



Supplement of

A combination of time-variable gravity field solutions from multi-satellite datasets (1993–2024) via constrained collocation model

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S1. Supplementary Tables and Figures

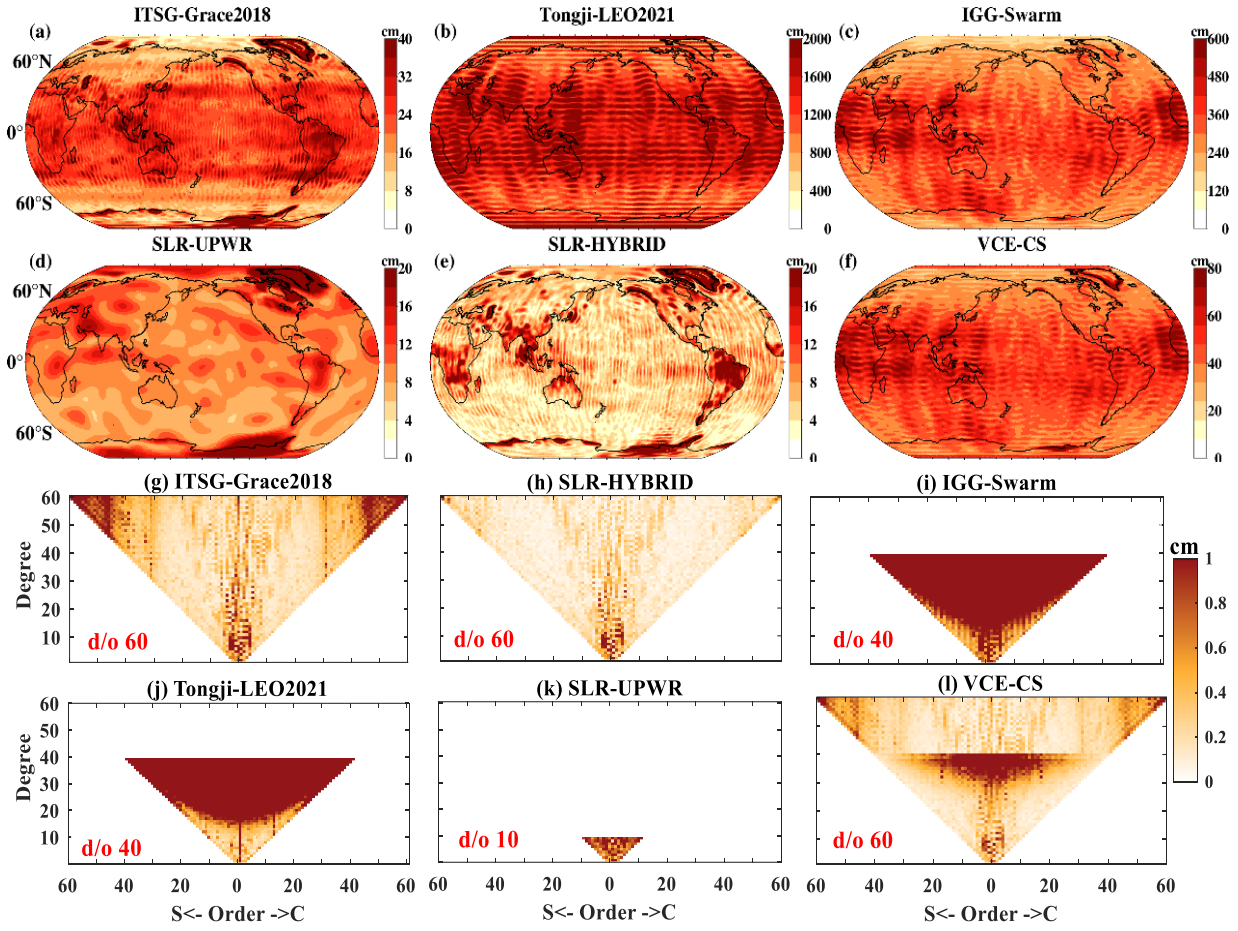


Figure S1: (a-f) RMS of spatial TWSAs and (g-l) SHCs derived from individual and VCE-CS.

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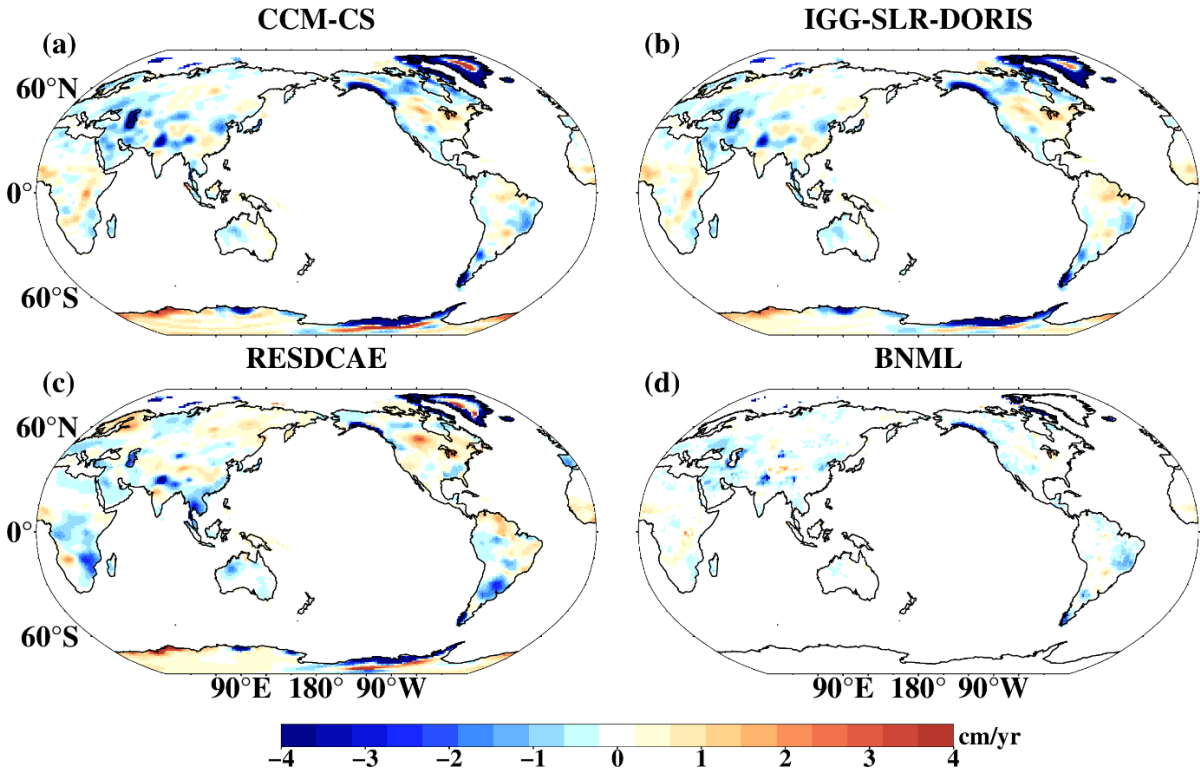


Figure S2: Linear trends of global TWSA during the common period from January 1994 to December 2020.

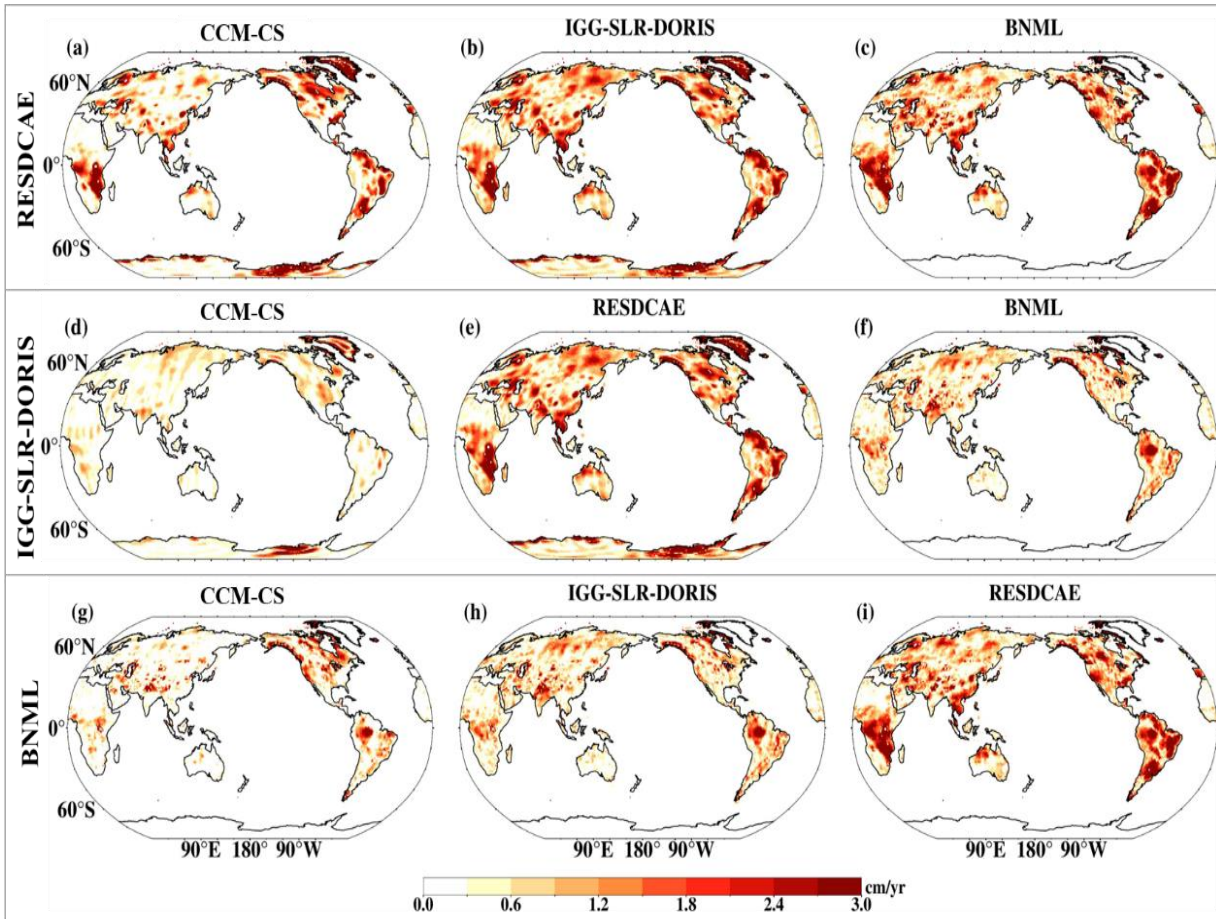


Figure S3: Absolute differences in linear trend of global TWSA from various solutions relative to RESDCAE, IGG-SLR-DORIS, and BNML corresponding to the first to third rows (January 1994 to December 2020).

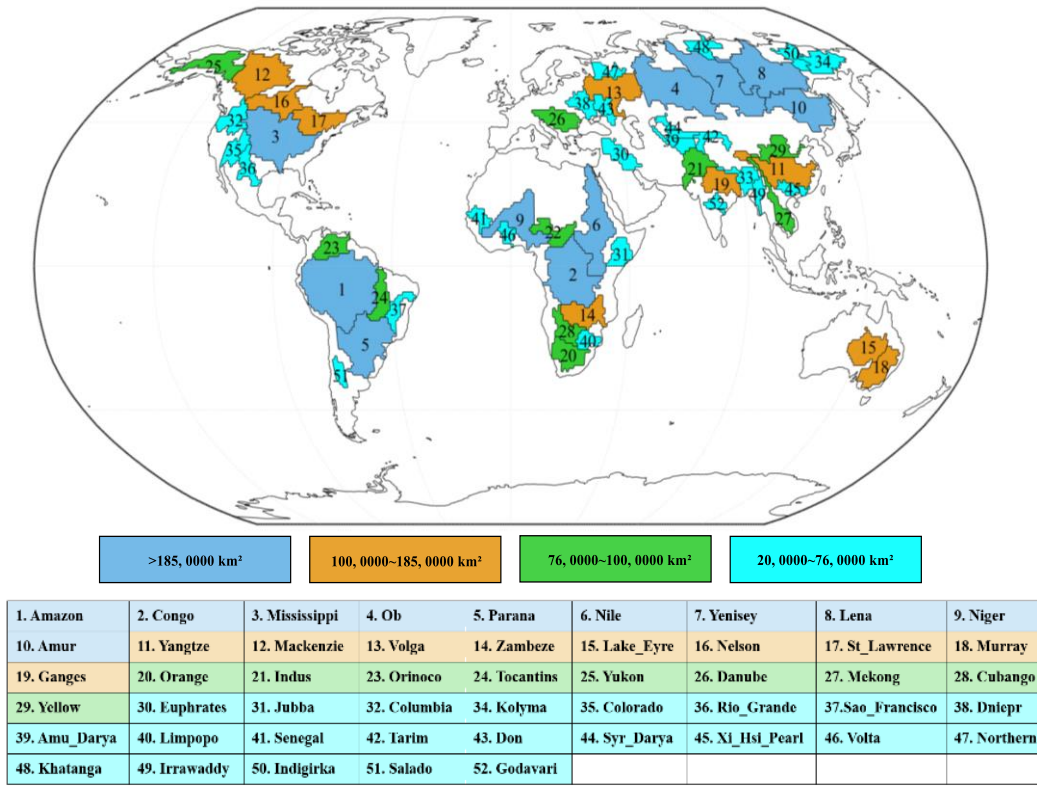


Figure S4: Spatial distributions of 52 major basins over the world, with different colors representing various area scales.

Table S1. Details of multi-type data products.

	Data type	Sources	Period	Maximum d/o (Grid resolutions)
TVGFS	GRACE/GFO	ITSG-Grace2018 ^[1]	2002.04-2024.12	60
	Swarm	IGG-Swarm ^[2]	2014.08-2021.03	40
	LEO	Tongji-LEO2021 ^[3]	1993.01-2004.12	
	SLR	IGG-SLR-UPWR ^[4]	1995.02-2023.11	
			IGG-SLR-HYBRID ^[5]	1993.01-2020.12
Previous studies	IGG-SLR-DORIS ^[6]	GRACE SHCs/SLR/DORIS	1984.01-2023.12	60
	BNML ^[7]	NOAH/CLSM	1960.01-2022.12	1° x 1°
	RESDCAE ^[8]	GRACE Mascon/SLR/ERA5	1994.01-2021.12	
		Mascon	CSR RL06 ^[9]	2002.04-2024.12
		JPL RL06 ^[10]	3° x 3°	
Sea level budget	$\Delta h_{\text{thermosteric}}$	^[11]	1900.01-2018.12	Time series (Yearly)
	$\Delta h_{\text{GrIS}}, \Delta h_{\text{AIS}}$			
	GMSL	^[11]		
		Satellite altimetry ^[12]	1993.01-2024.12	Time series (Monthly)
	Water balance equation	Precipitation	CRUv4.09 ^[13]	1901.01-2024.12
GPCCv2020 ^[14]			1982.01-2020.12	1° x 1°
TRMM ^[15]			1998.01-2020.01	0.25° x 0.25°
Evaporation		GLEAM ^[16]	1993.01-2024.12	0.1° x 0.1°
		FluxCom ^[17]	2001.01-2013.12	0.5° x 0.5°
		PML-v2 ^[18]	2002.06-2019.08	0.5° x 0.5°
		Global-ET ^[19]	1993.01-2006.12	1° x 1°
		G-RUN ^[20]	1901.07-2019.12	0.5° x 0.5°
Runoff		SURFEX-TRIP ^[21]	1979.01-2012.12	
		W3RA ^[22]		
			CNRDv1 ^[23]	2001.01-2018.12
	GRDC ^[24]	1950.01–2023.12	In-situ	
Ice Sheets	AIS, GrIS	IMBIE ^[25]	1993.01-2020.12	Time series (Monthly)

Table S2. Notation box for core symbols used in the Methodology.

Symbol	Description	Dimension	Initial appears in
k, i	Month index and TVGFS index.	Scalars	Eq. (1)
l, m	Spherical harmonic degree and order.	Scalars	Eq. (1)
$M_{k,i}$	Number of SHCs provided by the i -th TVGFS at month k .	1×1	Eq. (3)
M	Number of SHCs in the target combined TVGFS.	1×1	Eq. (3)
q_k	Number of individual TVGFS available at month k .	1×1	Eq. (2)
N_k	Total number of observations at month k	1×1	Eq. (2)
G	Number of global grids for one month	$G \times 1$	Eq. (7)
$y_{k,i}^{lm}$	SHC from the i -th TVGFS for degree l and order m at month k .	1×1	Eq. (1)
Δt_k	Time interval between month k and the reference epoch.	1×1	Eq. (1)
$a_{0,i}^{lm}, \dots, a_{6,i}^{lm}$	Deterministic coefficients: constant, trend, acceleration, annual and semi-annual.	1×1	Eq. (1)
$s_{k,i}^{lm}$	Non-seasonal signal (NSS) for the corresponding SHC.	1×1	Eq. (1)
$e_{k,i}^{lm}$	Observation error corresponding to $y_{k,i}^{lm}$.	1×1	Eq. (1)
$\mathbf{y}_{k,i}$	Observation vector stacking SHCs from the i -th TVGFS at month k .	$M_{k,i} \times 1$	Eq. (2)
$\mathbf{y}_k$	Combined observation vector stacking all available TVGFS at month k .	$N_k \times 1$	Eq. (2)
$\mathbf{A}_{k,i}$	Design matrix for the i -th TVGFS harmonic model.	$M_{k,i} \times 7M$	Eq. (4)
$\mathbf{A}_k$	Stacked design matrix for all available TVGFS at month k .	$N_k \times 7M$	Eq. (2)
$\mathbf{B}_{k,i}$	Selection/extension matrix mapping target SHCs to the i -th TVGFS support.	$M_{k,i} \times M$	Eq. (3)
$\mathbf{B}_k$	Stacked selection matrix for all available TVGFS at month k .	$N_k \times M$	Eq. (2)
$\mathbf{x}$	Combined deterministic parameter vector for all target SHCs.	$7M \times 1$	Eq. (2)
$\mathbf{s}_k$	Combined NSS vector at month k .	$M \times 1$	Eq. (2)
$\mathbf{e}_k$	Combined observation-error vector at month k .	$N_k \times 1$	Eq. (2)
$\mathbf{P}_{e_k}$	Block-diagonal weight matrix of combined observation errors.	$N_k \times N_k$	Eq. (2)
$\mathbf{\Sigma}_{e_k}$	Covariance matrix of combined observation errors.	$N_k \times N_k$	Eq. (2)
$\sigma_{e_i}^2$	Time-invariant variance factor for the i -th TVGFS.	1×1	Eq. (2)
$\Phi_{k,j}$	State transition matrix from epoch j to k in the GM model.	$M \times M$	Eq. (5)
r	Order of multi-order GM model	1×1	Eq. (5)
τ_s	Correlation time of the GM process.	1×1	Eq. (6)
σ_s^2	Variance component of the GM process.	1×1	Eq. (6)
$\mathbf{w}_k$	GM process noise at month k .	$M \times 1$	Eq. (5)
$\mathbf{Q}_k$	Covariance matrix of GM process noise.	$M \times M$	Eq. (6)
$\mathbf{D}$	Diagonal degree-dependent scale matrix.	$M \times M$	Eq. (6)
$\bar{\mathbf{s}}_k$	Predicted NSS before the Kalman update.	$M \times 1$	Eq. (9)
$\mathbf{\Sigma}_{\bar{\mathbf{s}}_k}$	Predicted/updated covariance matrix of NSS at month k .	$M \times M$	Eq. (9)
α	Regularization parameter selected by the minimum-MSE criterion.	1×1	Eq. (7)
$\mathbf{R}$	Regularization matrix propagated from the spatial expression of $\mathbf{x}$.	$7M \times 7M$	Eq. (7)
$\mathbf{T}$	Spherical harmonic analysis matrix used in constructing $\mathbf{R}$	$7M \times 7G$	Eq. (7)
$\mathbf{x}_g$	Spatial expression of the deterministic parameter vector $\mathbf{x}$.	$7G \times 1$	Eq. (7)
$\mathbf{K}_k$	Kalman gain matrix for updating NSS at month k .	$M \times N_k$	Eq. (11)
L	Cost function minimized to determine r , τ_s , and σ_s^2 .	1×1	Eq. (12)
$\bar{\mathbf{v}}_k$	Prediction residual used in the GM-model cost function.	$N_k \times 1$	Eq. (12)
$\mathbf{C}_k$	Covariance matrix of $\bar{\mathbf{v}}_k$.	$N_k \times N_k$	Eq. (12)
$\mathbf{M}_{\hat{\mathbf{x}}}$	MSE matrix of the combined deterministic parameter vector $\hat{\mathbf{x}}$.	$7M \times 7M$	Eq. (12)

20 S2. Iterative process for combining TVGFS

Since the estimated equations for $\hat{\mathbf{x}}$ and $\hat{\mathbf{s}}_k$ in Eqs. (8) and (11) are mutually nested; the estimation process is iteratively conducted. This process involves updating the variance factors $\sigma_{e_i}^2$, regularization parameter α , regularization matrix $\mathbf{R}$, optimal variables of GM model, as summarized in Fig. S5.

The iteration initializes with variance factors $(\sigma_{e_i}^2)^{(0)} = 1$ for $i = 1, \dots, q_k$, NSS $(\hat{\mathbf{s}}_k)^{(0)} = \mathbf{0}$, and parameters obtained from
 25 least-squares solutions $((\hat{\mathbf{x}})^{(0)} = \hat{\mathbf{x}}_{ls})$. At h th iteration, covariance matrix $\boldsymbol{\Sigma}_{e_k}^{(h)} = (\sigma_{e_{k,i}}^2)^{(h)} \mathbf{P}_{e_{k,i}}^{-1}$ and regularization matrix $\mathbf{R}^{(h)} = (\mathbf{D} \mathbf{T} \hat{\mathbf{x}}_g^{(h)} (\hat{\mathbf{x}}_g^{(h)})^T \mathbf{T}^T \mathbf{D}^T)^{-1}$ are computed beforehand, where $\hat{\mathbf{x}}_g^{(h)}$ represents the spatial expression of $(\hat{\mathbf{x}})^{(h)}$. $\alpha^{(h)}$ is determined using the minimum MSE criterion [26; 27]. Subsequently, $(\hat{\mathbf{x}})^{(h+1)}$ is updated via Eq. (8), while $(\hat{\mathbf{s}}_k)^{(h+1)}$ is updated using bi-directional KF (Eqs. (10) and (11)) with the GM variables r , τ_s , and σ_s^2 selected by minimizing Eq. (12) over predefined grid-search ranges: $r = 1-6$, $\tau_s = 30-360$ days with a 30-day interval, and $\sigma_s^2 = 0.001-10$ cm² with an interval
 30 of 0.01 cm². Finally, the variance factors $(\sigma_{e_{k,i}}^2)^{(h+1)}$ are updated using bias-corrected VCE [28] with $\alpha^{(h)}$, $\mathbf{R}^{(h)}$, and $(\hat{\mathbf{x}})^{(h+1)}$.

Finally, the iteration continues until the differences of regularization solutions $\hat{\mathbf{x}}$ between consecutive iterations falls below

$$1\% \quad (\text{i.e., } \frac{\|\hat{\mathbf{x}}^{(h)} - \hat{\mathbf{x}}^{(h-1)}\|_2}{\|\hat{\mathbf{x}}^{(h-1)}\|_2} < 0.01). \quad \text{The combined TVGFS } \hat{\mathbf{y}}_k = \bar{\mathbf{A}}_k \hat{\mathbf{x}} + \hat{\mathbf{s}}_k, \quad \text{with } \bar{\mathbf{A}}_k =$$

$$[1 \quad \Delta t_k \quad \Delta t_k^2 \quad \sin(2\pi \Delta t_k) \quad \cos(2\pi \Delta t_k) \quad \sin(4\pi \Delta t_k) \quad \cos(4\pi \Delta t_k)] \otimes \mathbf{I}_M.$$

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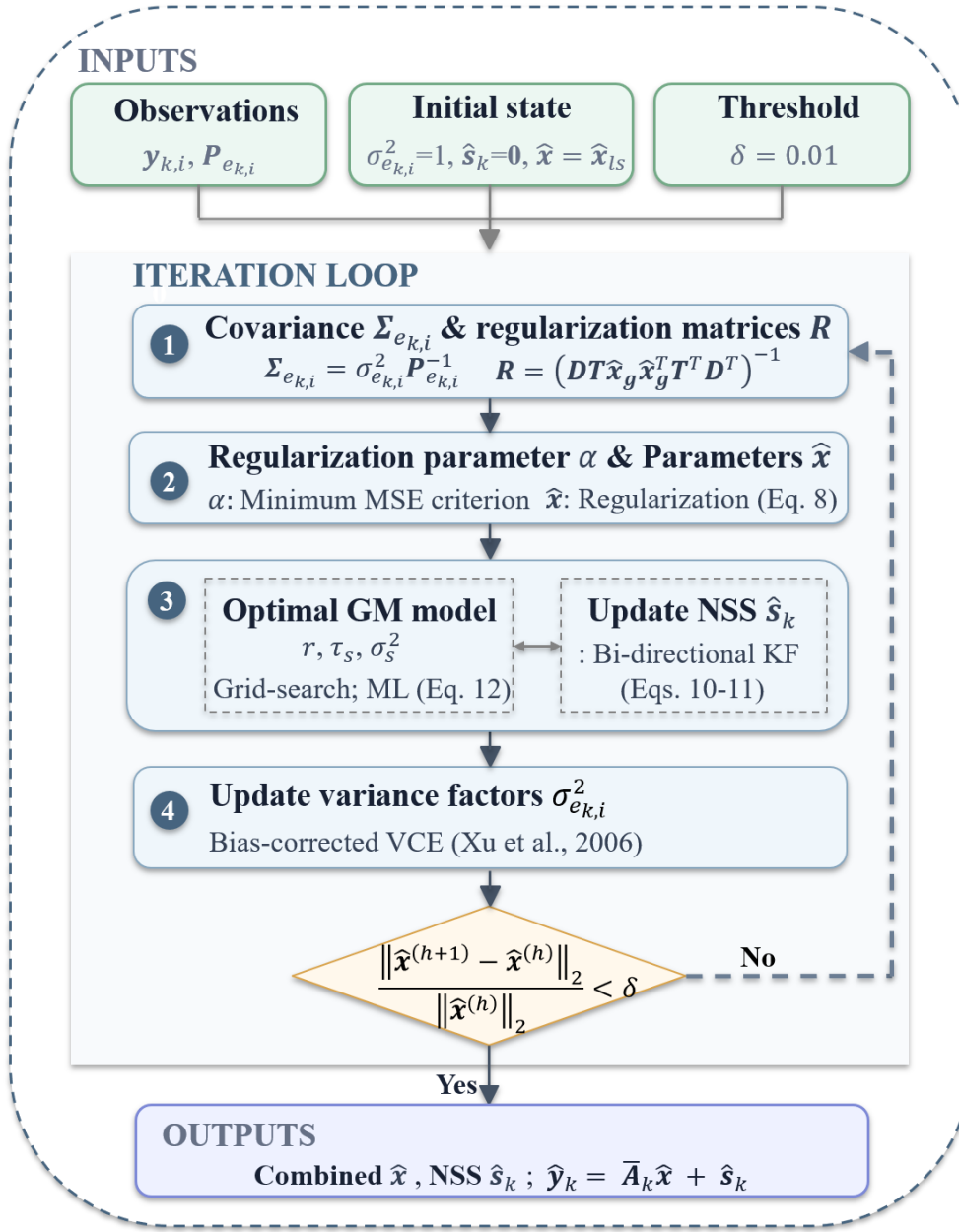


Figure S5: Flowchart for iteratively combining TVGFS (The symbols are introduced in Tab. S2).

S3. Fusion of in-situ observations with gridded simulated runoff

For month t , the observation equation is written as,

$$y_t = H_t x_t + \varepsilon_t \quad (S1)$$

where y_t is the observation vector formed from monthly GRDC runoff observations in terms of runoff depth, ε_t is the observation error, x_t is the simulated runoff state vector, H_t is the design matrix that maps gridded runoff to each in-situ station by aggregating grid-cell runoff over the corresponding station-controlled drainage area [29].

50 The fused runoff state is obtained by minimizing the cost function,

$$J(\mathbf{x}_t) = (\mathbf{x}_t - \mathbf{x}_t^b)^T (\mathbf{Q}_t^b)^{-1} (\mathbf{x}_t - \mathbf{x}_t^b) + (\mathbf{y}_t - \mathbf{H}_t \mathbf{x}_t)^T \mathbf{\Sigma}_t^{-1} (\mathbf{y}_t - \mathbf{H}_t \mathbf{x}_t) \quad (\text{S2})$$

where the background state $\mathbf{x}_t^b = \frac{1}{N} \sum_{k=1}^N \mathbf{x}_t^{b,(k)}$ with $\mathbf{x}_t^{b,(k)}$ denoting the k th simulated runoff product among N ensemble members; the background error covariance $\mathbf{Q}_t^b = \frac{1}{N-1} \sum_{k=1}^N (\mathbf{x}_t^{b,(k)} - \mathbf{x}_t^b)(\mathbf{x}_t^{b,(k)} - \mathbf{x}_t^b)^T$; and the observation-error covariance $\mathbf{\Sigma}_t = \text{diag}(\sigma_{1,t}^2, \dots, \sigma_{m_t,t}^2)$, with $\sigma_{s,t}$ representing the uncertainty of the runoff observation at s th station, and m_t is the number of valid GRDC stations at month t .
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The corresponding ensemble solution $\mathbf{x}_t^a$ is,

$$\mathbf{x}_t^a = \mathbf{x}_t^b + \mathbf{K}_t (\mathbf{y}_t - \mathbf{H}_t \mathbf{x}_t^b) \quad (\text{S3})$$

where $\mathbf{K}_t = \mathbf{Q}_t^b \mathbf{H}_t^T (\mathbf{H}_t \mathbf{Q}_t^b \mathbf{H}_t^T + \mathbf{\Sigma}_t)^{-1}$ is the gain matrix.

S4. Evaluation Metrics

60 (1) Sea level budget

TWS contribution to global mean sea level (Δh_{GMSL}) variations is deived by subtracting thermosteric expansion (Δh_{therm}) and mass changes of Greenland (Δh_{GrIS}) and Antarctic (Δh_{AIS}) Ice Sheets from total GMSL ^[11],

$$\Delta h_{\text{TWS}} = \Delta h_{\text{GMSL}} - \Delta h_{\text{therm}} - \Delta h_{\text{GrIS}} - \Delta h_{\text{AIS}} \quad (\text{S4})$$

(2) Water balance equation

65 TWSCs from TVGFS ($\Delta \text{TWSC}_{\text{TVGFS}}$) computed from TWSAs between two adjacent months can be evaluated by computing the misclosure with water balance estimates composed of precipitation (P), runoff (R), and evaporation (E) ^[30],

$$\Delta \text{TWSC}_{\text{TVGFS}} = P - R - E \quad (\text{S5})$$

(3) Land-to-ocean Signal-to-Noise Ratios (SNRs)

The SNR at latitude θ_i (i.e., SNR_{θ_i}) is computed using the Root Mean Square (RMS) of mass changes over land
70 ($\text{MASS}_{\text{land},\theta_i}$) and ocean ($\text{MASS}_{\text{ocean},\theta_i}$) at the corresponding latitude^[31; 32],

$$\text{SNR}_{\theta_i} = \frac{\text{RMS}(\text{MASS}_{\text{land},\theta_i} + \text{Err}_{\theta_i})}{\text{RMS}(\text{MASS}_{\text{ocean},\theta_i} + \text{Err}_{\theta_i})} \quad (\text{S6})$$

The overall SNR is determined using the global latitude weighted average, $\text{SNR} = \frac{\sum_{i=1}^n \cos \theta_i \cdot \text{SNR}_{\theta_i}}{\sum_{i=1}^n \cos \theta_i}$, n indicates the number of latitude divisions in the global grid.

(4) Degree Power σ_l^2

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$$\sigma_l^2 = \frac{\sum_{m=0}^l [(\Delta C_{lm}^\gamma)^2 + (\Delta S_{lm}^\gamma)^2]}{2l+1} \quad (S7)$$

where, C_{lm}^γ and ΔS_{lm}^γ are filtered SHCs at degree l and order m ^[33].

(5) Nash-Sutcliffe Efficiency (NSE)

80

$$NSE = 1 - \frac{\sum_{t=1}^n (TWSA_{\text{evaluated}}(t) - TWSA_{\text{reference}}(t))^2}{\sum_{t=1}^n (TWSA_{\text{evaluated}}(t) - \overline{TWSA_{\text{reference}}})^2} \quad (S8)$$

where, TWSA derived from various solutions to be evaluated and the references are denoted as $TWSA_{\text{filtered}}$ and $TWSA_{\text{reference}}$; $\overline{TWSA_{\text{reference}}}$ is the mean value of $TWSA_{\text{reference}}$. NSE approaching 1 means excellent consistency while negative NSE denotes worse consistency^[34].

References

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