Correcting Thornthwaite potential evapotranspiration using a global grid of local coefficients to support temperature-based estimations of reference evapotranspiration and aridity indices

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Abstract. Thornthwaite's formula is globally an optimum candidate for large scale applications of potential evapotranspiration and aridity assessment at different climates and landscapes since it has the lower data requirements compared to other methods and especially from the ASCE-standardized reference evapotranspiration (former FAO-56), which is the most data demanding method and is commonly used as benchmark method. The aim of the study is to develop a global database of local coefficients for correcting the formula of monthly Thornthwaite potential evapotranspiration (E_p) using as benchmark the ASCE-standardized reference evapotranspiration method (E_r). The validity of the database will be verified by testing the hypothesis that a local correction coefficient, which integrates the local mean effect of wind speed, humidity and solar radiation, can improve the performance of the original Thornthwaite formula. The database of local correction coefficients was developed using global gridded temperature, rainfall and E_r data of the period 1950-2000 at 30 arc-sec resolution (~1 km at equator) from freely available climate geodatabases. The correction coefficients were produced as partial weighted averages of monthly E_r/E_p ratios by setting the ratios' weight according to the monthly E_r magnitude and by excluding colder months with monthly values of E_r or E_p <45 mm month⁻¹ because their ratio becomes highly unstable for low temperatures. The validation of the correction coefficients was made using raw data from 525 stations of Europe, California-USA and Australia including data up to 2020. The validation procedure showed that the corrected Thornthwaite formula E_{ps} using local coefficients led to a reduction of RMSE from 37.2 to 30.0 mm m⁻¹ for monthly and from 388.8 to 174.8 mm y⁻¹ for annual step estimations compared to E_p using as benchmark the values of E_r method. The corrected E_{ps} and the original E_p Thornthwaite formulas were also evaluated by their use in Thornthwaite and UNEP (United Nations Environment Program) aridity indices using as benchmark the respective indices estimated by E_r. The analysis was made using the validation data of the stations and the results showed that the correction of Thornthwaite formula using local coefficients increased the accuracy of detecting identical aridity classes with E_r from 63% to 76% for the case of Thornthwaite classification, and from 76% to 93% for the case of UNEP classification. The performance of both aridity indices using the corrected formula was extremely improved in the case of non-humid classes. The global database of local correction factors can support applications of reference evapotranspiration and aridity indices assessment with the minimum data requirements (i.e. temperature) for locations where climatic data are limited. The global

grids of local correction coefficients for Thornthwaite formula produced in this study are archived in PANGAEA database and can be assessed using the following link: https://doi.pangaea.de/10.1594/PANGAEA.932638 (Aschonitis et al., 2021).

1 Introduction

The assessment of potential or reference evapotranspiration is among the most important components for many hydro-climatic applications such as irrigation design and management, water balance assessment studies, and assessment of aridity classification and drought indices (Weiß and Menzel, 2008; Wang and Dickinson, 2012; McHanon, 2013; Aschonitis et al., 2017).

Such applications, and especially applications of aridity classification and drought indices (UNEP 1997; Thornthwaite, 1948; Palmer, 1965; Holdridge, 1967; Beguería et al., 2014) that are usually employed at large scales, require estimations of potential or reference evapotranspiration of respective scale. The major problem in such applications is not only the limited availability of stations per se but also the limitation of many stations to provide data for a complete set of parameters (i.e. precipitation, temperature, solar radiation, wind speed, humidity). A complete set of climate parameters is prerequisite for accurate estimations of potential or reference evapotranspiration using integrated methods such as these of Penman (1948), Shuttleworth, 1993; Allen et al. (1998), Allen et al. (2005), and others which are expressions of energy balance. Unfortunately, large scale applications suffer from these limitations and the common solution is to use temperature-based formulas (Thornthwaite, 1948; McCloud, 1955; Hamon 1961, 1963; Baier and Robertson, 1965; Malmström, 1969; Hargreaves et al., 1982; Camargo et al., 1999; Droogers and Allen 2002; Pereira and Pruitt 2004; Oudin et al., 2004; Trajkovic 2005, 2007; Trajkovic and Kolakovic, 2009a,b; Almorox et al., 2015; Aschonitis et al. 2017; Sanikhani et al. 2019; Quej et al., 2019; Trajkovic et al., 2020). However, extensive literature shows that temperature-based formulas are inherently of low performance because temperature cannot describe properly the evaporative flux, while various studies have shown differences among the Penman–Monteith-based and temperature-based potential evapotranspiration assessments such as the one of Thornthwaite (1948), which is the most popular in aridity and drought indices applications (Sheffield et al., 2012; Dai, 2013; van der Schrier et al., 2013; Trenberth et al., 2014; Yuan and Quiring, 2014; Zhang et al., 2015; Asadi Zarch et al., 2015).

The formula of Thornthwaite (1948) was firstly proposed as internal part of the respective Thornthwaite aridity/humidity index and it was calibrated based on measured monthly evapotranspiration from some well-watered grass-covered lysimeters in the eastern and central USA (Willmott et al.1985; Van Der Schrier et al., 2011). The specific formula overestimates the potential evapotranspiration in humid climates and underestimates it in arid climates (Pereira and Pruitt, 2004; Castaneda and Rao, 2005; Trajkovic and Kolakovic, 2009), and thus, a number of efforts have been made to amend the parameters or constants of the empirical formula to adapt it to various geographical zones (Jain and Sinai, 1985; Pereira and Pruitt, 2004; Castaneda and Rao, 2005; Zhang et al., 2008; Bakundukize et al., 2011; Yang et al., 2017). Indicative modifications were proposed by Willmott et al. (1985) using an additional parametrization presented for mean monthly temperature above 26.5 ℃ and an adjustment for variable daylight and month lengths. Camargo et al. (1999) substituted the

mean monthly temperature by another factor called effective temperature considering the amplitude between maximum and minimum temperature. Jain and Sinai (1985) modified the constant in the general formula based on the min-max range of the annual mean air temperature to calculate the evapotranspiration for semiarid conditions. Pereira and Pruitt (2004) proposed an adaptation of the Thornthwaite scheme to estimate the daily reference evapotranspiration on two contrasting environments in USA and Brazil. Castaneda and Rao (2005) recalibrated the coefficient of the general formula based on estimations of potential evapotranspiration using the FAO Penman-Monteith method in southern California while Bautista et al. (2009) performed a similar procedure for stations located in coastal semi-arid climate and inland tropical subhumid climate regions of México. Zhang et al. (2008) used a modified formula to estimate the actual evapotranspiration in cropland, shrubland and forest located in the subalpine region of southwestern China. Bakundukize et al. (2011) used two modifications and of the original Thornthwaite method to for groundwater recharge estimations in the inter-lacustrine zone of East Africa. Yang et al. (2017) presented a method to quantitatively identify the differences in the spatiotemporal variabilities of global drylands between the Thornthwaite and Penman–Monteith parameterizations. Trajkovic et al. (2019; 2020) provided successful corrections of the original formula based on the FAO Penman-Monteith method for stations located in Hungary, Serbia, Romania, Croatia and Slovakia.

The last years, advanced interpolation techniques, climatic models and other methods have achieved to generate gridded datasets of various climatic parameters (Hijmans et al., 2005; Sheffield et al., 2006; Osborn and Jones, 2014; Harris et al., 2014; Brinckmann et al., 2016; Liu et al. 2020) facilitating attempts to develop global maps of potential/reference evapotranspiration and to investigate the accuracy of formulas of reduced parameters versus benchmark methods at global scale (Droogers and Allen, 2002; Weiß and Menzel, 2008; Zomer et al., 2008; Aschonitis et al., 2017). A similar attempt is performed in this study aiming to develop a global database of local correction coefficients for the original Thornthwaite formula. This attempt aims that will better to support all hydro-climatic applications and especially specifically to support large scale applications of aridity indices, which are highly prone to data limitations are highly affected by the use of different potential evapotranspiration methods (Proutsos et al., 2021). The hypothesis that is tested in this work is that a global grid of local correction coefficients that integrates the local mean effects of wind speed, humidity and solar radiation can improve the performance of the original potential evapotranspiration formula of Thornthwaite formula and toby converting it at the same time to a formula of reference evapotranspiration for short reference crop based on the FAO Penman-Monteith concept.

2 Data and Methods

2.1 Data

The methodological steps of the next sections are used to develop a global map of local coefficients for correcting the original potential evapotranspiration formula of Thornthwaite following a calibration and a validation procedure.

The derivation/calibration procedure was performed at global scale using global gridded data from two databases. The first database of Hijmans et al. (2005) provides gridded data of mean monthly precipitation P and mean monthly temperature

95   T of the period 1950-2000 (WorldClim version 1.2) at 30 arc-sec spatial resolution (~1×1 km at the equator) (Fig.1a,b). The second database is of Aschonitis et al. (2017), which provides gridded data of mean monthly reference evapotranspiration E_r of the period 1950-2000 at five different resolutions (30 arc-sec, 2.5 arc-min, 5 arc-min, 10 arc-min and 0.5 deg) (Fig.1c). The method used for estimating E_r is the ASCE-standardized method (former FAO-56 Penman-Monteith), which estimates reference evapotranspiration for short, clipped grass (Allen et al., 2005). The database of E_r (Aschonitis et al., 2017) was built

100   using the temperature from the first database of Hijmans et al. (2005) at 30 arc-sec resolution and for this reason the two gridded databases are compatible.

[FIGURE 1]

105   The validation procedure was performed using raw data of stations from three different databases. The first database is the CIMIS database (California Irrigation Management System – CIMIS, http://www.cimis.water.ca.gov), which includes stations from California-USA and it was selected because it provides a dense and descriptive network of stations for a specific region that combines semi-arid/temperate coastal, plain, mountain environments. In total 60 stations (Fig.2a) were used from CIMIS database that have at least 15 years of observations with a significant part of their observations after 2000. The second

110   database is the AGBM database (Australian Government – Bureau of Meteorology, http://www.bom.gov.au). This database includes many stations from Australia and was selected because the station's network covers a large territory with a large variety of climate classes from desert to tropical climate. The selection of stations was performed in order to cover all the possible existing Köppen-Geiger climatic types (Peel et al., 2007) and altitude ranges that exist in the Australian territory. In total 80 stations were used (Fig.2b), that have at least 15 years of observations with a significant part of their observations after

115   2000. The third database is the ECAD database (European Climate Assessment & Database, https://www.ecad.eu). This database is a network that contains more than 20,000 stations throughout Europe and provides daily observations of climatological parameters. In this study, a final number of 385 stations (Fig.2c) was selected from this database because they contained complete data of precipitation, temperature, solar radiation, relative humidity and wind speed for a period of at least 20 years with a significant part of their observations after 2000. Some additional stations from the three databases (CIMIS,

120   AGBM, ECAD), which do not have at least 15 years of observations, were selected due to their special climate Köppen-Geiger class or the high altitude of their location). The total final number of stations used in the study from the three databases is 525 and their full description is given in Table S1 of the Supplementary material.

[FIGURE 2]

2.2 Derivation and validation of Thornthwaite correction coefficients for short reference crop based on ASCE-
125 **standardized method**

The monthly potential evapotranspiration E_p using the Thornthwaite (1948) method after its adjustment for variable daylight and month lengths (Willmott et al., 1985) is estimated as follows:

$$E_p = 16 \cdot \left(\frac{10 \cdot T_{mean}}{J} \right)^a \cdot \frac{N \cdot n}{365} \tag{1}$$

$$J = \sum_{i=1}^{12} j_i$$

$$j_i = \left(\frac{T_{mean,\,i}}{5} \right)^{1.514} \tag{2a,b,c}$$

$$\alpha = (6.75 \cdot 10^{-7}) \cdot J^3 - (7.71 \cdot 10^{-5}) \cdot J^2 + (1.79 \cdot 10^{-2}) \cdot J + 0.492$$

$$N = \frac{24}{\pi} \cdot \omega_s$$

$$\omega_s = \frac{\pi}{2} - \arctan \left[\frac{-\tan(\varphi) \cdot \tan(\delta)}{X^{0.5}} \right]$$

$$\text{where: } X = 1 - [\tan(\varphi)]^2 \cdot [\tan(\delta)]^2 \text{ , if } X \leq 0 \text{ then } X = 0.00001 \tag{3a,b,c,d}$$

$$\delta = 0.409 \cdot \sin \left(2 \cdot \pi \cdot \frac{d_j}{365} - 1.39 \right)$$

where E_p: the mean monthly potential evapotranspiration or potential evapotranspiration of month i (mm month^{-1}), $T_{mean,i}$: the mean monthly temperature (ºC), n: the number of days in the month, N: the mean length of daylight of the days of the month
130 (hours), J: the annual heat index, j_i: the monthly heat index, α: the function of the annual heat index and d_j: the Julian day.

The benchmark method that was used for developing correction coefficients for the temperature-based method of Thornthwaite E_p is ASCE-standardized method (former FAO-56 Penman-Monteith), which estimates reference evapotranspiration from short, clipped grass, as follows (Allen, et al., 2005):

$$E_r = \frac{0.408 \cdot \Delta \cdot (R_n - G) + \dfrac{\gamma \cdot u_2 \cdot (e_s - e_a) \cdot C_n}{(T_{\text{mean}} + 273.16)}}{\Delta + \gamma \cdot (1 + C_d \cdot u_2)} \tag{4}$$

where E_r: the reference evapotranspiration (mm d^{-1}), Δ: the slope of the saturation vapour pressure-temperature curve (kPa ºC^{-1}), R_n: the net radiation at the crop surface (MJ m^{-2} d^{-1}), G: the soil heat flux density at the soil surface (MJ m^{-2} d^{-1}), γ: the psychrometric constant (kPa ºC^{-1}), u_2: the wind speed at 2 m height above the soil surface (m s^{-1}), e_s: the saturation vapour pressure (kPa), e_a: the actual vapour pressure (kPa), T_{mean}: the mean daily air temperature (ºC), C_n and C_d: constants, which vary according to the time step and the reference crop type and describe the bulk surface resistance and aerodynamic roughness. Eq.3 can be applied for two types of reference crop (i.e. short and tall). The short reference crop (ASCE-short) corresponds to
140 clipped grass of 12 cm height and surface resistance of 70 s m^{-1} where the constants C_n and C_d have the values 900 and 0.34, respectively. (Allen et al., 2005). The use of Eq.3 in daily or monthly step for short reference crop is equivalent to FAO-56 method (Allen et al., 1998) and this is how it is used in this study.

The derivation of a correction coefficient for Eq.1 using as benchmark the values of Eq.3 is performed based on the same procedure proposed by Aschonitis et al. (2017) that has been used before for developing partial weighted annual

correction coefficients for Priestley-Taylor and Hargreaves-Samani evapotranspiration methods. The procedure starts with the derivation of the monthly coefficient $c_{th,i}$ for each month i based on Eq.5. Applying this procedure, twelve values of monthly $c_{th,i}$ are produced. The 12 monthly c_{th} coefficients are then used to build mean annual coefficients. As it was mentioned in Aschonitis et al. (2017), the efficiency of mean annual correction coefficients is mainly associated to their ability to better describe the larger values of the dependent variable (i.e. the values of E_r during summer/hot months) and not the smaller values during cold period where the absolute errors ($e_i = E_{r,i} - E_{p,i}$) are smaller. For this reason, weighted annual averages based on the monthly $c_{th,i}$ coefficients are estimated considering the participation weight of each month in the annual E_r. Moreover, under cold conditions, the monthly coefficients $c_{th,i}$ may present unrealistic values that significantly affect the weighted averages. To solve this problem, threshold values for the monthly $E_{p,i}$ and $E_{r,i}$ were used before the inclusion of their $c_{th,i}$ in the weighted average estimations. Preliminary analysis showed that when the mean monthly $E_{p,i}$ and/or $E_{r,i}$ are below ~45 mm month^{-1} (~1.5 mm d^{-1}), then unrealistic mean monthly $c_{th,i}$ values occur (as unrealistic values are considered those, which are at least one order of magnitude larger or smaller from 1). Taking into account the above, the following procedure was performed in order to obtain a partial weighted average based on monthly $c_{th,i}$ values after excluding those months with E_r and/or $E_p \leq 45$ mm month^{-1} as follows:

$$c_{th,i} = E_{r,i}/E_{p,i} \tag{5}$$

$$\text{If } E_{r,i} > 45 \text{ mm month}^{-1} \text{ then } F_{r,i} = 1 \text{ else } = 0 \tag{6}$$

$$\text{If } E_{p,i} > 45 \text{ mm month}^{-1} \text{ then } F_{m,i} = 1 \text{ else } = 0 \tag{7}$$

$$E_{r,i}^{adj} = E_{r,i} \cdot F_{r,i} \cdot F_{m,i} \tag{8}$$

$$AE_r^{adj} = \sum_{i=1}^{12} \left(E_{r,i}^{adj} \right) \tag{9}$$

$$C_{th} = \sum_{i=1}^{12} \left(\frac{E_{r,i}^{adj}}{AE_r^{adj}} \cdot c_{th,i} \right) \tag{10}$$

where $c_{th,i}$: the monthly correction coefficient, $F_{r,i}$: the filter function for the reference method (ASCE) with values 0 or 1, $F_{m,i}$: the filter function for the understudy model (Thornthwaite formula) with values 0 or 1, $E_{r,i}^{adj}$: the adjusted monthly value of $E_{r,i}$ from ASCE-short method that becomes 0 when $F_{r,i}$ or $F_{m,i}$ is 0, AE_r^{adj}: the annual sum of the monthly $E_{r,i}^{adj}$ adjusted values, C_{th}: the annual partial weighted average (p.w.a.) of the monthly $c_{th,i}$ coefficients for short reference crop and i: the index of each month. Considering the above, the final corrected Thornthwaite formula for monthly calculations is given by the following equation:

$$E_{ps,i} = C_{th} \cdot E_{p,i} \tag{11}$$

where $E_{ps,i}$: the corrected temperature-based short reference crop evapotranspiration (mm month^{-1}) of month i.

The above procedure was followed ~~in order~~ to calibrate the annual partial weighted average C_{th} (Eq.10) for every location on the globe based on mean monthly E_r and E_p of 1950-2000 using:

- the gridded mean monthly temperature data of Hijmans et al. (2005) that were further used to estimate the mean monthly gridded original Thornthwaite E_p (Eq.1) for the period 1950-2000 (in the form of 12 raster datasets of E_p for each month),

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- the respective mean monthly grids of E_r based on ASCE-standardized for short reference crop (Eq.1) from Aschonitis et al. (2017) (in the form of 12 raster datasets of E_r for each month).

The validation procedure with the data of the 525 stations was performed by comparing the mean monthly and the mean annual benchmark values of E_r (Eq.4) versus the original E_p (Eq.1) and versus the corrected E_{ps} Thornthwaite formula (Eq.11) ~~taking into account~~considering the annual partial weighted average coefficients C_{th} at the location of each station. The

175 validation was ~~made~~ performed separately for each database of stations (ECAD, AGBM, CIMIS) but also all together using the following five statistical criteria:

$$MAE = \frac{1}{N}\sum_{i=1}^{N}|S_i - O_i| \tag{12}$$

$$ME = \frac{1}{N}\sum_{i=1}^{N}(S_i - O_i) \tag{13}$$

$$RMSE = \sqrt{\frac{1}{N}\sum_{i=1}^{N}(S_i - O_i)^2} \tag{14}$$

$$R_{Sqr} = \left[\frac{\sum_{i=1}^{N}(O_i - \overline{O_i})(S_i - \overline{S_i})}{\sqrt{\sum_{i=1}^{N}(O_i - \overline{O_i})^2 \sum_{i=1}^{N}(S_i - \overline{S_i})^2}}\right]^2 \tag{15}$$

$$d = 1 - \frac{\sum_{i=1}^{N}(S_i - O_i)^2}{\sum_{i=1}^{N}(|S_i - \bar{O}_i| + |O_i - \bar{O}_i|)^2} \tag{16}$$

where *MAE*: the mean absolute error, *ME*: the mean error, *RMSE*: the root mean square error, R_{Sqr}: the coefficient of determination and *d*: the index of agreement, *O*: the observed or benchmark value (i.e. E_r), *S*: the simulated value by the model (i.e. E_p or E_{ps}), *N*: the number of observations, *i*: the subscript referred to each observation. The value of perfect fit is 0 for the

180 criteria *MAE*, *ME* and *RMSE* while is 1 for the criteria R_{Sqr} and *d*. The values of *MAE*, *ME* and *RMSE* criteria have the same units with the observed and simulated data while R_{Sqr} and *d* are unitless.

2.3 Evaluating the use of correction coefficients in aridity indices based on stations data

The role of the new corrected formula of Thornthwaite (Eq.11) as internal parameter of aridity indices was also evaluated against the original method (Eq.1). For this purpose, the AI_{UNEP} (UNEP, 1997) and AI_{TH} (Thornthwaite, 1948) aridity indices

185 were used. The difference between the two indices is that AI_{UNEP} does not consider seasonality. The two indices estimated based on E_r (Eq.4) were used as benchmark in order to compare the respective indices calculated with the original Thornthwaite E_p (Eq.1) and the corrected E_{ps} (Eq.11) using the 525 stations data. The evaluation was performed:

- by comparing the estimated aridity classes of 525 stations produced by the benchmark AI_{UNEP} and AI_{TH} values using E_r versus the classes of the two indices using E_p and E_{ps}, respectively.

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- by comparing the respective values of the indices using 1:1 plots and the statistical metrics of Eqs.12-16.

The AI_{UNEP} aridity index is the simpler method for hydroclimatic analysis and it is given by the following equation:

$$AI_{UNEP} = \frac{P_y}{E_y} \tag{17}$$

where P_y: mean annual precipitation (mm/year) and E_y: mean annual potential evapotranspiration (mm/year). The values of Eq.16 are classified according to the following (UNEP, 1997; Cherlet, 2018):

- $AI_{UNEP}<0.05 \rightarrow$ Hyper-arid

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- $0.03 \leq AI_{UNEP}<0.2 \rightarrow$ Arid

- $0.2 \leq AI_{UNEP}<0.5 \rightarrow$ Semi-arid

- $0.5 \leq AI_{UNEP}<0.65 \rightarrow$ Dry subhumid

- $0.65< AI_{UNEP} \rightarrow$ Humid

The classes for $AI_{UNEP}>0.65$ are usually given as one humid class. The UNEP index does not consider the effect of seasonal

200 variation of precipitation and potential evapotranspiration.

The AI_{TH} aridity index is calculated as follows:

$$S = \sum_{i=1}^{12} (P_i - E_i) \quad and \quad D = \sum_{i=1}^{12} (E_i - P_i) \tag{18a,b}$$

$$AI_{TH} = 100 \frac{S - 0.6D}{E_y} \tag{19}$$

where P_i and E_i are the monthly precipitation and potential evapotranspiration of month i, respectively. S (mm y^{-1}) considers only the positive values of $(P_i-E_i)>0$, while $(P_i-E_i)<0$ are set 0. In the case of D (mm y^{-1}), only the positive values of $(E_i -P_i)$ >0 are considered while for $(E_i -P_i)<0$ are set 0. The various climatic types according to AI_{TH} values are the following:

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- $-60>AI_{TH} \rightarrow$ Hyper-arid (HE)

- $-60 \leq AI_{TH}<-40 \rightarrow$ Arid (E)

- $-40 \leq AI_{TH}<-20 \rightarrow$ Semi-arid (D)

- $-20 \leq AI_{TH}<0 \rightarrow$ Dry sub-humid (C1)

- $0 \leq AI_{TH}<20 \rightarrow$ Moist sub-humid (C2)

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- $20 \leq AI_{TH}<40 \rightarrow$ Low Humid (B1)

- $40 \leq AI_{TH}<60 \rightarrow$ Moderate Humid (B2)

- $60 \leq AI_{TH}<80 \rightarrow$ Highly Humid (B3)

- $80 \leq AI_{TH}<100 \rightarrow$ Very Humid (B4)

- $100 \leq AI_{TH} \rightarrow$ Hyper-humid (A)

3. Results

3.1 Derivation and validation of the C_{th} correction coefficients

The global map of the C_{th} correction coefficient was developed following the procedure described in Section 2.2 and it is given in Fig.3. The validation of the derived C_{th} coefficients was performed for each one of the three datasets of stations (California-CIMIS, Australia-AGBM, Europe-ECAD), separately, by comparing the performance of mean monthly values (Fig.S1a-f, supplementary material) and the performance of mean annual values (Fig.S2a-f, supplementary material) of E_p (Eq.1) and E_{ps} (Eq.11) versus the benchmark values of E_r (Eq.4). The statistical criteria (Eqs.12-16) for both monthly and annual comparisons for each one of the three datasets of stations are given in Table 1. The respective monthly and annual comparisons after merging all the stations from the three datasets are also presented in Fig.~~6a~~4a-d. From the results shown in Figs.~~S1, S2,~~ 4~~,5,6~~ and Table1, it is observed a much better performance of E_{ps} compared to the original Thornthwaite formula E_p in all cases providing not only better monthly but also better annual reference evapotranspiration estimations that approximate the values of ASCE for short reference grass.

[FIGURE 3]

[TABLE 1]

[FIGURE 4]

3.2 Evaluating the use of C_{th} coefficient in AI_{UNEP} and AI_{TH} *aridity indices*

The use of C_{th} coefficients in AI_{UNEP} and AI_{TH} aridity indices was also evaluated based on the raw data of all 525 stations (California-CIMIS, Australia-AGBM, Europe-ECAD).

The aridity classes of 525 stations given by the benchmark AI_{UNEP} using E_r were identical at 76% with the classes of the AI_{UNEP} using E_p and 93% identical with the classes of the AI_{UNEP} using E_{ps}. Similarly, the aridity classes of 525 stations given by the benchmark AI_{TH} using E_r were identical at 52% with the classes of the AI_{TH} using E_p and 58% identical with the classes of the AI_{TH} using E_{ps}. E_{ps} showed better performance compared to E_p at correctly identifying the aridity classes in both indices. The lower percentages of success in the case of AI_{TH} for both E_p and E_{ps} are due to the double number of classes of AI_{TH} in comparison to AI_{UNEP}. Merging the B and A classes of AI_{TH} to one Humid class, as in the case of AI_{UNEP}, the successful identical codes with E_r are raised to 63% for E_p and 76% for E_{ps}.

The 1:1 log-log plots of AI_{UNEP} using E_r versus the AI_{UNEP} using E_p and E_{ps} are given in Fig.5a,b, respectively, while the same comparisons using AI_{TH} are given in Fig.6a,b. The visual inspection of Figs.5,6 clearly shows that E_{ps} outperforms the E_p in the range of non-humid classes of both AI_{UNEP} and AI_{TH}. ~~In order t~~To highlight this result, the statistical metrics (Eqs.12-16) were estimated after splitting the stations in two groups (non-humid and humid) based on the respective thresholds of humid classes of each index calculated using E_r (Table 2). Table 2 verifies the better performance of E_{ps} compared to E_p in both AI_{UNEP} and AI_{TH} aridity indices for the non-humid classes.

On the other hand, the statistics showed that E_p showed better performance in both AI_{UNEP} and AI_{TH} aridity indices for their respective humid classes. This result is of less importance since E_{ps} showed better performance compared to E_p at correctly identifying the aridity classes in both indices based on all stations despite the fact that the stations belonging to humid classes were more in both indices (Table 2). Moreover, in the case of AI_{UNEP}, there is only one Humid class ($AI_{UNEP}>0.65$) and thus there is no point to compare the performance of E_p and E_{ps} from a statistical point of view since their values will always lead to the same classification code/characterization (i.e. Humid). In the case of $AI_{TH}>20$, the same justification of AI_{UNEP} could be used since the detailed division of five humid classes (B1, B2, B3, B4, A) provided by AI_{TH} was proposed for the alternative use of the index as "humidity index" (Thornthwaite, 1948).

[FIGURE 5]

[FIGURE 6]

[TABLE 2]

4 Discussion

4.1 Validity of the derived C_{th} for periods beyond the calibration period

The derivation of local C_{th} coefficients at global scale was performed using the mean monthly grid datasets of 1950-2000 assuming stationary climate conditions, while the validation was performed using stations' raw data from California and Australia that are expanded up to 2016, and stations' raw data from Europe that are expanded up to 2020 (Table S1). The reasons for choosing the specific grid datasets for the derivation of C_{th} coefficients are the following:

- They are in the form of high-resolution grids (30 arc-sec, ~1 km at equator), which have been developed using interpolation techniques that include the effects of latitude, longitude and elevation. These grids allow to derive more representative C_{th} values for every position even when weather stations do not locally exist.

- They cover a large period of time (i.e. 1950-2000) so they can provide more representative mean annual p.w.a. C_{th} values. The upper threshold of the year 2000 of these grids also allows the validation dataset of stations to be more valid since the larger part of their data is after 2000 and this reduces the possibility of having been used in grids' development.

On the other hand, several works have shown climate differences after 2000 (Hansen et al., 2010; McVicar et al., 2012a,b; Wild et al., 2013; Willet et al., 2014; Sun et al., 2017). Such changes could possibly affect the validity of C_{th} coefficients and the final estimated values of E_r for periods beyond 2000. For this reason, the C_{th} values and the mean monthly E_r values of the grids of Aschonitis et al. (2017) of the period 1950-2000 were extracted from the positions of all 525 stations and compared with the respective values of computed E_r and C_{th} using stations' raw data, which go beyond 2000. The results of this comparison are given in Figs.S3a,b (supplementary material) and clearly show that the gridded E_r data and C_{th} of 1950-2000 do not show serious deviations from their respective values for periods beyond 2000 allowing their safe use. Moreover, the fact that the original Thornthwaite (1948) formula was built before 1950 using data from the eastern and central USA and

that the C_{th} values of the specific territories range between 0.9-1.1 for 1950-2000 (Fig.3), it is not only a verification of the C_{th} derivation methodology but also an additional indication of a generalized temporal stability of C_{th}.

In the case of Fig.S3b, there is a distinctly deviated C_{th} pair of values from the 1:1 line (point indicated by a red arrow),

280 which is associated to a specific station belonging to the Centro de Investigación Atmosférica de Izaña. This station is an exceptional case since it is at the top of a mountain at 2371 m a.s.l. in Tenerife ~~island~~Island. The derived C_{th} of this station from the grid of the period 1950-2000 is almost half (C_{th} value equal to 1.37) from the one estimated using stations' raw data (C_{th} value equal to 2.44). This large difference is not the result of climate difference before and after 2000 but it is fully justified by the fact that the C_{th} value of the grid corresponds to an area of ~1 km^2 while the specific position of the station is at ~~a very~~

285 ~~unique~~a unique position, which can be described as the most extreme position within this pixel. There are also 3 stations in Tenerife ~~island~~ Island at lowland areas where the derived C_{th} values of 1950-2000 are in agreement with those estimated by the stations' raw data.

4.2 Scale and other effects on the accuracy of the derived C_{th}

290 The case of Izana station in Tenerife was the perfect example for triggering further investigation for the possible effects of scale in similar environments with extremely variable topography. Investigating the individual stations with the larger % deviation of E_{ps} from E_r, it was observed a relative systematic deviation in some stations of CIMIS-California database, which are concentrated in the coastline between Los Angeles and San Diego. The specific region is a narrow (~20-30 km), highly urbanized coastal zone of ~200 km, which is enclosed between the coastline and a hilly/mountainous zone. In the specific

295 stations, the average of C_{th} values of the period 1950-2000 from the position of these stations was 1.85, while the average of C_{th} values using their raw data was estimated at 1.46. Apart from the large topographic variation, another reason for the C_{th} differences in these stations could be the bias that has been removed by clearing extreme flagged wind values in the data of CIMIS database, which are probably associated to hurricane or other extreme events in this region. The coastline region of California is strongly affected by hurricanes and the higher wind speeds during such events may have not been removed by

300 the Sheffield et al. (2006) wind grids that were used by Aschonitis et al. (2017) to build the E_r grids. This could justify the fact that the gridded C_{th} values of 1950-2000 at the positions of the stations are greater than the C_{th} values estimated by their raw data from CIMIS after removing flagged extreme values.

An additional analysis based only on the stations of California was made to show that a wider regional mean value of C_{th} coefficient could also be an additional option, especially when the whole territory is described by local C_{th} coefficients that

305 are only >1 or only <1 (in California all local C_{th} coefficients are >1). For this analysis, the average value of C_{th}=1.66 was estimated based on the values of local C_{th} coefficients of 1950-2000 from the locations of all stations of CIMIS-California. The mean monthly and mean annual E_{ps} values of these stations were computed using C_{th}=1.66 for all of them and compared with the respective E_r values estimated with stations' raw data (Fig.S4a,b, supplementary material). The results of Fig.S4a,b showed that even a regional average of C_{th} values for California can lead to better results of E_{ps} compared to E_p as it was given

310 for monthly and annual estimations in Figs.S1a and S2a, respectively.

4.3 Justifications about the methodology for deriving annual C_{th} correction coefficients based on partial weighted averages

The initial trials to derive annual correction coefficients C_{th} of this study were made using the average value of the twelve monthly $c_{th,i}$ values of each i month. This procedure led to unreasonably high values due to the extreme high values during winter. An example of this problem based on the gridded data used in the calibration/derivation procedure, is given in Fig.S5a (supplementary material), which corresponds to a position close to Garda Lake in Italy (10.124º E, 45.45º N). According to Fig.S5a, the annual average of monthly $c_{th,i}$ values for this location is equal to 2.4 due to the extremely high values during winter and especially during January. Using the 2.4 value as annual correction coefficient, the $E_{ps,i}$ value of July becomes equal to 338 mm, which is 203 mm larger from the respective $E_{r,i}$ value of July (Fig.S5a). The specific procedure for deriving annual C_{th} coefficients was rejected due to this problem. A second approach was to use the 12 pairs of monthly E_r and E_p for each position on the grid in order to perform regression analysis based on the form $y = a \cdot x$ without intercept based on the form of $E_r = C_{th} \cdot E_p$. An example of the specific procedure is given in Fig.S5b using the data of Fig.S5a, where the annual C_{th} value was found equal to 0.98. The specific procedure provides annual C_{th} values, which are always closer to the monthly coefficients of the warmer months since optimization algorithms try to minimize the total error, which is mainly originated by the months that show larger evapotranspiration values. Despite the fact that the specific procedure pays less attention to the monthly $c_{th,i}$ values of colder months, it was considered acceptable since most of the hydroclimatic applications require higher accuracy to the larger evapotranspiration values rather to the lower ones.

A similar approach with the one of Fig.S5b was performed by Cristea et al. (2013) for deriving annual correction coefficients for the Priestley-Taylor method for 106 stations across the contiguous USA. The correction coefficients were estimated for each station by minimizing the sum of the squared residuals between Priestley-Taylor and the benchmark FAO-56 considering data only for the period April-September (warmer semester). The obtained optimized values of the correction coefficients for each station were then interpolated to produce a map of the Priestley-Taylor correction coefficients. For our study, the specific procedure was found to be extremely demanding in computing requirements since it was impossible to be performed pixel by pixel (777.6 million pixels) with a conventional computer unit for the whole globe using as input 24 rasters of extremely high resolution (~1 km) with total size of ~70GB. In order to solve this problem, the method of partial weighted average (Eqs.5-10) developed by Aschonitis et al. (2017) was used, which provides similar results to the regression analysis of $y = a \cdot x$ but allows to perform calculations step by step with a conventional computer unit in GIS environment using large, gridded databases. For the data of Fig.S5a, the partial weighted average method provided a C_{th} value equal to 0.99, which is almost equal to 0.98 of Fig.S5b. The method of partial weighted average is also extremely efficient since it is not restricted only to the warmer semester or to any other predefined period like the case of Cristea et al. (2013) since it controls all months one by one using the threshold of 45 mm month^{-1}, which is more appropriate for global applications and especially for applications of high-resolution data, giving the appropriate weight to the months with significant values of evapotranspiration.

The threshold of 45 mm month^{-1} was derived empirically after analysing many datasets using monthly and mean monthly data. In the case of monthly data, a representative example is given in Figs.S6a,b (supplementary material) using the monthly data of Embrun station in France (6.50º E, 44.57º N) 1980-2020. Fig.S6a shows the box-whisker plots of monthly $E_{r,i}$ values of the station, while Fig.S6b shows the respective box-whisker plots of monthly $c_{th,i}$ values. The maximum $c_{th,i}$ values of December, January and February are outside the plot of Fig.S6b with values 30.1, 129.4 and 210.1, respectively. Figs.S6a,b show that the monthly $c_{th,i}$ values of months with $E_{r,i} < 45$ mm month^{-1} are extremely unstable and their mean monthly value, even if it seems normal, cannot guarantee its safe use. In the case of mean monthly data, a representative example is given in Figs.7, where the 6300 mean monthly $c_{th,i}$ values derived by the raw data of the 525 stations were plotted against their respective mean monthly E_r values using a 2D density scatter plot. Fig.7 shows that the mean monthly $c_{th,i}$ values of the stations start to exhibit extremely high dispersion below the threshold of 45 mm month^{-1} with values reaching one order of magnitude larger than unity. In the case where there is a location where all months show E_r or E_p values below 45 mm month^{-1}, it is suggested either to use the non-zero C_{th} value of the closer location in the map of Fig.3 or to use directly the original Thornthwaite formula without correction.

[FIGURE 7]

4 Data availability

The produced global database of local C_{th} coefficients of this study has been archived in PANGAEA and can be assessed using the following link: https://doi.pangaea.de/10.1594/PANGAEA.932638 (Aschonitis et al., 2021). The database is provided at 5 different resolutions (30 arc-sec, 2.5 arc-min, 5 arc-min, 10 arc-min, 0.5 deg). The coarser resolutions are provided in order to cover the observed resolution range in the initial climatic data used for developing the published E_r gridded data by Aschonitis et al. (2017) (e.g., the temperature data of Hijmans et al. (2005) were provided at 30 arc-sec resolution, while the solar radiation, humidity and wind speed data of Sheffield et al. (2006) were provided at 0.5 deg resolution and rescaled to 30 arc-sec using bilinear interpolation). The data of different resolutions can be used as a tool to assess uncertainties associated to temperature variation effects within different resolution pixels or to estimate average values of the coefficients for larger territories, which have problems at coarse resolutions (e.g., coastlines or islands that do not exist in 0.5 degree resolution) taking into account the concept and concerns of Daly et al. (2006).

5 Conclusions

A global database of local correction coefficients for improving the performance of the monthly temperature-based Thornthwaite potential evapotranspiration method was built using gridded data covering the period 1950-2000. The method for developing the correction coefficients was based on partial weighted averages of their respective mean monthly values estimated as the monthly ratios between the benchmark ASCE-standardized E_r method (former FAO-56) versus the original

Thornthwaite E_p. The correction coefficients were produced as partial weighted averages of monthly E_r/E_p ratios by setting the ratios' weight according to the monthly E_r magnitude and by excluding colder months because the E_r/E_p ratio becomes highly unstable for low temperatures. The correction coefficients were validated using raw data from 525 stations of California, Australia and Europe that include independent data beyond 2000 up to 2020. The results showed that the corrections coefficients significantly improved the monthly and annual results of original Thornthwaite method E_p. The use of E_p with or without correction coefficients was also evaluated through their use in the aridity indices of Thornthwaite and UNEP versus the respective indices estimated based on the benchmark ASCE-standardized E_r. The results showed again that the correction coefficients significantly improved the performance of the indices compared to the original Thornthwaite method especially in non-humid environments. The global database of local correction coefficients supports applications of reference evapotranspiration and aridity indices assessment with minimum data requirements (i.e. mean temperature) for locations where climate data are limited. Uncertainties in the values of correction coefficients were observed in regions of high topographic variability and a recommendation for such cases is the use of a regional average of correction coefficients or the use of local C_{th} values based on the available coarser resolutions provided in the database. The methods and results presented in this study and the observed uncertainties can be used as a base for future works focusing on: (a) the validation of the correction coefficients for other places in the world, (b) comparison with other models of low data requirements, (c) use of the p.w.a. method for recalibrating correction coefficients using station or climate models' data of recent periods.

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Tables

575 **Table 1.** Statistical metrics (Eqs.12-16) for the comparisons between E_p vs. E_r and E_{ps} vs. E_r for CIMIS-California, AGBM-Australia and ECAD-Europe stations (the unit for *MAE*, *ME*, *RMSE* is mm month^{-1}).

	California		Australia		Europe	
	E_p vs. E_r	E_{ps} vs. E_r	E_p vs. E_r	E_{ps} vs. E_r	E_p vs. E_r	E_{ps} vs. E_r
	Metrics based on mean monthly values					
No. records	720	720	960	960	4620	4620
MAE	40.3	22.6	64.6	45.2	14.5	11.9
ME	-39.7	4.1	-60.5	17.3	-7.4	-6.9
RMSE	46.4	31.0	74.2	63.7	20.1	15.3
R_{Sqr}	0.852	0.858	0.624	0.746	0.824	0.919
d	0.847	0.948	0.743	0.867	0.945	0.972
	Metrics based on mean annual values					
No. records	60	60	80	80	385	385
MAE	476.2	142.1	730.5	256.8	116.6	101.6
ME	-476.2	49.8	-726.5	208.0	-89.3	-83.1
RMSE	500.1	177.9	800.2	317.0	184.7	126.0
R_{Sqr}	0.717	0.603	0.526	0.812	0.785	0.879
d	0.501	0.845	0.571	0.906	0.728	0.94

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Table 2. Statistical metrics (Eqs.12-16) for the comparisons between E_p vs. E_r and E_{ps} vs. E_r when they are applied in the (a) AI_{UNEP} and (b) AI_{TH} aridity indices by dividing the 525 stations to two groups based on non-humid or humid classes of each index (*MAE*, *ME*, *RMSE* are unitless as the indices).

	E_p vs. E_r	E_{ps} vs. E_r	E_p vs. E_r	E_{ps} vs. E_r
(a)	*Stations with $AI_{UNEP} \leq 0.65^*$ (non-humid)*		*Stations with $AI_{UNEP} > 0.65^*$ (humid)*	
No. stations	197	197	328	328
MAE	0.169	0.036	0.151	0.264
ME	0.169	0.003	0.035	0.233
RMSE	0.194	0.056	0.264	0.376
R_{Sqr}	0.867	0.893	0.875	0.932
d	0.773	0.969	0.963	0.950
(b)	*Stations with $AI_{TH} \leq 20^*$ (non-humid)*		*Stations with $AI_{TH} > 20^*$ (humid)*	
No. stations	257	257	268	268
MAE	12.8	6.3	14.9	26.7
ME	12.7	3.6	3.0	24.2
RMSE	15.1	10.0	26.6	39.4
R_{Sqr}	0.842	0.882	0.872	0.928
d	0.855	0.939	0.962	0.945

*estimated by the benchmark E_r.

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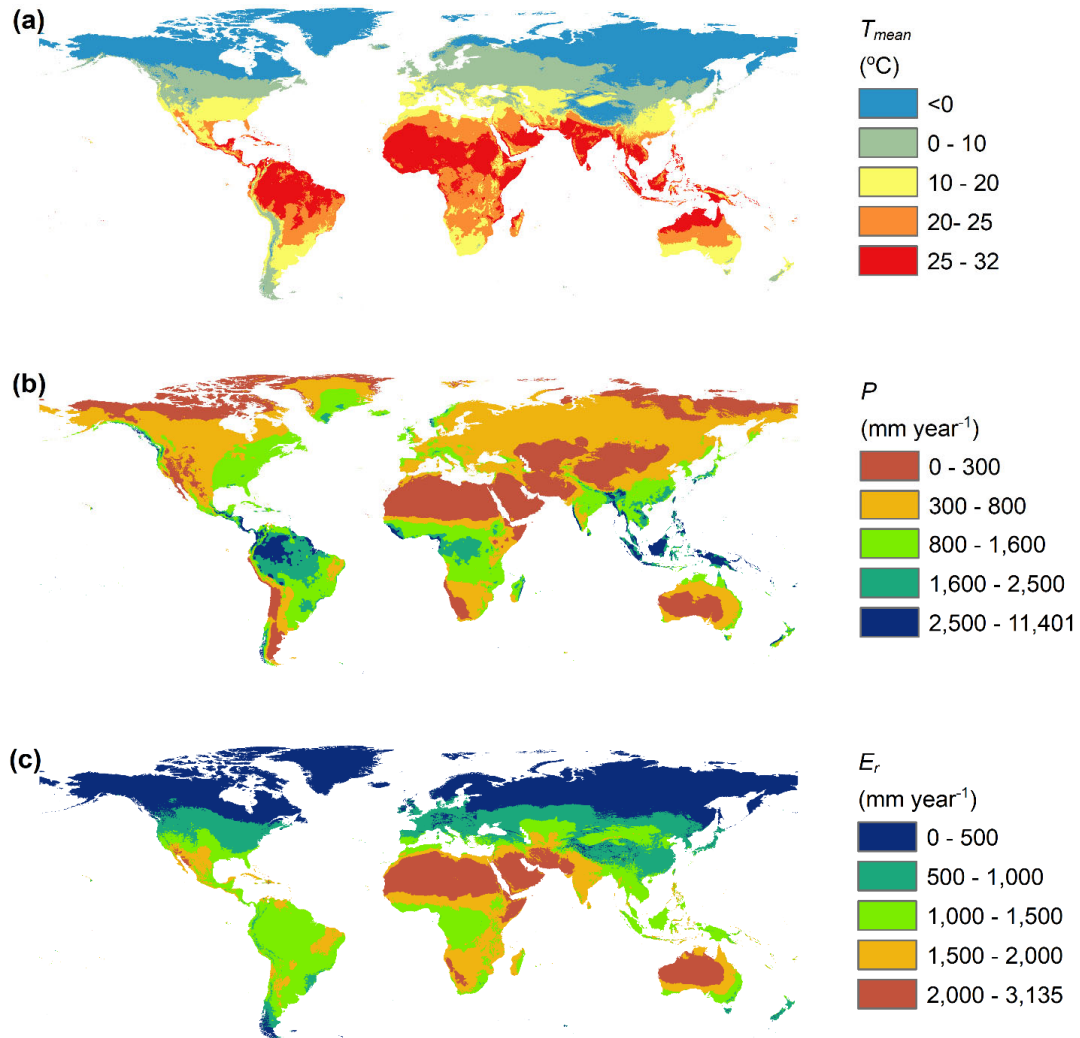
620   **Figure 1. (a)** Mean annual temperature for the period (Hijmans et al., 2005), **(b)** Mean annual precipitation for the period (Hijmans et al., 2005), **(c)** mean annual reference evapotranspiration of ASCE-standardized method for short reference crop for the period (Aschonitis et al., 2017) of 1950-2000.
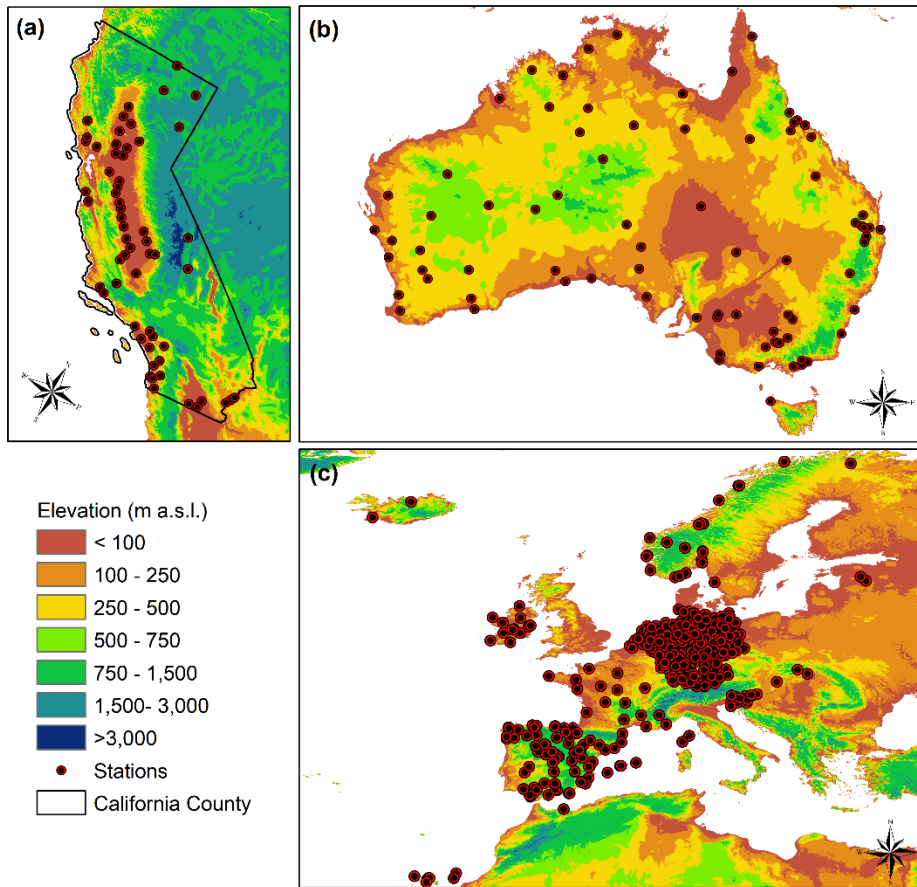
Figure 2. (a) 60 stations of California from CIMIS database, **(b)** 80 stations of Australia from AGBM database, and **(c)** 385 stations of Europe from ECAD database.
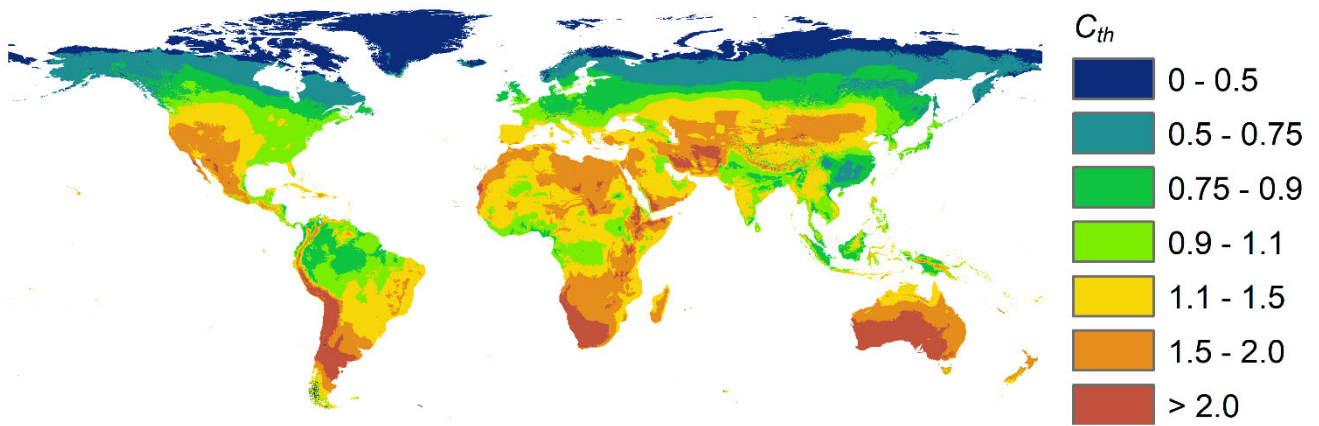
Figure 3. Global map of the annual partial weighted average C_{th} coefficients.
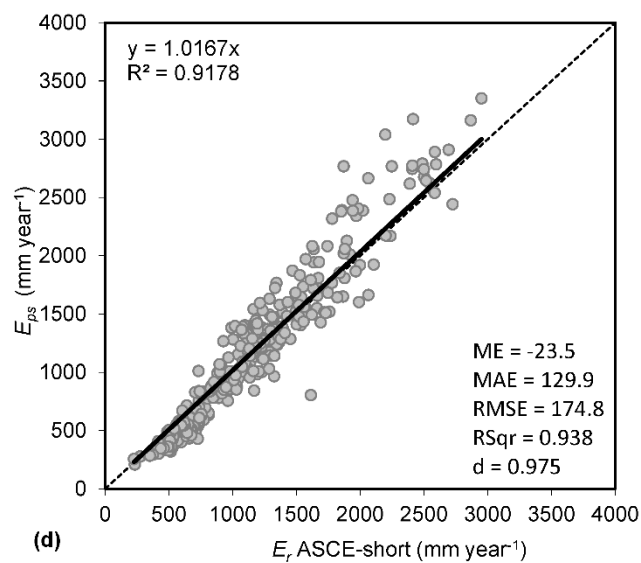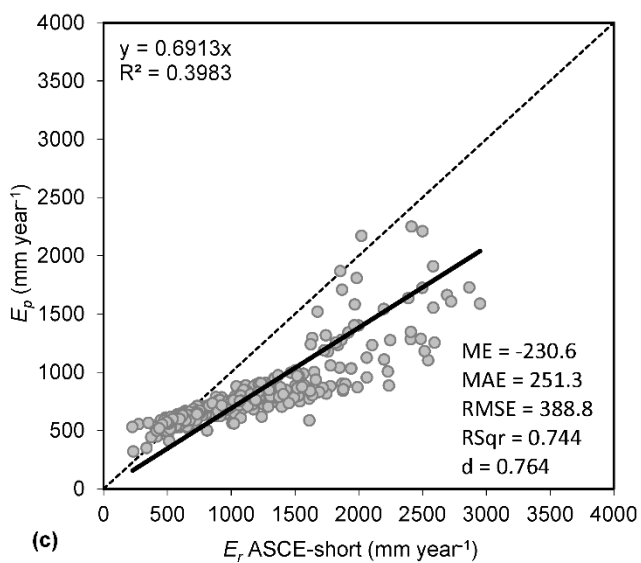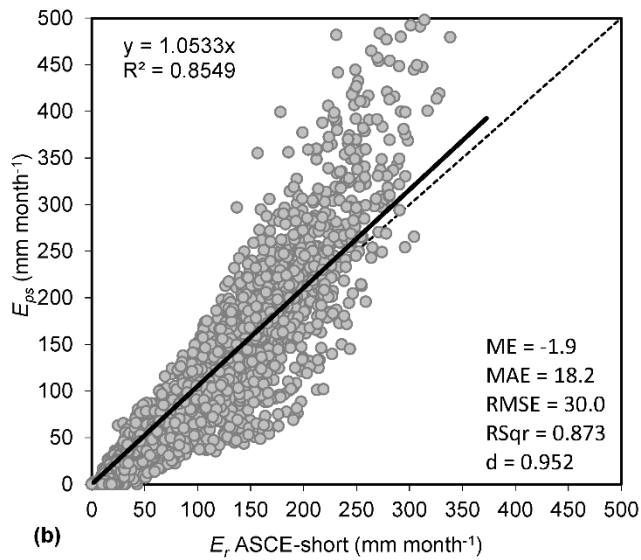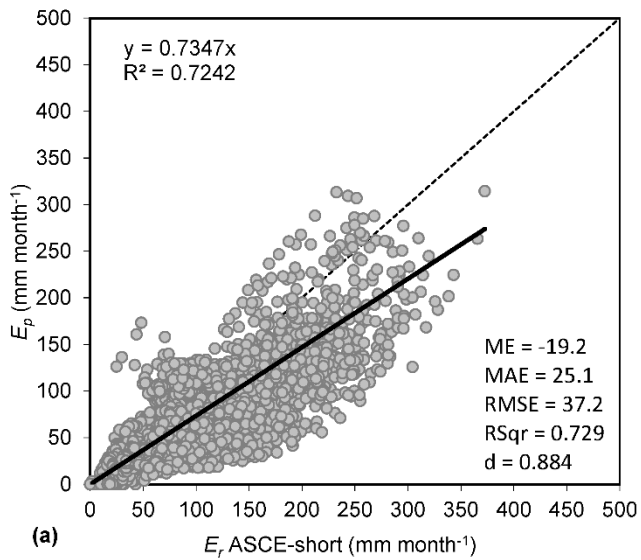
Figure 4. (a) 1:1 plots of mean monthly E_p versus mean monthly E_r, **(b)** mean monthly E_{ps} versus mean monthly E_r, **(c)** mean annual E_p versus annual monthly E_r, **(d)** mean annual E_{ps} versus annual monthly E_r, using the data of all 525 stations from the three databases of CIMIS, AGBM, ECAD.

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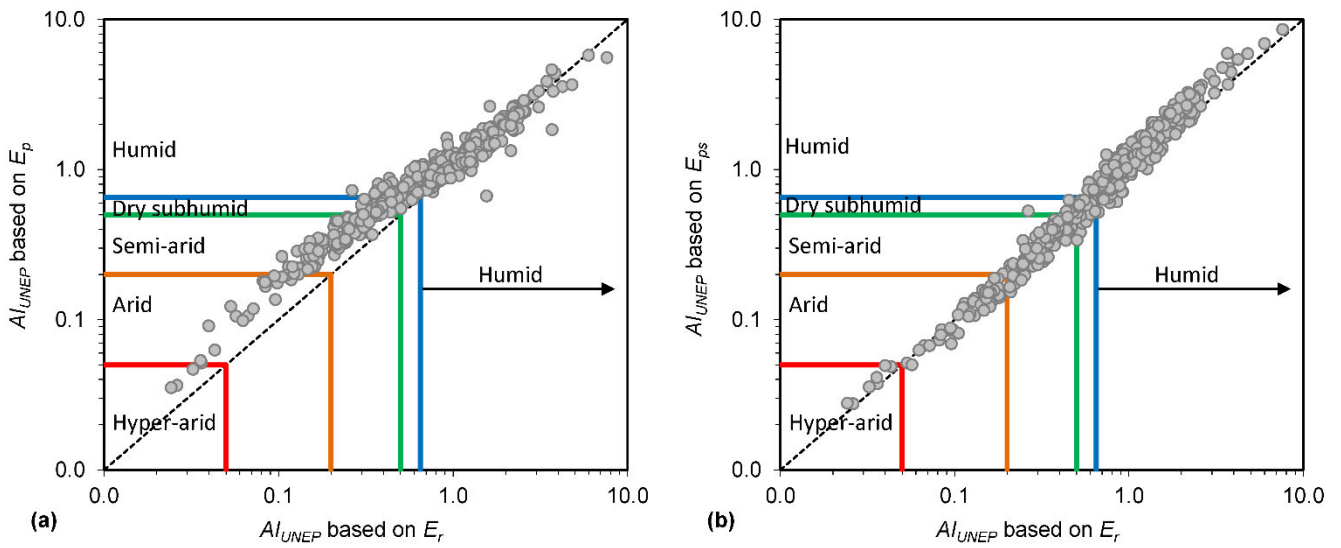
Figure 5. (a) 1:1 log-log plots of AI_{UNEP} using mean monthly E_p versus AI_{UNEP} using mean monthly E_r, **(b)** AI_{UNEP} using mean monthly E_{ps} versus mean monthly E_r using the data of all 525 stations from the three databases of CIMIS, AGBM, ECAD.

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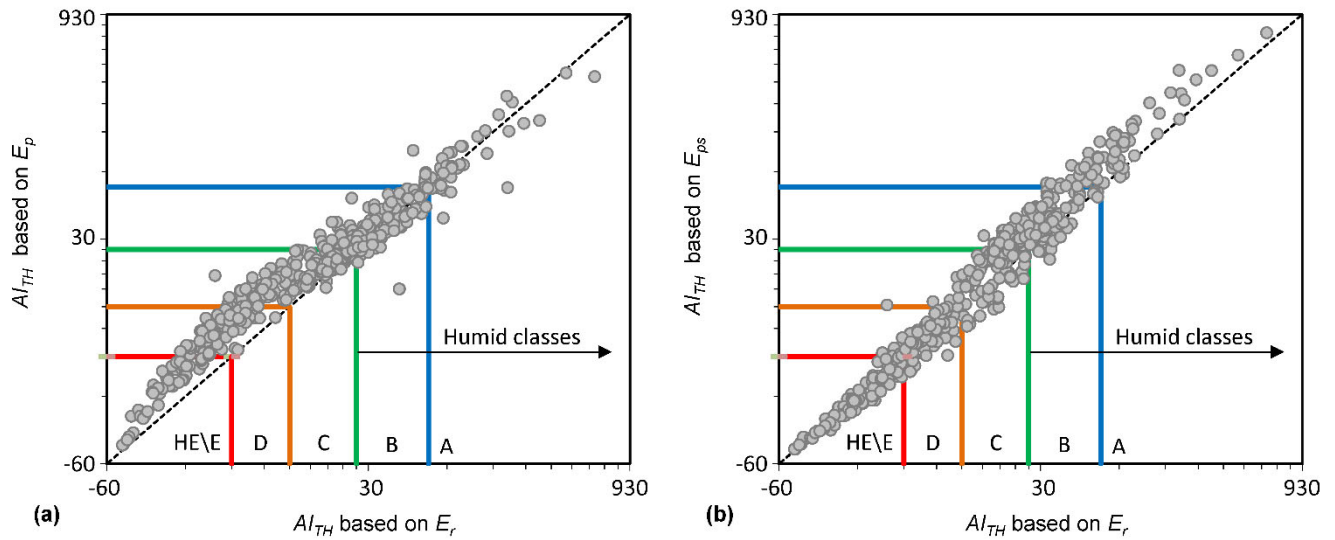
Figure 6. (a) 1:1 log-log plots of AI_{TH} using mean monthly E_p versus AI_{TH} using mean monthly E_r, **(b)** AI_{TH} using mean monthly E_{ps} versus mean monthly AI_{TH} using the data of all 525 stations from the three databases of CIMIS, AGBM, ECAD.

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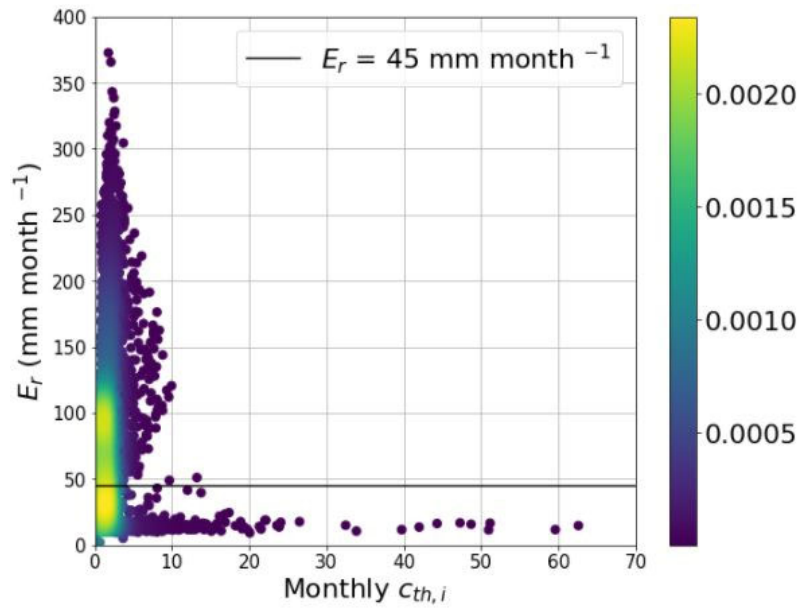
Figure 7. 2D scatter density plot between the 6300 mean monthly $c_{th,i}$ values versus the respective mean monthly E_r values derived by the raw data of the 525 stations ($c_{th,i}$ =0 or non-defined due to E_r and/or E_p =0 were not included in the graph).