



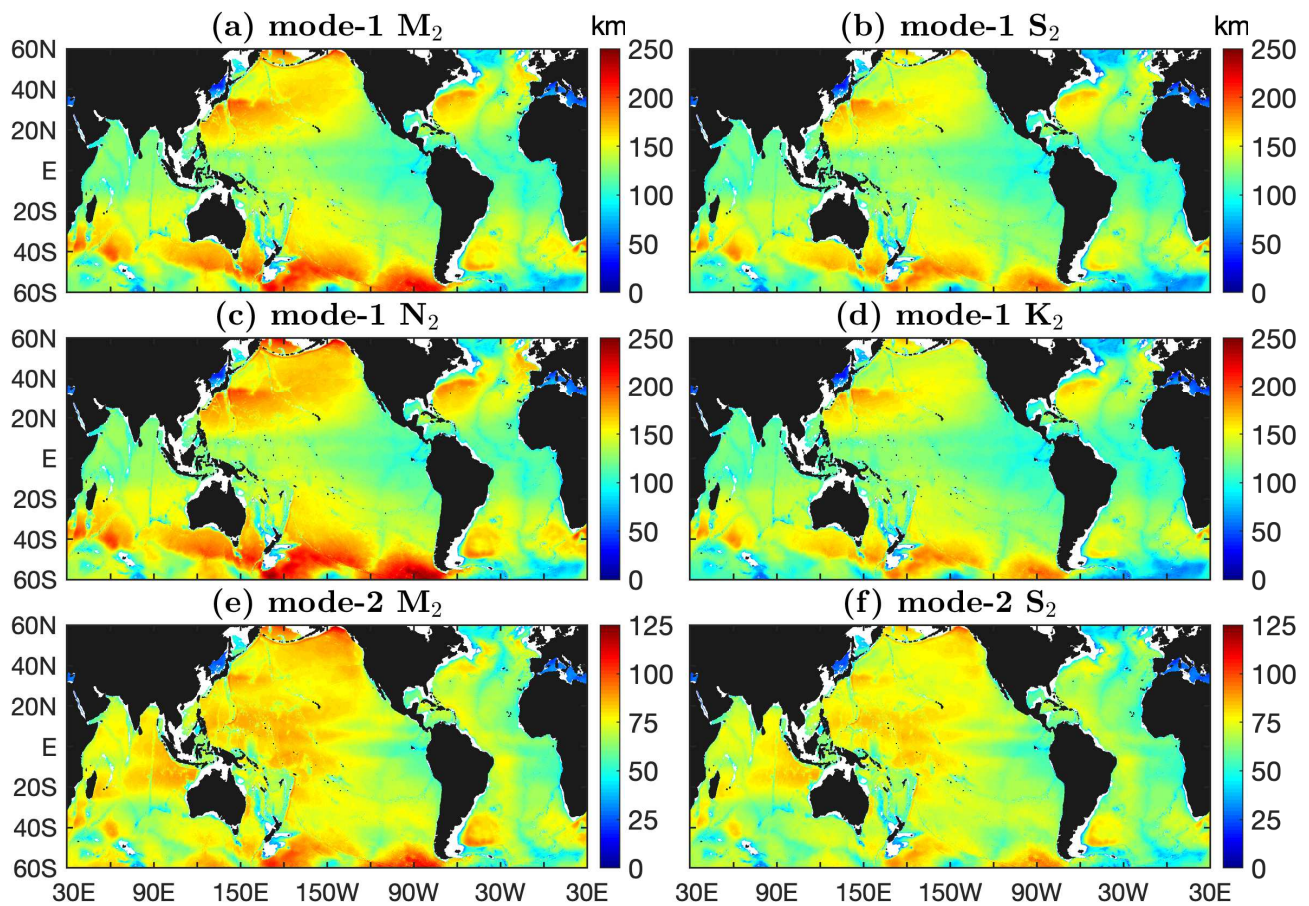
## *Supplement of*

# **A new-generation internal tide model based on 30 years of satellite sea surface height measurements: multiwave decomposition and isolated beams**

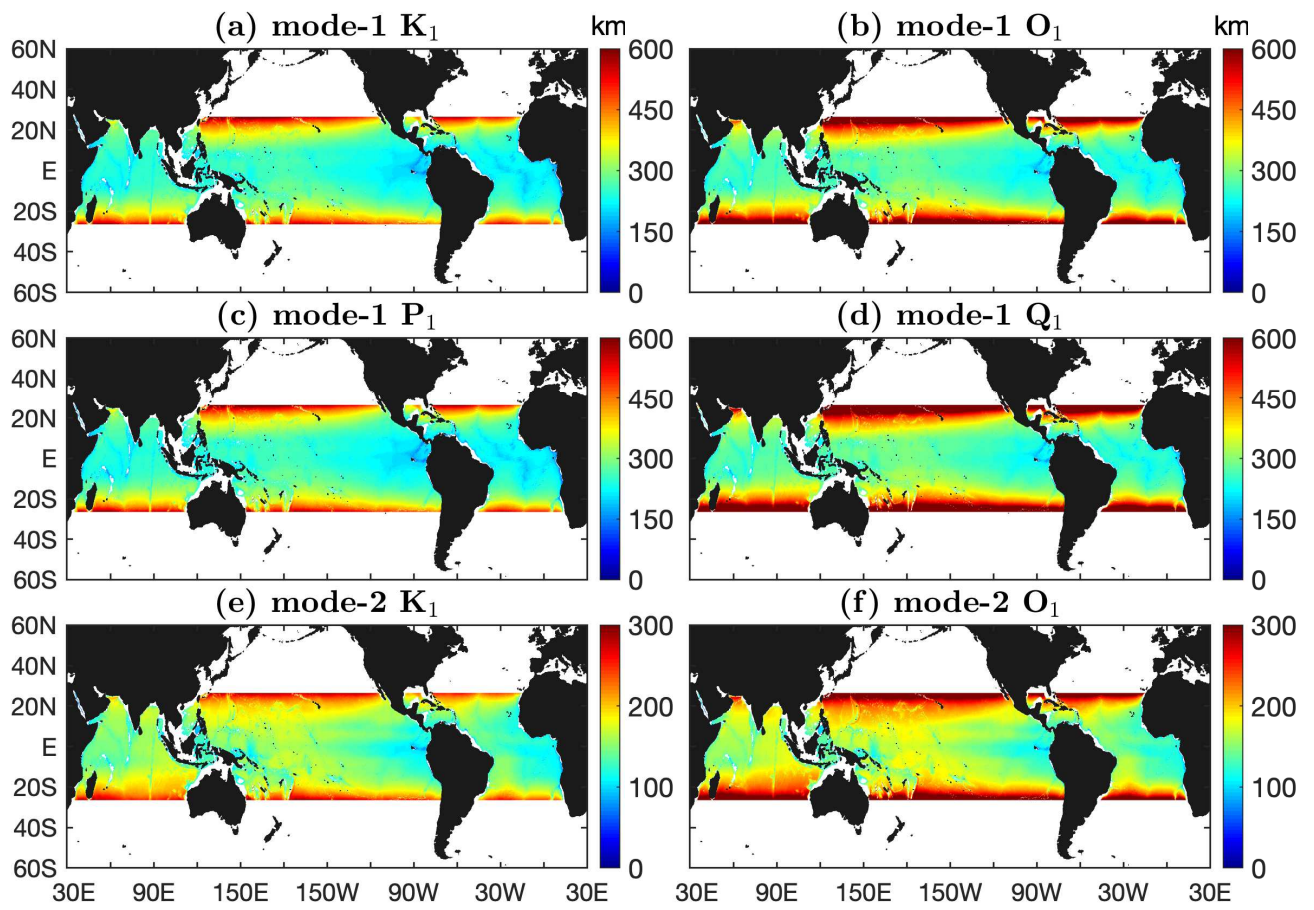
**Zhongxiang Zhao**

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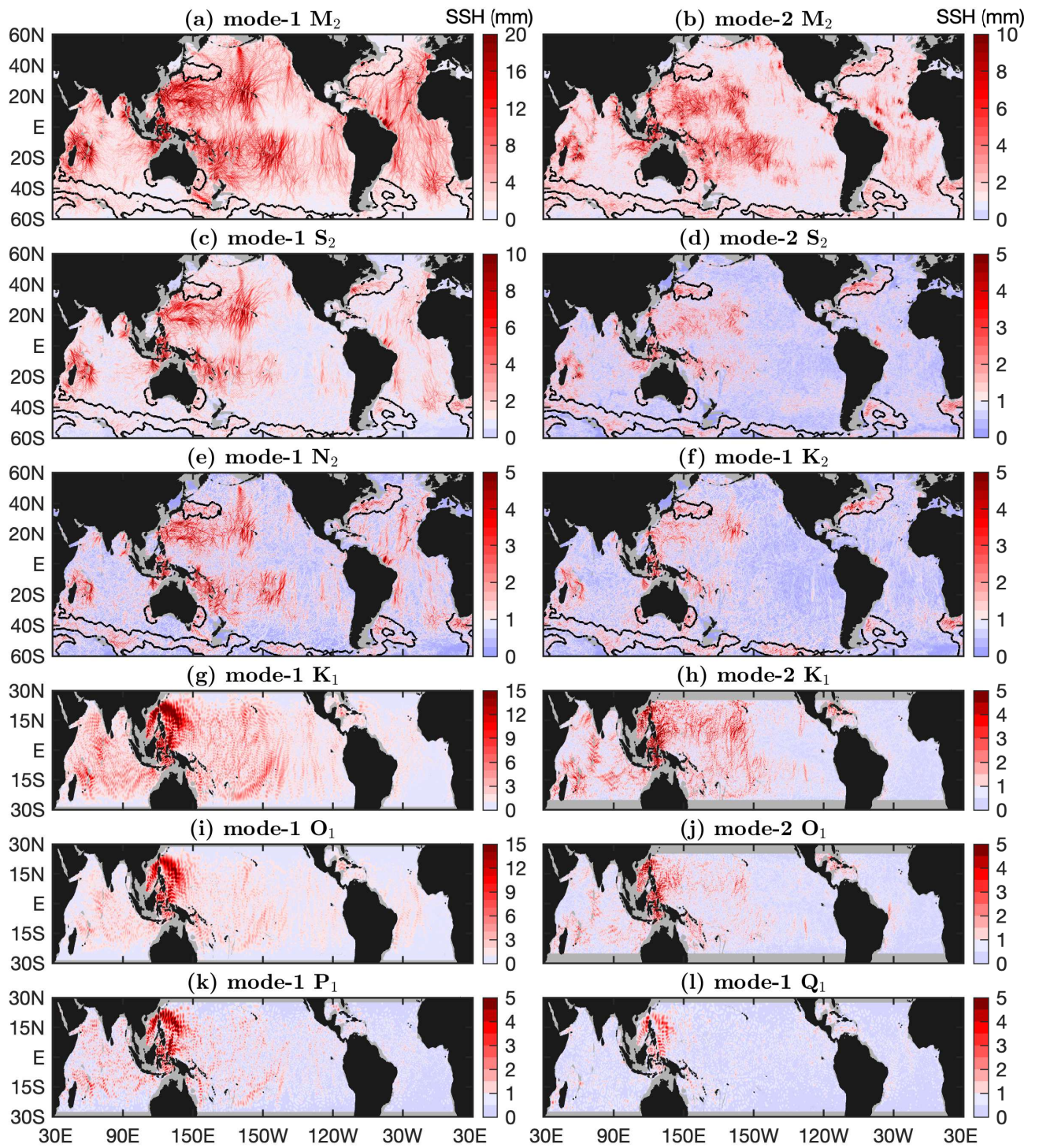


**Figure S1.** Wavelengths of semidiurnal internal tides obtained by solving the Sturm-Liouville orthogonal problem using the climatological annual-mean hydrographic profiles in the World Ocean Atlas 2018 and the dispersion relation of linear internal gravity waves with Earth's rotation.



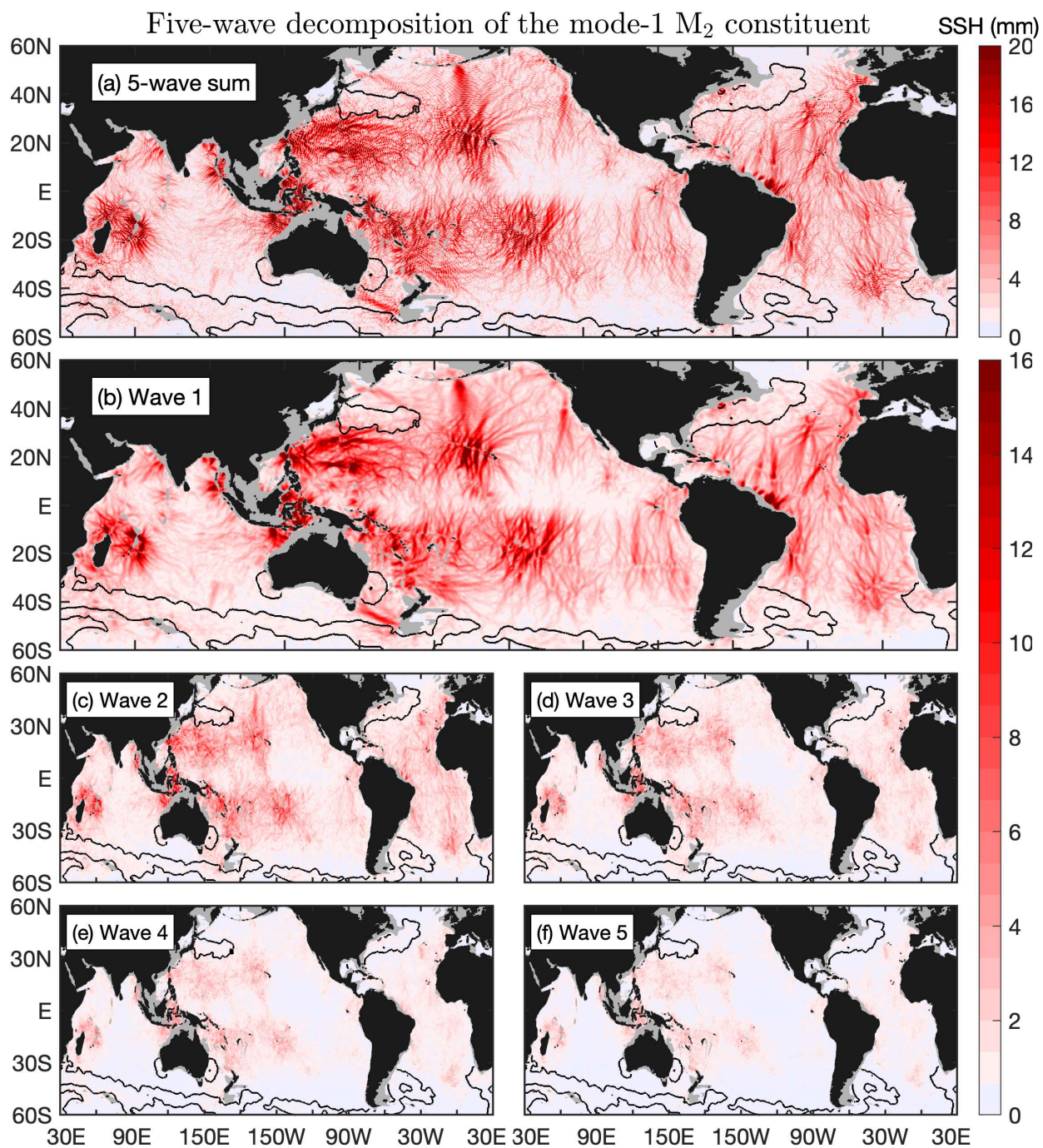
**Figure S2.** As in Figure S1 but for diurnal internal tide constituents.





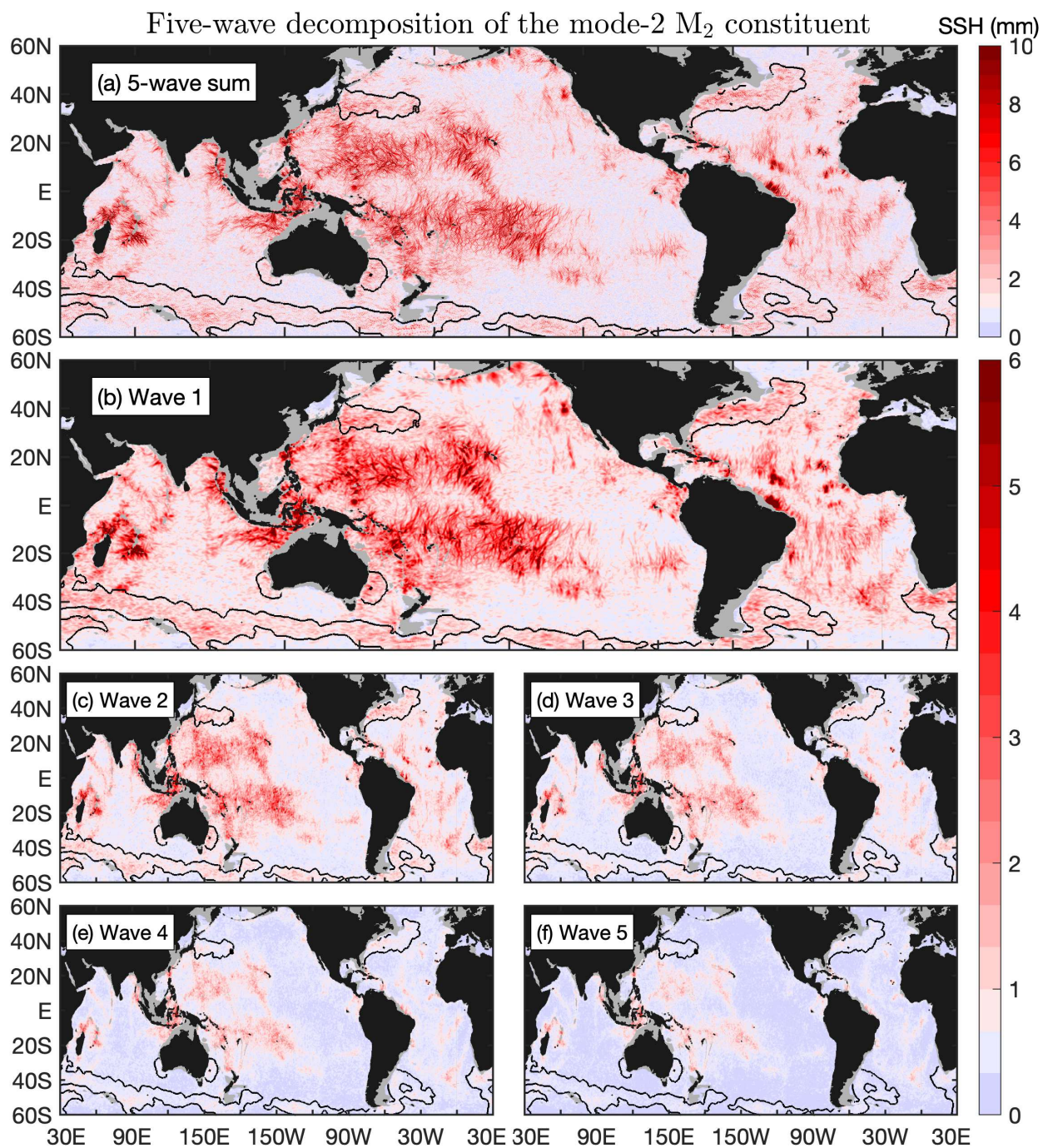
**Figure S3.** Twelve internal tide constituents in ZHAO30yr. Internal tides with amplitudes lower than 1 mm are shown in light blue. Black contours indicate regions of large model errors.





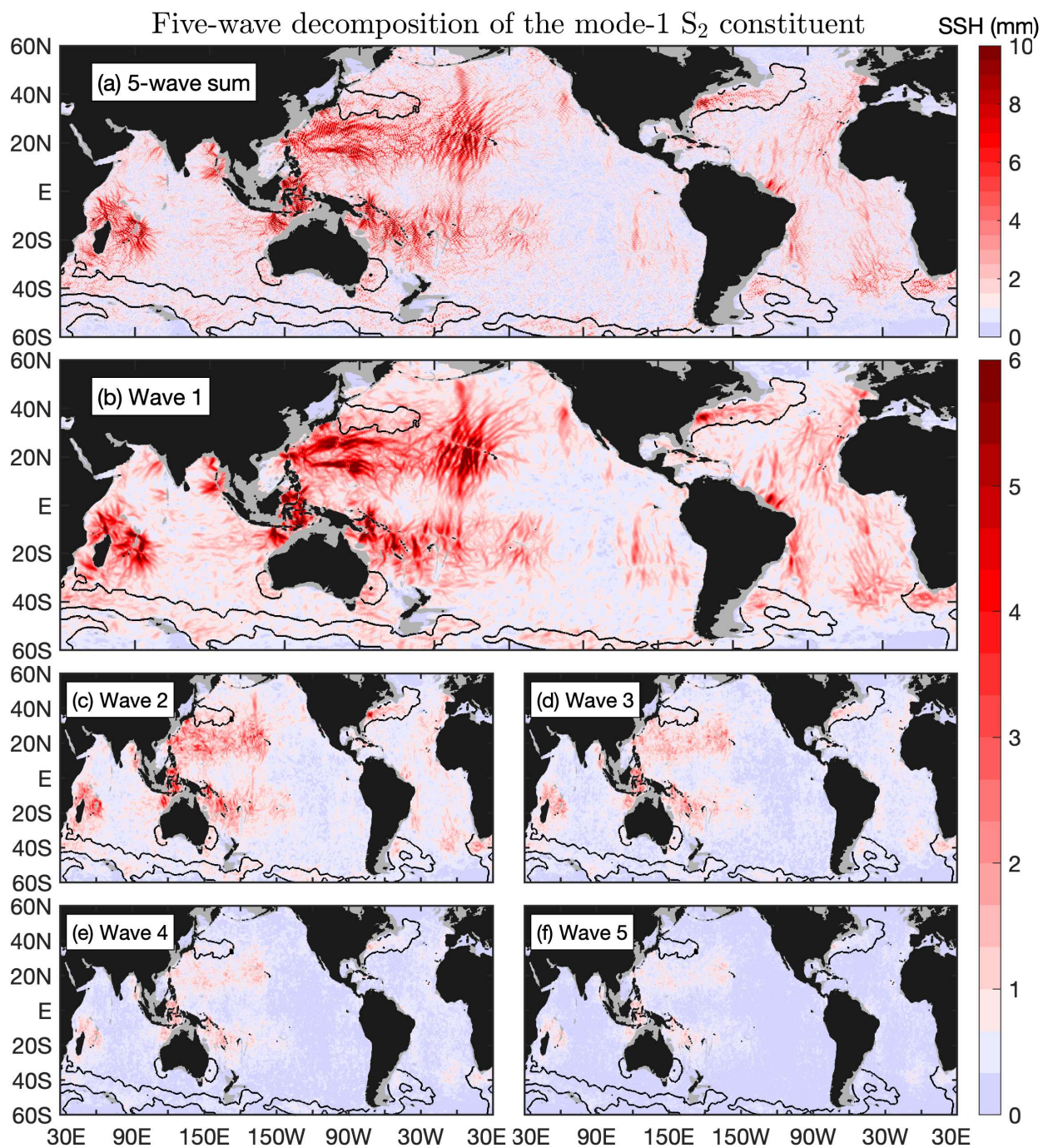
**Figure S4.** Five-wave decomposition of the mode-1  $M_2$  internal tide constituent. (a) The 5-wave sum. (b)-(f) The 5 waves. At each grid point, five mode-1  $M_2$  internal tidal waves in arbitrary horizontal directions are determined by plane wave analysis. Black contours indicate regions of large model errors. Panel (b) shows well-defined long-range internal tidal beams associated with notable topographic features.





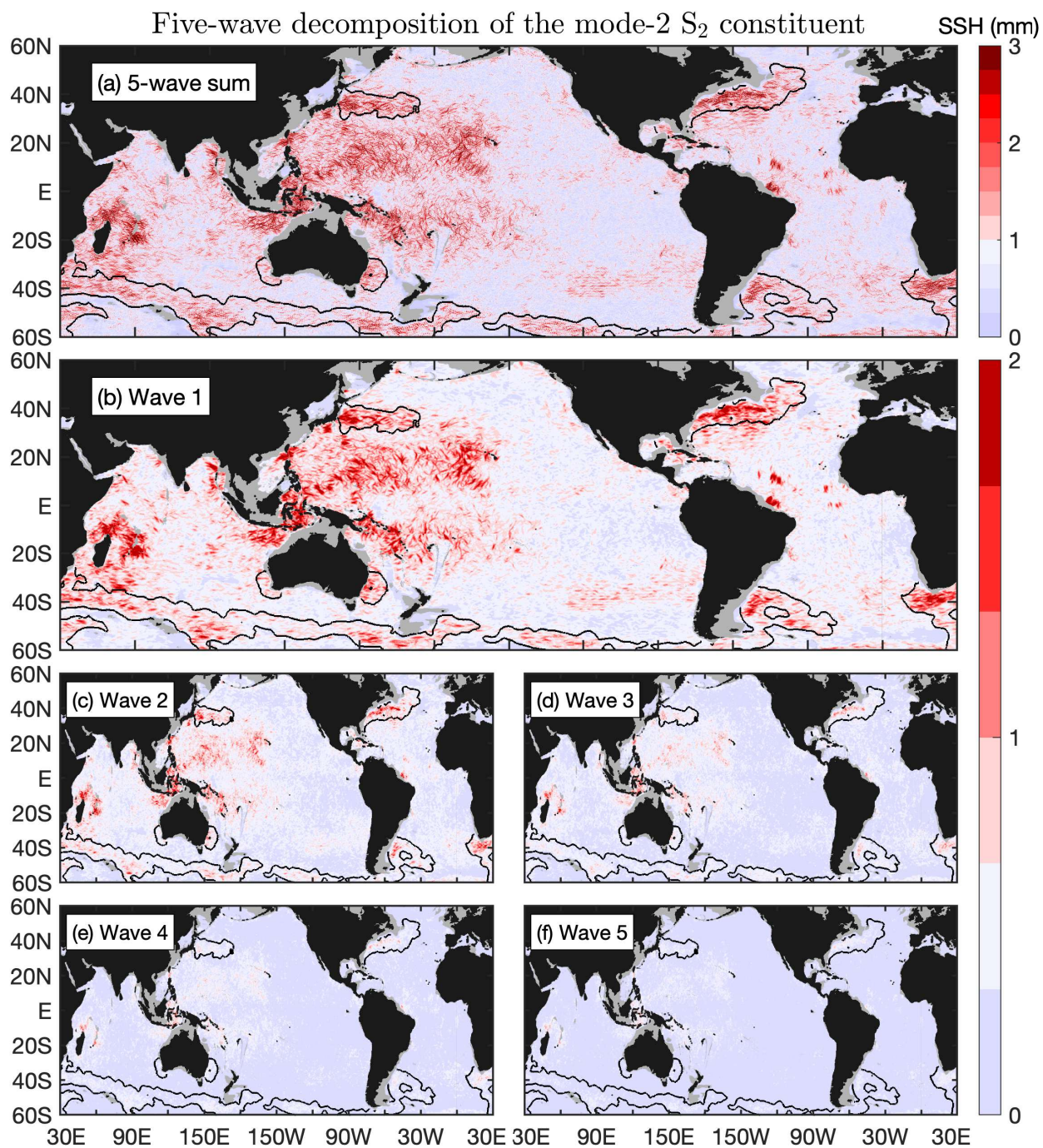
**Figure S5.** As in Figure S4 but for the mode-2  $M_2$  internal tide constituent.





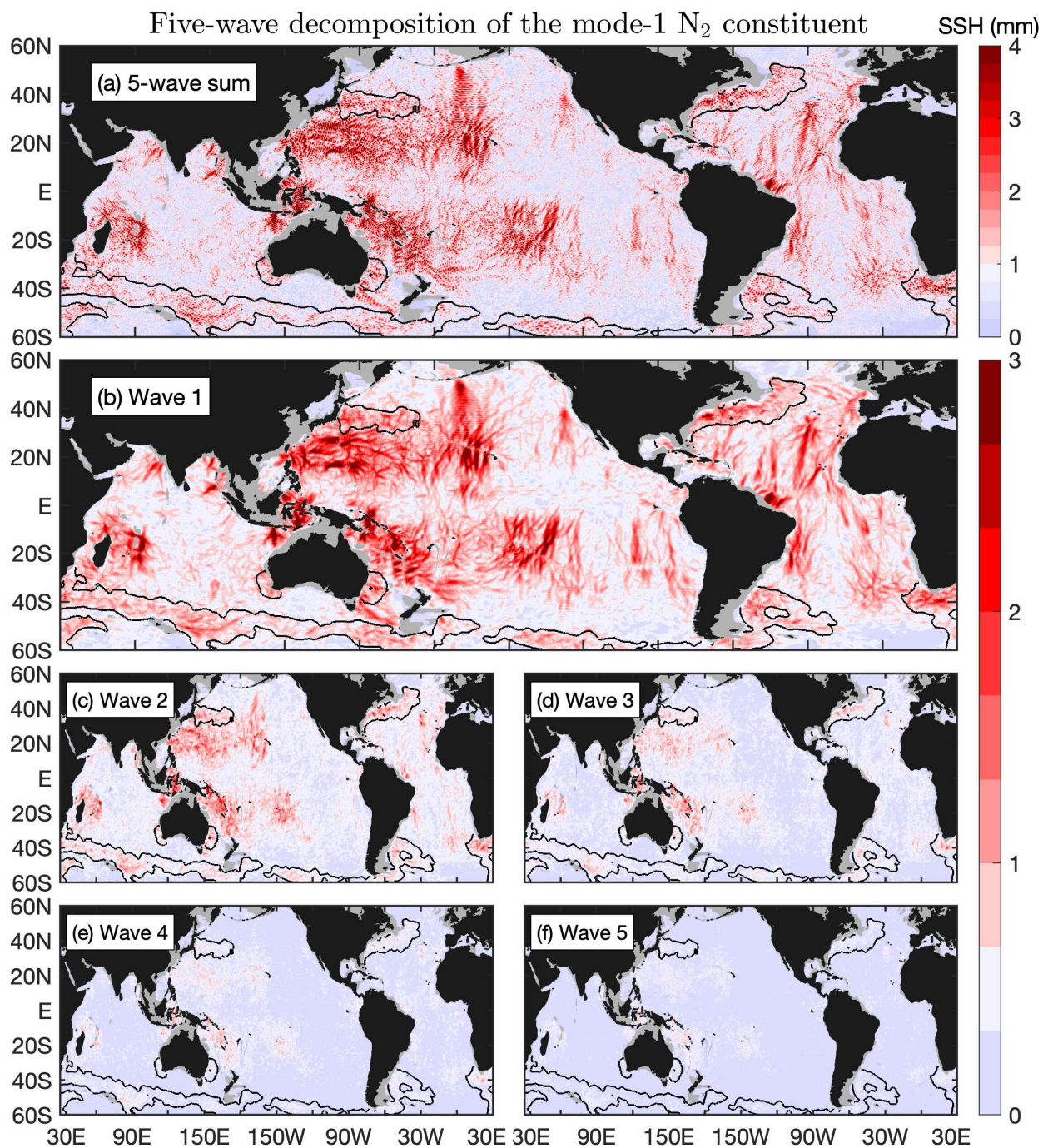
**Figure S6.** As in Figure S4 but for the mode-1  $S_2$  internal tide constituent.





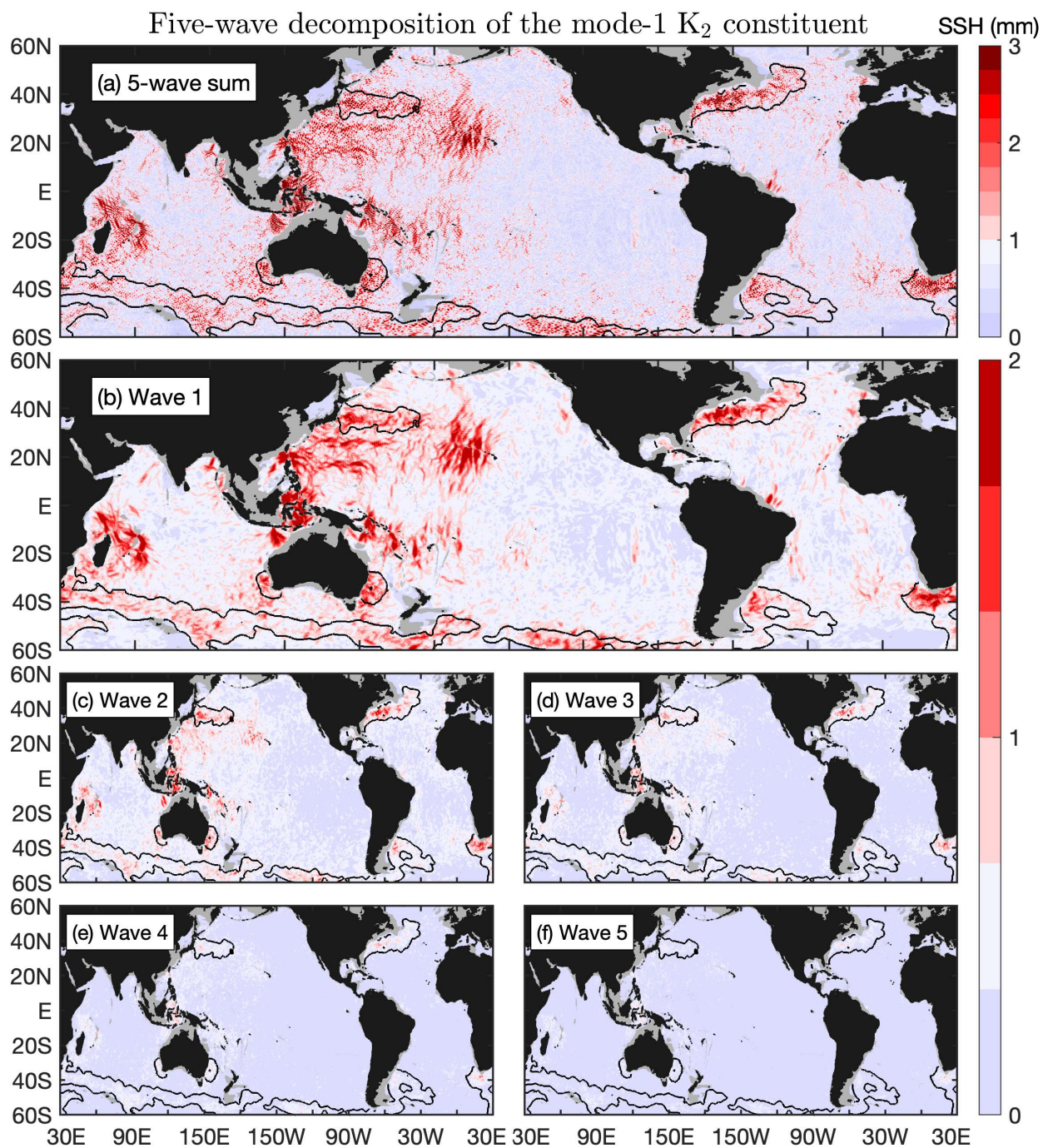
**Figure S7.** As in Figure S4 but for the mode-2  $S_2$  internal tide constituent.





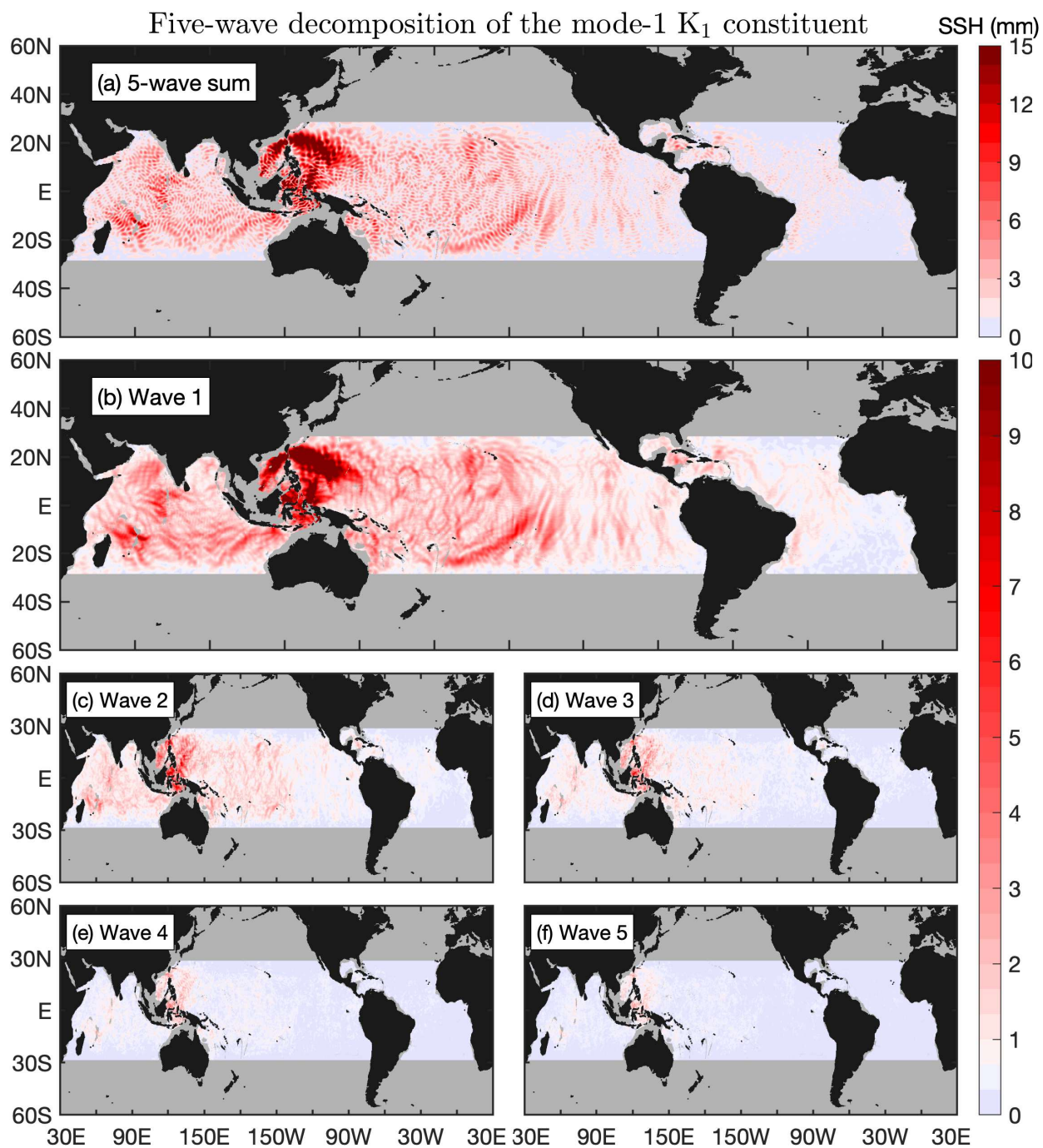
**Figure S8.** As in Figure S4 but for the mode-1  $N_2$  internal tide constituent.



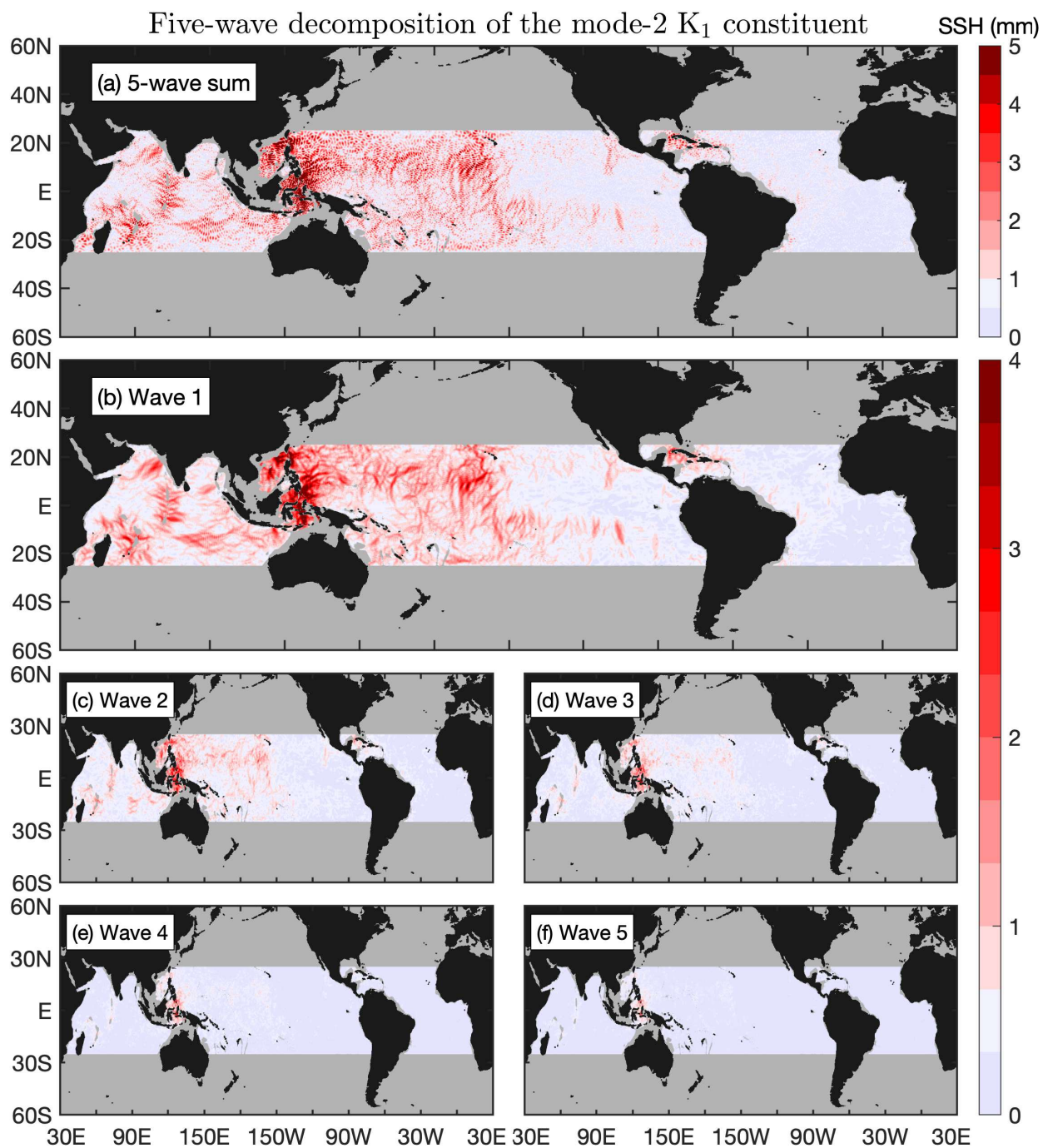


**Figure S9.** As in Figure S4 but for the mode-1  $K_2$  internal tide constituent.

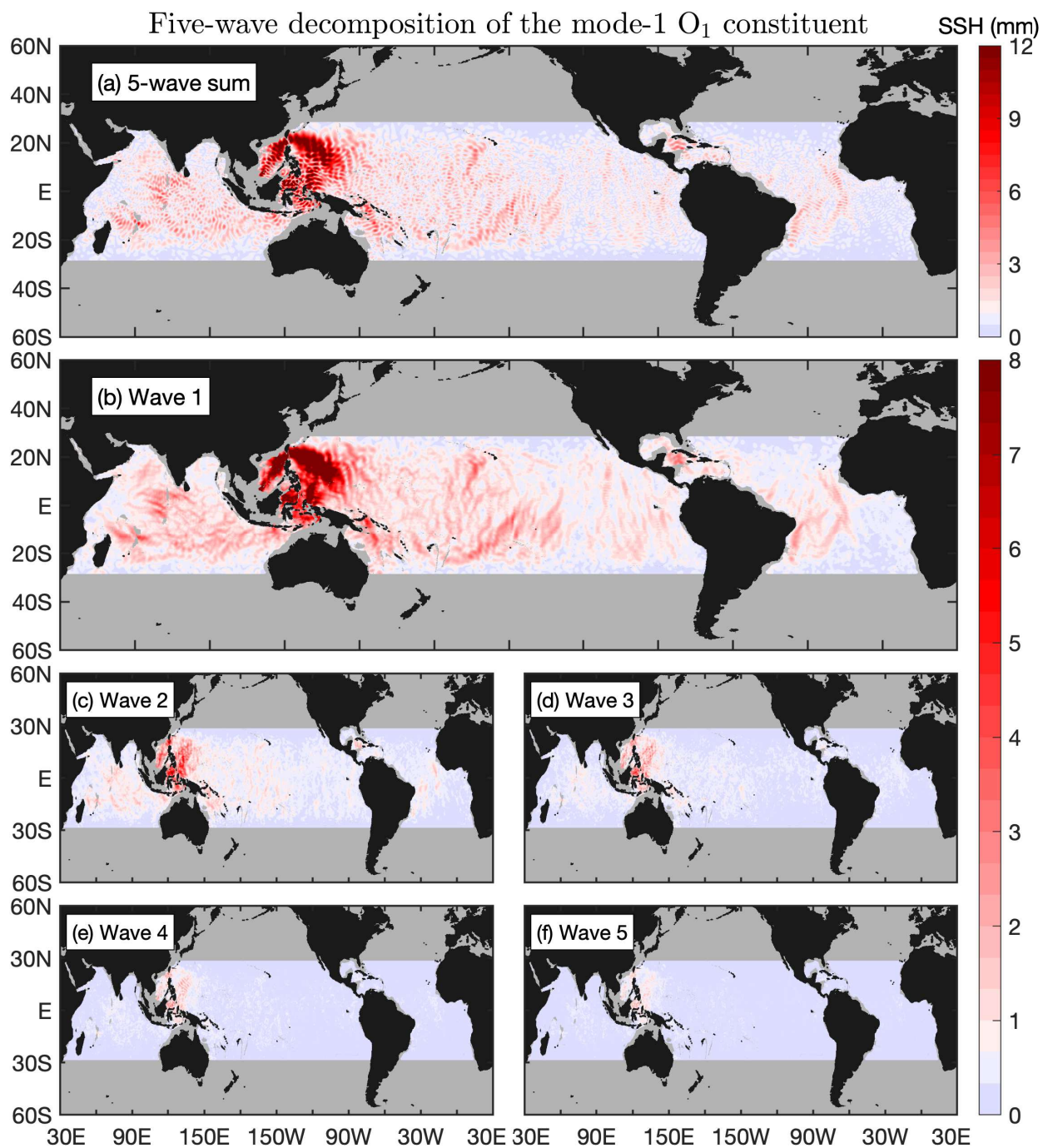




**Figure S10.** Five-wave decomposition of the mode-1  $K_1$  internal tide constituent. (a) The 5-wave sum. (b)-(f) The 5 waves. At each grid point, five mode-1  $K_1$  internal tidal waves in arbitrary horizontal directions are determined by plane wave analysis. Panel (b) shows well-defined long-range internal tidal beams associated with notable topographic features.

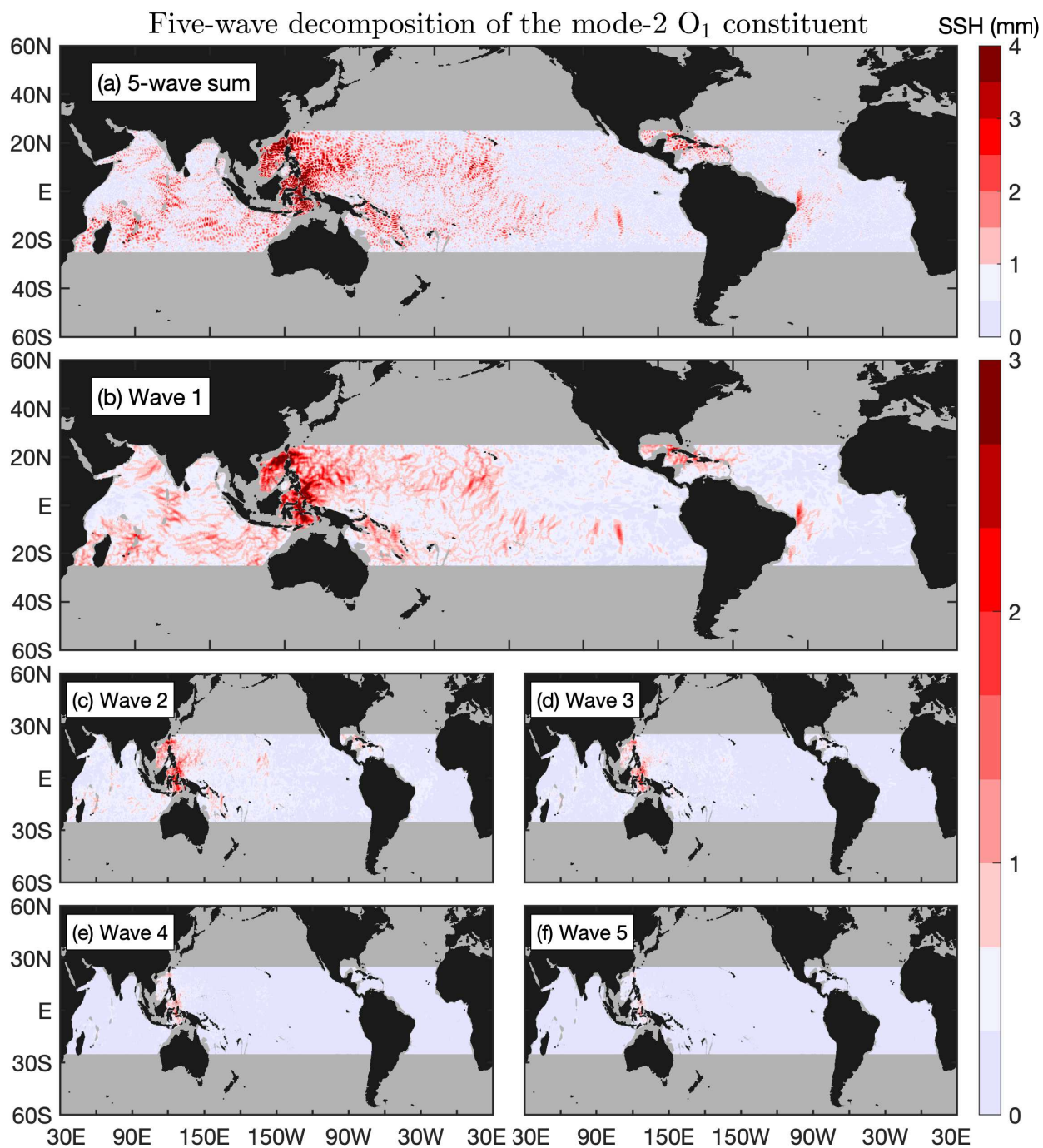


**Figure S11.** As in Figure S10 but for the mode-2  $K_1$  internal tide constituent.

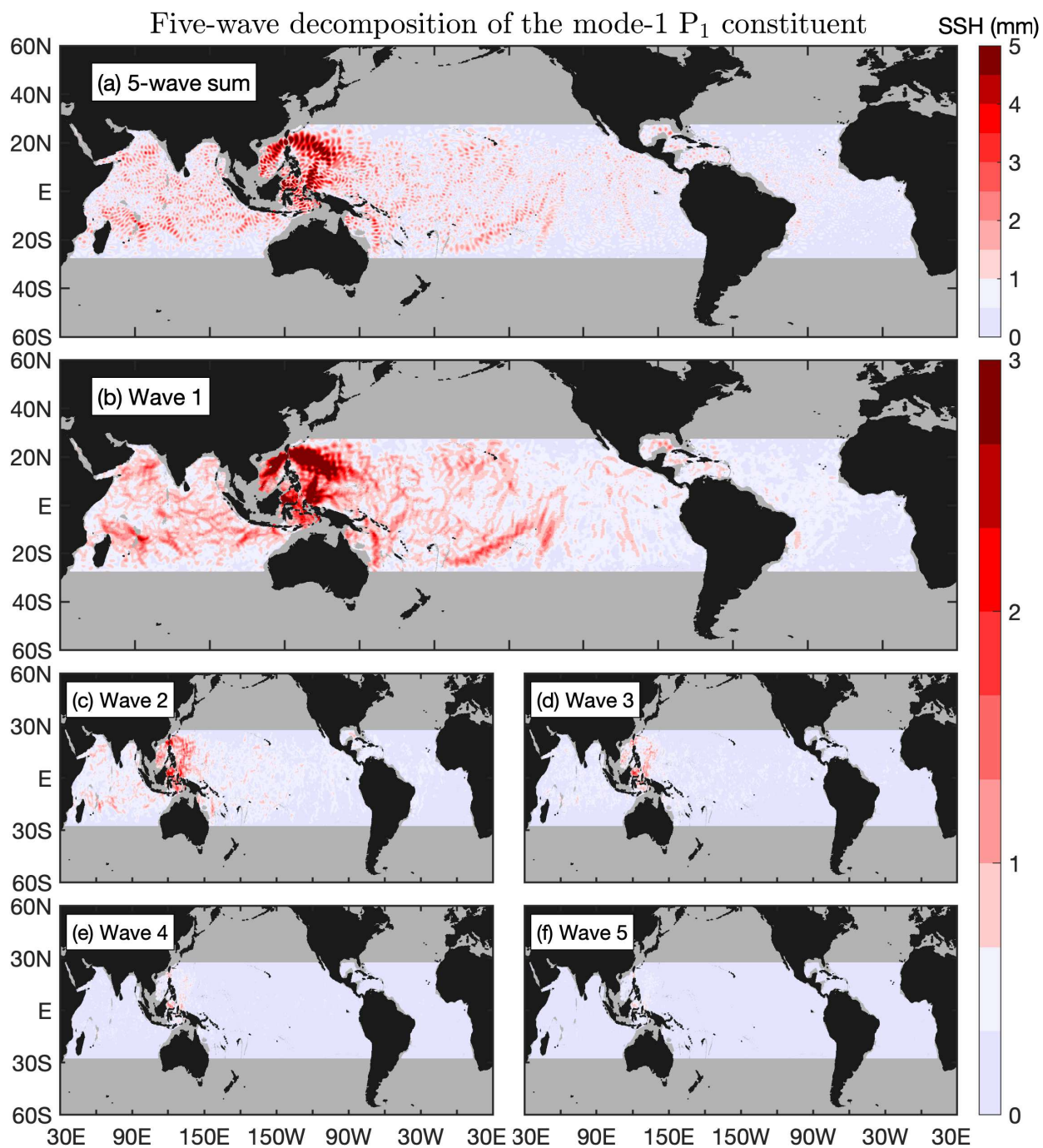


**Figure S12.** As in Figure S10 but for the mode-1  $O_1$  internal tide constituent.

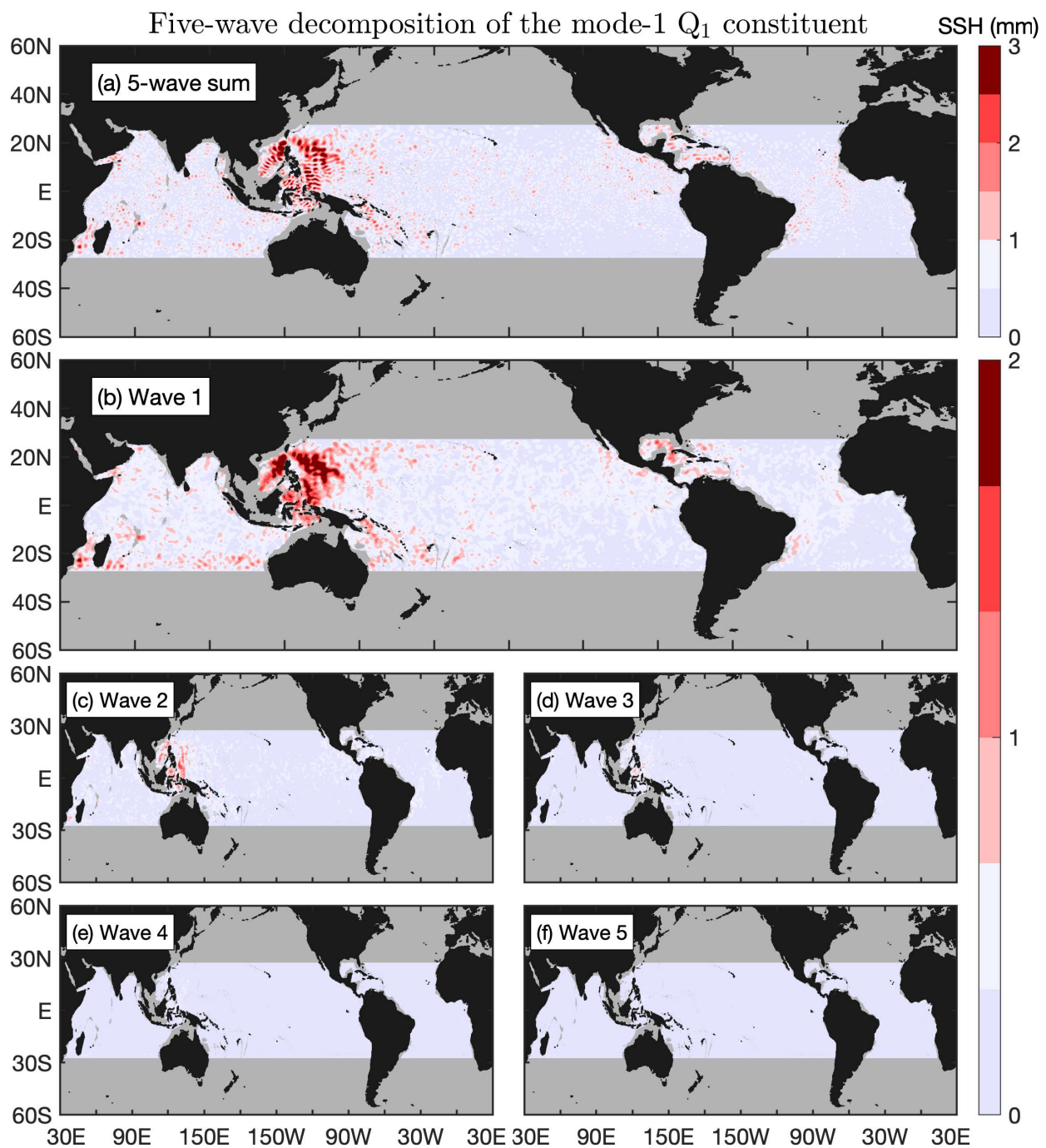




**Figure S13.** As in Figure S10 but for the mode-2  $O_1$  internal tide constituent.

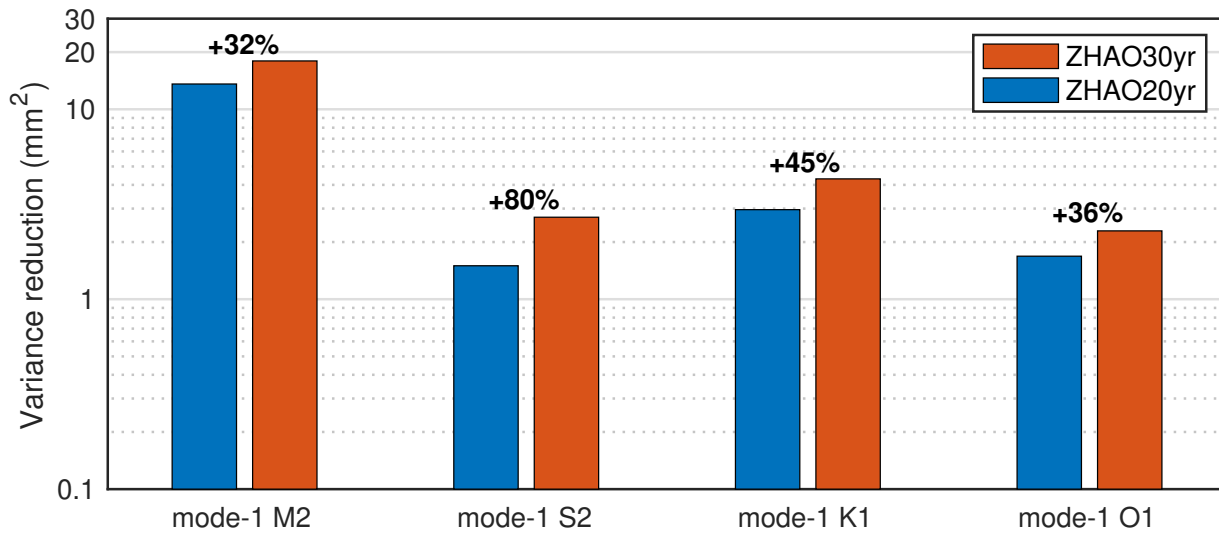


**Figure S14.** As in Figure S10 but for the mode-1  $P_1$  internal tide constituent.

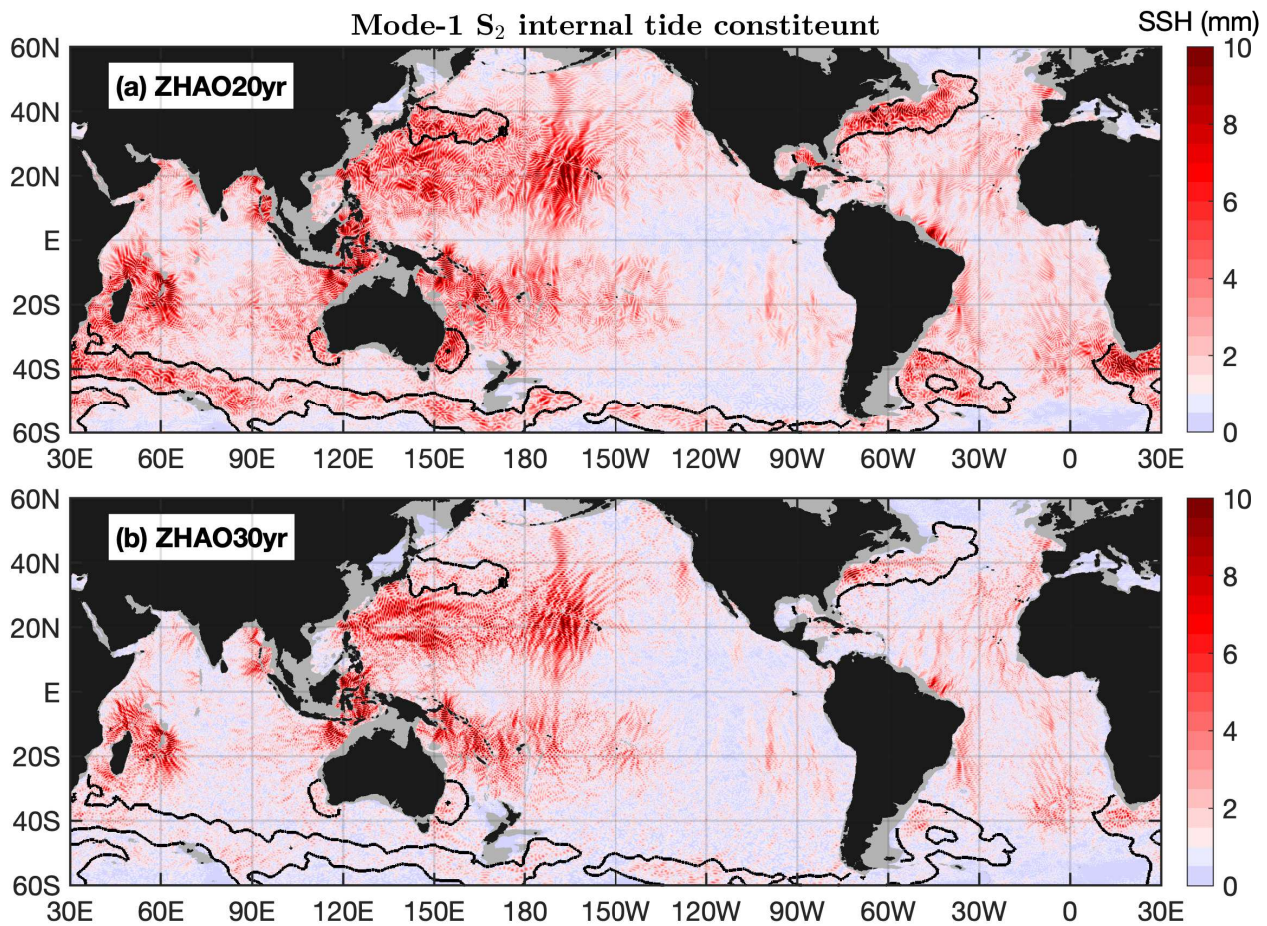


**Figure S15.** As in Figure S10 but for the mode-1  $Q_1$  internal tide constituent.

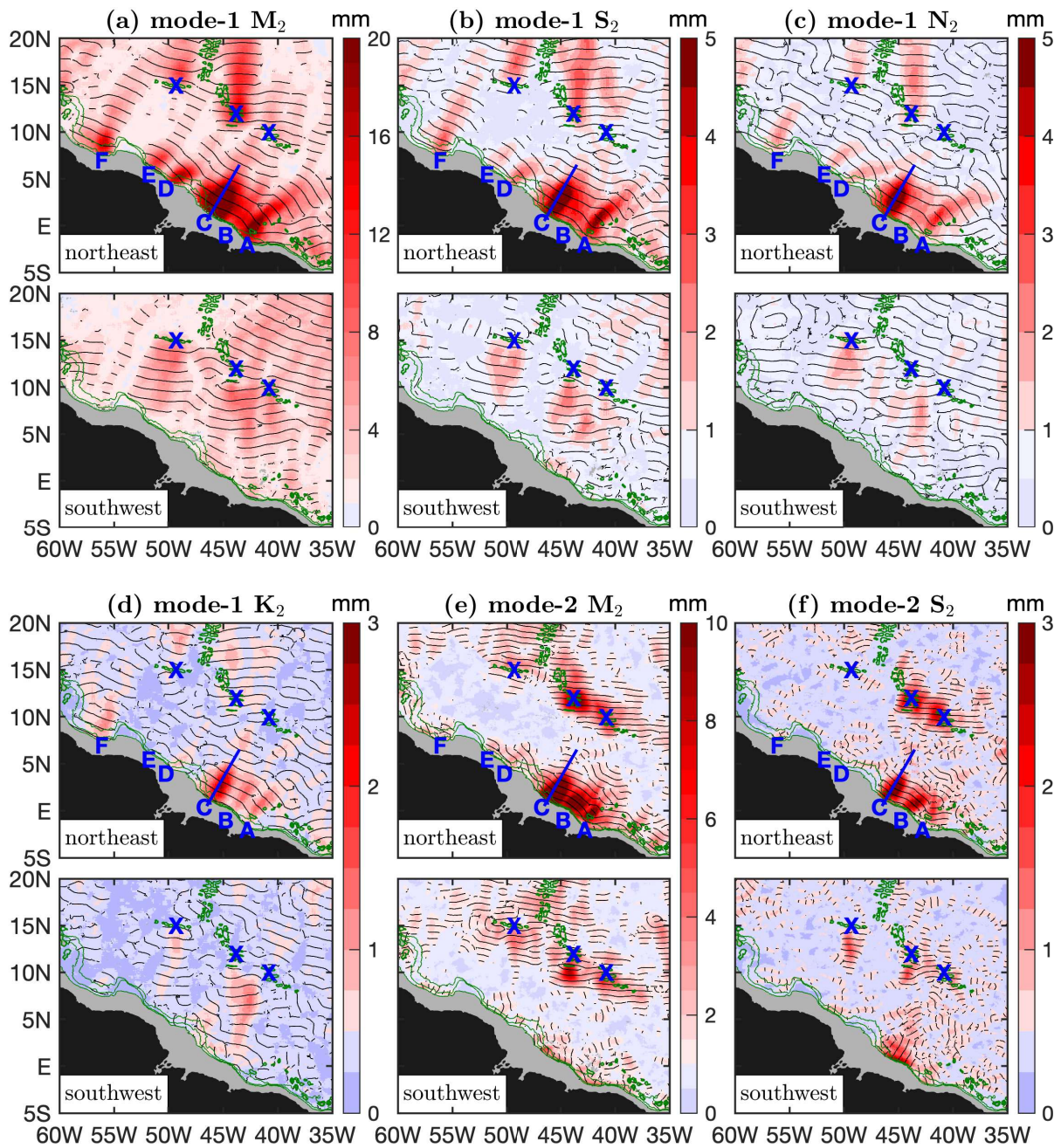




**Figure S16.** Histogram of global area-weighted mean variance reductions caused by ZHAO20yr and ZHAO30y. ZHAO30yr improves over ZHAO20yr by different percentages for different constituents.

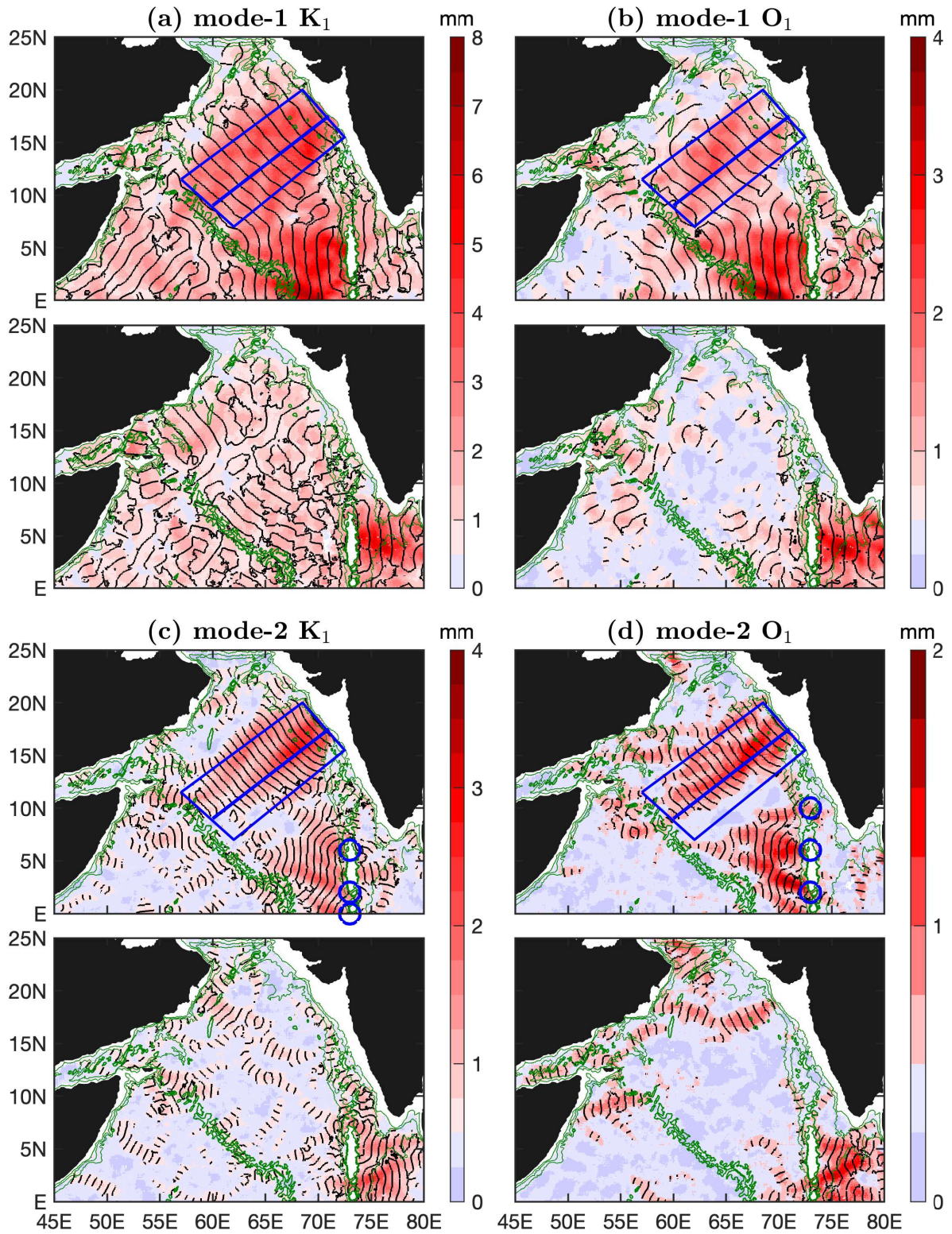


**Figure S17.** Mode-1  $S_2$  internal tide constituents in (a) ZHAO20yr and (b) ZHAO30yr. Black contours indicate regions of large model errors. ZHAO30yr has a higher spatial resolution and lower model errors.



**Figure S18.** Semidiurnal internal tidal beams off the Amazon shelf. Each constituent is divided into northeastward ( $-45^{\circ}$ – $135^{\circ}$ ) and southwestward ( $135^{\circ}$ – $315^{\circ}$ ) components. Black lines indicate the  $0^{\circ}$  co-phase charts. Green contours indicate the 1000-, 2000-, and 3000-m isobaths. Isolated beams off the Amazon shelf are labeled A–F. Blue lines highlight the strongest beams generated at the mouth of the Amazon River. Beams generated at the Mid-Atlantic Ridge are marked.





**Figure S19.** Diurnal internal tidal beams in the Arabian Sea. Each constituent is divided into eastward ( $-90^{\circ}$ – $90^{\circ}$ ) and westward ( $90^{\circ}$ – $270^{\circ}$ ) components. Internal tides with amplitudes lower than 0.5 mm are shown in light blue. Black lines indicate the  $0^{\circ}$  and  $180^{\circ}$  co-phase charts. Green contours indicate the 1000-, 2000-, and 3000-m isobaths. Blue circles mark some isolated mode-2 beams at the Chagos–Laccadive Ridge.