non-normality of the distribution. West et al 1995, recommend these values as the values for which the distribution begins to depart substantially from normality.

[West et al (1995)] West SG, Finch JF, Curran PJ. Structural equation models with nonnormal variables: problems and remedies. In: Hoyle RH, editor. Structural equation modeling: Concepts, issues and applications. Newbery Park, CA: Sage; 1995. pp. 56–75.

#### -Line 230-233: Also here : could you better explain how the thresholds were selected?

These thresholds have been selected purely by trial and error. However, they are not too restrictive: salinity must be positive and less than 50 psu, for usual salinity values we don't expect large differences between the retrieved value and WOA value, and for low salinity values we relax the value to take into account possible rivers discharges and ice melting (WOA does not account for transient states)

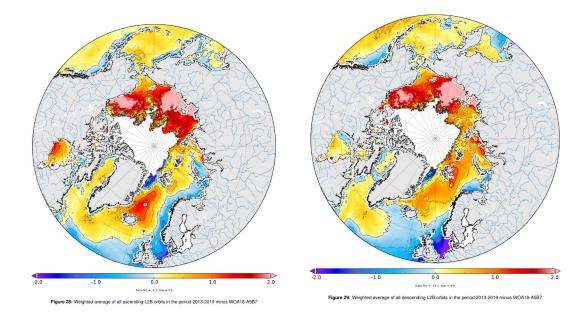
-line 260: The 12 psu bias has, in my view, severe implication. It implies that the retrieval largely overestimates the retrieved SSS besides the numerous procedures, averaging, de-bias which were conducted to derive it. Did you have an explanation for the bias? There is a problem of representativeness of SSS retrieved by SMOS and what provided by HYCOM? Or there is an absolute error on HYCOM only as bias but it didn't affect the temporal variability? At the end you plan to use it for the temporal correction.

There is no problem with HYCOM (or at least its use in the temporal correction is not the cause of this bias). The main cause is that WOA2018 is assuming a Gaussian distribution of SST and SSS whereas the first stokes distributions provided by SMOS are generally positively skewed (a more detailed explanation is provided in section 2.7 of the manuscript "Correction of the residual spatial bias"). The temporal correction is performed before the correction of residual spatial bias due to computational optimization requirements, requiring this high initial step to speed up the convergence.

### -line 276: how much the number differs from zero? This could be a useful information for the reader.

The weighted average of all L2B orbits in the 2013-2019 period minus the value provided by WOA ranges between -10 and 10 psu but mainly between -2 and 2 psu. The values differ a lot between the

Arctic zones being smaller in the open ocean and larger in the North Sea (negative), in the Beaufort Sea (positive) and the East Siberian Sea (positive) . [See following figures]



This information, not the figures, has been included in the text.

## -figure 5: why the error is only represented for radiometric uncertainty? you have different factors that contribute to the error computation. This is bit reductive

Yes, we agree that this is only a portion of the error, but the radiometric error is the only one that can be computed with an acceptable degree of reliability. Moreover, it is the only one that depends on the instrument and not on the geophysical models.

-Argo validation: not clear to me why BEC V2.0 data provides better results in 2011 -2012. If SMOS is affected by RFI (as the authors mention) this impact on all the products. Moreover, for BECV3.1 you develop an approach which is devoted to mitigate RFI effects.

This is mainly because in v2.0 the bias was corrected using ARGO data. Therefore, it is expected a better correspondence with ARGO data. However, in v3.1 the approach was not focus on mitigating RFI effects, but to improve the inversion at low SSS values, and therefore improve the spatial resolution.

-Tara Validation: from table it seems to me that the affirmation "Arctic+ v3.1 product, better than the previous BEC v2.0 product in most of the seas" is questionable. I see a clear advantage in two cases only (Kara and Beaufort).

Yes, the reviewer is right! We have specified on the text when v3.1 better than v2.0 with this sentence.

"Matchups with TARA are different results depending on the sub-basin. Arctic+ v3.1 product have less RMSD than BEC v2.0 product for three sub-basins (Kara, East Siberia and Beaufort seas) and also for the global value."

-Spectral Analysis : the difference between SMAP and BECV3.1 seems to me very small in the figure then my conclusion is that both method provide similar results. It is correct?

We have added this sentence to clarify:

"Moreover, Arctic SSS v3.1 resolves smaller scales than SMAP JPL in Laptev and Bering regions, where SMAP JPL exhibits a flattening in the PDS slope below 50 km wavelength."

-Lie 427: while I recognize that validation for 3 days product require additional effort, although it could be very interesting for potential users, I believe that validation at 18 days should be simple and can be easily implemented.

We agree, that the validation of the two additional products (3 days and 19 days) would be interesting, but this is out of scope of the project Arctic + Salinity and of this paper. However, this is something we have in our plans to do.