Rainfall erosivity mapping over mainland China based on high-density hourly rainfall records

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Abstract. Rainfall erosivity quantifies the effect of rainfall and runoff on the rate of soil loss. Maps of rainfall erosivity are needed for erosion assessment using the Universal Soil Loss Equation (USLE) and its successors. To improve erosivity maps that are currently available, hourly and daily rainfall data from 2381 stations for the period 1951–2018 were used to generate new R-factor and 1-in-10-year event EI³₀ maps for mainland China (available at https://doi.org/10.12275/bnu.clicia.rainfallerosivity.CN.001; Yue et al., 2020b). One-minute rainfall data from 62 stations, of which 18 had a record length > 29 years, were used to compute the “true” rainfall erosivity against which the new R-factor and 1-in-10-year EI³₀ maps were assessed to quantify the improvement over the existing maps through cross-validation. The results showed that (1) existing maps underestimated erosivity for most of the south-eastern part of China and overestimated for most of the western region; (2) the new R-factor map generated in this study had a median absolute relative error of 16 % for the western region, compared to 162 % for the existing map, and 18 % for the rest of China. The new 1-in-10-year EI³₀ map had a median absolute relative error of 14 % for the central and eastern regions of China, compared to 21 % for the existing map (map accuracy was not evaluated for the western region where the 1 min data were limited); (3) the R-factor map was improved mainly for the western region, because of an increase in the number of stations from 87 to 150 and temporal resolution from daily to hourly; (4) the benefit of increased station density for erosivity mapping is limited once the station density reached about 1 station per 10 000 km².

1 Introduction

Soil erosion has been a major threat to soil health, soil and river ecosystem services in many regions of the world (Pennock, 2019). Soil erosion has on-site impacts, such as the reduction of soil and water, the loss of soil nutrients, the decrease of land quality and food production, as well as off-site impacts, such as excessive sedimentation and water pollution.

Soil erosion models are tools to evaluate the rate of soil loss and can provide policymakers useful information for taking measures in soil and water conservation. The Universal Soil Loss Equation (USLE; Wischmeier and Smith, 1965, 1978) and the Revised USLE (RUSLE; Renard et al., 1997; USDA-ARS, 2013) have been widely used to estimate soil erosion in at least 109 countries over the past 40 years (Alewell et al., 2019). Rainfall erosivity is one of the factors in the USLE and RUSLE to represent the potential ability of rainfall and runoff to affect soil erosion.

In the USLE, erosivity of a rainfall event is identified as the EI value, also denoted as EI³₀, which is the product of the total storm energy (E) and the maximum 30 min intensity (I₃₀) (Wischmeier, 1959). The erosivity factor (R-factor) in the USLE is the mean annual total EI values of all erosive events. To recognize interannual rainfall variability, rainfall data of long periods are required (Wischmeier and Smith, 1978). In
the original isoerodent maps generated by Wischmeier and Smith (1965), stations with rainfall data of at least 22 years were used.

To use the USLE, two additional input parameters are required. One is the seasonal distribution of the \( R \)-factor. To compute the soil erodibility factor (\( K \)-factor) and cover-management factor (\( C \)-factor), seasonal distribution of \( E_I \) (monthly, Wischmeier and Smith, 1965; or half-month percentage of \( E_I \), Wischmeier and Smith, 1978; Renard et al., 1997) is needed. In addition, 1-in-10-year storm \( E_I \) value (called “10-yr \( E_I \)” in Renard et al., 1997) is needed to compute the support practice factor (\( P \)-factor) for the contour farming (Renard et al., 1997).

Kinetic energy generated by raindrops can be calculated based on raindrop disdrometer data and estimated based on breakpoint or hyetograph data via \( K \)-equations, while \( P \) based on raindrop disdrometer data and estimated based on the same data as Wischmeier and Smith (1965) for the eastern farming (Renard et al., 1997).

Recently, the Food and Agriculture Organization (FAO) proposed to produce a Global Soil Erosion Map (GSErmap) which encouraged scientists around the world to generate their own national level maps making the most of the country knowledge, locally available methods and input data (FAO, 2019). Rainfall erosivity maps for China were reviewed, and relevant information on how they were generated is presented in Table 1, which shows that current \( R \)-factor maps for mainland China typically used readily available daily rainfall data from about 500–800 stations (e.g. Zhang et al., 2003; Liu et al., 2013; Qin et al., 2016; Yin et al., 2019; Liu et al., 2020), which were recorded by simple rain gauges. However, daily rainfall data are not enough to derive sub-daily intensities, which reduced the accuracy of estimated rainfall erosivity (Yin et al., 2015). One-minute data are the finest-resolution data measured by automatic tipping bucket rain gauges we can obtain up to now; therefore they are one of the best datasets for deriving precipitation intensity and estimating rainfall erosivity. However, 62 stations with 1 min data collected were inadequate for the spatial interpolation of rainfall erosivity over mainland China. Hourly data were believed to reflect the temporal variation of precipitation intensity better than daily data, which can be used to improve the estimation of at-site rainfall erosivity with precipitation observations. In addition, the increase of station density for the interpolation can better describe the spatial variation of rainfall erosivity and improve the estimation of rainfall erosivity for areas without observations together with the improvement of interpolation models and procedures.

Therefore hourly and daily data for more than 2000 stations were collected, together with the 1 min data for 62 of them to do the following: (a) develop high-quality maps of the \( R \)-factor and 1-in-10-year \( E_I \) over the mainland China; (b) quantify the improvement of the new erosivity maps using precipitation data in a higher temporal resolution and from more weather stations, and better interpolation techniques compared to those used to generate erosivity maps that are currently available (Yin et al., 2019). New \( R \)-factor and 1-in-10-year \( E_I \) maps were produced in this study may improve the estimation of the soil loss in mainland China. The meaning and rationale of the study is to (1) present and share high-precision maps of the \( R \)-factor and 1-in-10-year \( E_I \) over the mainland China with related Earth system science communities and (2) provide some insights into the improvement of rainfall erosivity maps for other regions.


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2 Data and methods

2.1 Data

2.1.1 Rainfall data

Rainfall data were obtained at the daily, hourly and 1 min intervals.

Daily rainfall data from 2381 meteorological stations over mainland China (Fig. 1) over the period of 1951–2014 were measured with simple rain gauges. The data were collected and quality controlled by the National Meteorological Information Center of China Meteorological Administration. Daily data were collected all year around at these stations. An effective year of the daily data was defined as a year when there were no missing data for 1 or more months in the year, and a missing month was defined as a month when there were more than 6 missing days in the month. The missing records in the effective years were input as zero. Based on this definition, the number of effective years ranged from 18 to 54 years. Most of the stations (88 %) have data for more than 50 years.

Hourly rainfall data from the same 2381 stations with daily data (Fig. 1) were collected by siphon rain gauges or tipping bucket rain gauges and also quality controlled by the National Meteorological Information Center of China Meteorological Administration. The period of record for hourly data was from 1951 to 2018. The start year of the data varied because data collection commenced in different years. Observation was suspended in the snowy season, which resulted in some missing months in winter for stations in the northern part of China. There were 932 (39 %) stations with data for the whole year, 550 (23 %) stations from April to October and 421 (18 %) stations from May to September.

The missing data were handled according to the following criteria: (a) a day with more than 4 missing hours was defined as a missing day; (b) a month with more than 6 missing days was defined as a missing month; (c) a year with any missing month in its wet season was defined as a missing year. The wet season for stations north of 32 °N was from May to September, and for those south of 32 °N was from April to October. Missing years were removed, and missing hours in the remaining effective years were input into two categories: (a) the missing period is followed by a non-zero record, which recorded the accumulated rainfall amount in the missing period based on data notes; (b) the missing period is followed by zero. In the first case, each missing hour and the following non-zero hour were assigned the mean value of the non-zero record in these hours. For the second case, the missing hours were input as zero value.

Data at 1 min intervals were collected from 62 stations in mainland China (Fig. 2; and were used in Yue et al., 2020a). Data from station No. 1–18 have effective years of 29–40 and cover the period of 1961(1971)–2000. Data from stations No. 19–62 have effective years of 2–12 and cover the period
of 2005–2016. The missing data in the effective years were assumed to be zero.

2.1.2 Published rainfall erosivity maps for China

The existing rainfall erosivity maps were collected and compared with the maps generated in this study. The current national $R$-factor map and 1-in-10-year EI$_{30}$ map are based on daily rainfall data only over the period from 1961 to 2016 from 774 stations in China (Yin et al., 2019). Another $R$-factor map shown in the discussion section of this study (Fig. 12) was based on the global rainfall erosivity dataset published by Joint Research Centre – European Soil Data Centre (ESDAC; Panagos et al., 2017).

2.2 Calculation of rainfall erosivity using 1 min, hourly and daily data

One-minute and hourly data were first separated into storm events. A continuous period of $\geq 6$ h of no-precipitation was used to separate storms (Wischmeier and Smith, 1978). Storms with the amount of $\geq 12$ mm were defined as erosive events (Xie et al., 2000) and were used to calculate the rainfall erosivity factors.

The $R$-factor was calculated using Eqs. (1)–(3) (USDA-ARS, 2013):

$$R = \frac{1}{N} \sum_{i=1}^{N} \sum_{j=1}^{m} (EI_{30})_{ij},$$

$$E = \sum_{i=1}^{l} (e_r \cdot P_r),$$

$$e_r = 0.29 \left[ 1 - 0.72 \exp(-0.082i_r) \right],$$

where $EI_{30}$ (event rainfall erosivity, MJ mm ha$^{-1}$ h$^{-1}$) is the product of the total storm energy $E$ (MJ ha$^{-1}$) and the maximum 30 min intensity $I_{30}$ (mm h$^{-1}$); $i = 1, 2, \ldots, N$, where $N$ is the number of effective years, and $j = 1, 2, \ldots, m$ means there are $m$ erosive storm events in the $i$th year. For each storm event, rainfall was divided into $l$ time intervals depending on the temporal resolution of rainfall data. The total storm energy $E$ was the sum of the energy for each time interval $r$, which was the unit energy $e_r$ (energy per mm of rainfall, MJ mm$^{-1}$ mm$^{-1}$) multiplied by the rainfall amount $P_r$ (mm) for each time interval. And $i_r$ was the intensity (mm h$^{-1}$) of the $r$th interval. $I_{30}$ (mm h$^{-1}$) was the maximum intensity over 30 consecutive minutes for each storm event. For hourly data, the $I_{30}$ was assumed to be the same as the maximum 1 h intensity.

The 1-in-10-year EI$_{30}$ with 1 min or hourly data was obtained by fitting the generalized extreme value distribution (GEV). The GEV distribution is a family of probability dis-
Spatial distribution of the stations with 1 min rainfall data.

Figure 2. Spatial distribution of the stations with 1 min rainfall data.

tributions of Gumbel, Fréchet and Weibull, and it can be de-
noted as $G(\mu, \sigma, \xi)$ with parameters $\mu$ (location), $\sigma$ (scale),
and $\xi$ (shape) (Coles, 2001):

$$G(z) = \exp \left\{ -\left[ 1 + \frac{x - \mu}{\sigma} \right]^{-\frac{1}{\xi}} \right\} \{ x : 1 + \xi (x - \mu) / \sigma > 0 \},$$

(4)

where $x$ is the annual maximum storm $E_{30}$ (MJ mm ha\(^{-1}\) h\(^{-1}\)), $-\infty < \mu < \infty$, $\sigma > 0$ and
$-\infty < \xi < \infty$. The extreme quantiles of the annual
maximum $E_{30}$ ($X_p$) can be obtained by inverting Eq. (4):

$$X_p = \begin{cases} \mu - \frac{\sigma}{\xi} [1 - (-\log(1 - p))^{-\xi}] & \text{for } \xi \neq 0, \\ \mu - \sigma \log(-\log(1 - p)) & \text{for } \xi = 0 \end{cases},$$

(5)

where $G(X_p) = 1 - p$. The 1-in-10-year $E_{30}$ was the value
of $X_p$ when $p$ was 1/10.

Parameter values for the GEV distribution were estimated
using daily data was the mean annual daily erosivity. Daily
rainfall erosivity was obtained by the following equation de-
volved by Xie et al. (2016):

$$R_{\text{daily}} = \alpha P_{\text{daily}}^{0.7265},$$

(6)

where $P_{\text{daily}}$ is the daily precipitation (\(\geq\) 10 mm) and param-
eter $\alpha$ is 0.3937 in the warm season (May to September) and
0.3101 in the cold season (October to April).

The 1-in-10-year $E_{30}$ using daily data was the 1-in-10-
year daily erosivity adjusted with a conversion factor of 1.17
based on 1 min data from 18 stations in China (Yin et al.,
2019). And the 1-in-10-year daily erosivity was obtained by
-calibrating the GEV distribution parameters as Eqs. (4)–(5)
and the $x$ in the functions was replaced by the annual maxi-
mum daily erosivity.

2.3 Rainfall erosivity for individual stations

Hourly data from 2381 stations were used to produce the
$R$-factor and the 1-in-10-year $E_{30}$ maps. Due to the annual
variability of rainfall erosivity, stations with less than 22 ef-
effective years should be excluded (Wischmeier and Smith,
1978). However, 133 out of 150 stations in western China
have less than 22 effective years (Fig. 1). Once these stations
are removed, the western stations would be too sparse, which
would reduce the interpolation accuracy of the rainfall er-
sivity map. To fill the gap due to the insufficient number of
years, daily rainfall data with longer periods of record were
used to adjust erosivity values based on hourly data at the same station.

When the effective years of hourly data were not less than those of daily data for 871 out of 2381 station, no adjustment of the \( R \)-factor was made. For the remaining 1510 stations, the \( R \)-factor from hourly data was then adjusted by a relationship between the mean annual rainfall and the \( R \)-factor computed with hourly data as follows (Zhu and Yu, 2015):

\[
R_{h,\text{adj}} = R_{\text{hour}} \left( \frac{P_d}{P_h} \right)^{1.481},
\]

(7)

where \( R_{h,\text{adj}} \) is the adjusted \( R \)-factor, \( R_{\text{hour}} \) is the estimated \( R \)-factor using hourly rainfall data, \( P_d \) is the mean annual precipitation of longer period (period of the daily data), and \( P_h \) is the mean annual precipitation of shorter period (period of the hourly data).

The exponent value of 1.481 was estimated based on a power relationship between the mean annual precipitation and the \( R \)-factor, and the latter was determined using 1 min and daily rainfall data of 35 stations in China (Fig. 2). All the daily and 1 min data shared common periods of record of more than 10 years.

\[
R_{\text{min}} = 0.156 \cdot P_m^{1.481},
\]

(8)

where \( R_{\text{min}} \) is the \( R \)-factor (MJ mm ha\(^{-1}\) h\(^{-1}\) a\(^{-1}\)), and \( P_m \) is the mean annual precipitation (mm) using 1 min data. The coefficient of determination \((R^2)\) is 0.776 for Eq. (8).

The 1-in-10-year EI\(_{30}\) for the stations was adjusted in a similar fashion. No adjustment is needed for 89% of the stations where the effective years of the hourly data were not less than 22 years. For the remaining 11% of the station, the 1-in-10-year EI\(_{30}\) was estimated with daily data.

The record length was 22 to 29 years for 16 (0.7%) stations, 30 to 39 years for 44 (1.8%) stations, 40 to 49 years for 216 (9.1%) stations, more than 50 years for 2105 (88.4%) stations when these adjustments were made.

2.4 Spatial interpolation and cross-validation

The erosivity maps were obtained using the method of universal kriging with the annual rainfall as a co-variable. The mean annual rainfall was computed using daily rainfall data and was interpolated using ordinary kriging, and interpolated mean annual rainfall was then used to interpolate the \( R \)-factor value using universal kriging. Both the mean annual precipitation and the erosivity factor were interpolated first for each of the four regions separately (Fig. 1; Li et al., 2014) and then combined to obtain annual precipitation and erosivity maps over China. Buffer areas were used to avoid discontinuity along region boundaries (Li et al., 2014).

To evaluate the efficiency of interpolation models, a leave-one-out cross-validation method was applied to each region. Symmetric mean absolute percentage error (sMAPE) and Nash–Sutcliffe coefficient of efficiency (NSE) were used for the assessment:

\[
s\text{MAPE} = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{F_i - A_i}{(F_i + A_i) / 2} \right| \times 100\%,
\]

(9)

\[
\text{NSE} = 1 - \frac{\sum_{i=1}^{n} (A_i - F_i)^2}{\sum_{i=1}^{n} (A_i - \bar{A})^2},
\]

(10)

where \( n \) is the number of stations, \( F_i \) is the estimated value through universal kriging for the \( i \)th station using data from surrounding stations and \( A_i \) is the observed value at the \( i \)th station.

2.5 Accuracy assessment of erosivity maps

To evaluate the accuracy of the new erosivity maps, erosivity factors using 1 min data were assumed as the “true” values to calculate relative errors since they are most accurate. For the \( R \)-factor, 1 min data for 62 stations were used. For 1-in-10-year EI\(_{30}\), 1 min data for 18 stations (No. 1–18; Fig. 2) of the 62 stations with more than 22 years were used. The cross-validation results for these stations from the interpolation of the two erosivity maps were compared to the values from 1 min data to calculate relative errors. Since the relative error tends to be high for stations with small \( R \)-factor values, the overall relative error for erosivity maps was represented with the median of the absolute value of the relative error for all the stations.

2.6 Comparative evaluation of the existing and new erosivity maps

Existing erosivity mapping at the national scale in mainland China usually uses daily rainfall data from about 500–800 stations. The \( R \)-factor and 1-in-10-year EI\(_{30}\) maps of Yin et al. (2019) were taken as references to evaluate the improvement in the accuracy of the erosivity maps generated in this study. Their relative errors were also obtained with 1 min data as described above.

New erosivity maps in this study followed a procedure that is different from Yin et al. (2019) mainly in three aspects: (1) temporal resolution (hourly vs. daily); (2) number of stations (2381 stations vs. 744 stations); (3) interpolation method (universal kriging vs. ordinary kriging).

To evaluate the effect of the temporal resolution on \( R \)-factor and 1-in-10-year EI\(_{30}\), data from the same set of stations were used, and the only difference was that in temporal resolution. Hourly and daily rainfall data with the same period as the 1 min data at the 62 stations were used to calculate \( R \)-factors and 1-in-10-year EI\(_{30}\) respectively. Erosivity factors from 1 min data are regarded as the most accurate values. The relative errors of erosivity factors from daily and hourly data were computed for evaluating accuracy.
To evaluate the effect of station density, maps were compared with the only difference in the number of stations. Hourly data from 774 stations (the same set of stations in Yin et al., 2019) and from 2381 stations (used in this study) were used to generate two separate erosivity maps. R-factor and 1-in-10-year E10 values were compared using a leave-one-out cross-validation method region by region. The sMAPE was calculated for accuracy assessment.

To evaluate the effect of interpolation methods, maps were compared with the only difference in interpolation methods. Ordinary kriging and universal kriging with the mean annual rainfall as the co-variable were applied for the R-factor and 1-in-10-year E10 computed using hourly data from 2381 stations. Both interpolation methods were applied to each of four different regions as shown in Fig. 1, and leave-one-out cross-validation results were compared. The sMAPE was calculated to evaluate the accuracy of interpolated values.

The framework of this study is shown in Fig. 3.

3 Results

3.1 Accuracy evaluation on erosivity maps

With erosivity maps from Yin et al. (2019) as references, this study shows improvement in the accuracy of estimated R-factor and 1-in-10-year E10 (Figs. 4 and 5; Table 2). The spatial distribution of the absolute relative errors of the maps from this study is shown in Fig. 6.

The R-factor values in the map of Yin et al. (2019) were underestimated where the R-factor was relatively high and overestimated where the R-factor was relatively low. The improvement was particularly noticeable for western China (R < 1000 MJ mm ha\(^{-1}\) h\(^{-1}\) a\(^{-1}\)) and the southeastern coastal region (R > 10 000 MJ mm ha\(^{-1}\) h\(^{-1}\) a\(^{-1}\)).

Relative errors of erosivity factors at the stations from the two maps are shown in Fig. 5a and b. Those with the relative error of more than 100% were all in the western (W) or mid-western (MW) region. The absolute relative error for the R-factor in this study and Yin et al. (2019) was no more than 19% for mid-western (MW), north-eastern (NE) and south-eastern (SE) regions (Table 2). However, there are some extremely high relative error values in Yin’s map which were found to be located in the MW region (Fig. 5a). The median values of the absolute relative error in the R-factor in western (W) region were 16.2% and 161.6%, respectively, for this study and Yin et al. (2019). For 1-in-10-year E10, the median values of the absolute relative error were 13.5% for this study and 20.6% for Yin et al. (2019), indicating a smaller improvement in the mid-western and eastern regions compared to the improvement for the R-factor map (Fig. 5b). The relative errors of the 1-in-10-year E10 in this study were concentrated in the range of -10% to +10%, whereas those in Yin et al. (2019) were concentrated in the range of -25% to -15% and +15% to +25% (Fig. 5c). The western region was excluded in the evaluation of the 1-in-10-year E10 map because the record length of the 1 min data was too short to estimate 1-in-10-year event erosivity.

3.2 Erosivity maps and improvements over previous studies

The R-factor in China generally decreased from the south-eastern to the north-western region (Fig. 7a), ranging from 0 to 25 300 MJ mm ha\(^{-1}\) h\(^{-1}\) a\(^{-1}\). The map of 1-in-10-year E10 shows a similar spatial pattern as that of the R-factor (Fig. 7b), ranging from 0 to 11 246 MJ mm ha\(^{-1}\) h\(^{-1}\).

Zero R-factor value is found at Turpan, Xinjiang Uygur Autonomous Region, where the mean annual rainfall is only 7.8 mm. The maximum of the R-factor (more than 20 000 MJ mm ha\(^{-1}\) h\(^{-1}\) a\(^{-1}\)) is found in the southern part of the Guangxi and Guangdong provinces, along the South China Sea, where the mean annual rainfall is more than 2500 mm.

In addition to the overall trend, some local-scale characteristics could be identified. For the R-factor map, in the western region, the wetter region in north-western China was located in the west of Dzungaria Basin and along Tian Shan, which has been captured on the map. Some statistical characteristics of the new maps of the erosivity factors are shown in Table 3 based for soil erosion and hydrological zones in China (Fig. 8).

Comparing with the maps in Yin et al. (2019), the new maps can be quite different at some local areas (Fig. 9a and b). The R-factor in the new map was higher for most of the south-eastern region and lower for most of the middle and western regions, especially for the south-western area (Fig. 9a). However, the 1-in-10-year E10 map shows a similar pattern as that of R-factor, and the overestimation in Yin et al. (2019) seems to be more pronounced for some hilly regions in southeastern China (Fig. 9b).

3.3 Evaluation on the improvement of the erosivity maps

3.3.1 Effect of data temporal resolution

Figure 10 shows that the R-factor estimated from daily data (Eq. 6) is underestimated when the R value is higher than 10 000 MJ mm ha\(^{-1}\) h\(^{-1}\) a\(^{-1}\) and slightly overestimated when the value is lower than 2000 MJ mm ha\(^{-1}\) h\(^{-1}\) a\(^{-1}\). The model using hourly data improved the accuracy by about 11.1% (median value of the relative error) compared to that from daily data (Fig. 10). Estimated 1-in-10-year E10 would be underestimated using hourly and daily data, and the underestimation is greater if daily data were used (Fig. 10). Unlike the R-factor, the 1-in-10-year E10 was not noticeably improved with an increase in the temporal resolution from daily to hourly data, probably due to the fact that the 1-in-10-year E10 values estimated using daily data in Yin et al. (2019) had already been multiplied by a conversion factor of 1.17 to correct the 1-in-10-year daily erosivity to approximate the 1-in-10-year event E10 from 1 min data.
Figure 3. Framework of this study.

Figure 4. Comparison of the $R$-factors and 1-in-10-year $EI_{30}$ of the cross-validation values at the station of the maps and the values from 1 min data. The graphs on the left are the evaluation of the maps generated in this study, and those on the right are the evaluation of the maps generated by Yin et al. (2019).
3.3.2 Effect of the station density

Interpolation for the western (W) region had the lowest NSE value compared to other regions, which may be caused by the low station density (Fig. 1) and the lower spatial correlation of rainfall. The fitted semivariogram for the R-factor in the western region had a range of 35 km, whereas the ranges for mid-western (MW), north-eastern (NE) and south-eastern (SE) regions were 288, 261 and 1235 km, respectively.

A comparison of cross-validation between the two maps with different station densities shows that the interpolation with denser stations can improve the accuracy by 2.6%–15.4% for the R-factor based on the sMAPE index and by 1.4%–31.8% for 1-in-10-year EI$_{30}$ (Table 4) when the station density increased. The NSE can increase by 0.013 to 0.110 for the R-factor. For the 1-in-10-year EI$_{30}$, the NSE decreased by 0.001 to 0.096 for western (W), mid-western (MW) and south-eastern (SE) regions and increased by 0.038 for the north-eastern (NE) region.

For the R-factor, in the western (W) region, the station density doubled (increased from 36 600 to 21 200 km$^2$ per station), and the accuracy improved by 15.4%, whereas the sMAPE of 53.3% was still high with this increase in station density. In the mid-western (MW) region, the station density tripled (from 13 900 to 4800 km$^2$ 1 station) and the accuracy was improved by 11.1% based on the sMAPE index from 30.7% to 19.6%. In north-eastern (NE) and south-eastern (SE) regions, the station density tripled and quadrupled, respectively, and the accuracy increased about 2.5%. For 1-in-10-year EI$_{30}$, the improvement was 31.8% in the western (W) region and 19.6% in the mid-western (MW) region. The improvement was mainly in western regions, and the station density in the eastern China before the increase is enough to describe the spatial variation of the R-factor and the 1-in-10-year EI$_{30}$. It can be inferred that when there were less than about 10 000 km$^2$ per station, the increase of the site den-

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**Table 2.** The statistical characteristics of the absolute relative errors of the erosivity factors from the maps.

<table>
<thead>
<tr>
<th></th>
<th>MW, NE, SE</th>
<th>W</th>
<th>MW, NE, SE</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>This study</td>
<td>Yin et al. (2019)</td>
<td>This study</td>
</tr>
<tr>
<td>25th percentile</td>
<td>9.3 %</td>
<td>8.8 %</td>
<td>11.4 %</td>
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<tr>
<td>Median</td>
<td>17.8 %</td>
<td>18.1 %</td>
<td>16.2 %</td>
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<td>75th percentile</td>
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<td>34.4 %</td>
<td>45.9 %</td>
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<tr>
<td>Mean</td>
<td>21.0 %</td>
<td>24.7 %</td>
<td>28.7 %</td>
</tr>
</tbody>
</table>

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**Figure 5.** The relative errors of the R-factor (a for regions MW, NE, SE; b for region W) and 1-in-10-year EI$_{30}$ (c for regions ME, NE, SE) maps.
Figure 6. Spatial distribution of the absolute relative errors in the map of $R$-factor for 62 stations (a) and in the map of 1-in-10-year $EI_{30}$ for 18 stations (b) with 1 min observation data.

Table 3. Statistical characteristics of $R$-factor and 1-in-10-year $EI_{30}$ in soil erosion and hydrological zonings.

<table>
<thead>
<tr>
<th>Parameters</th>
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<td>1564</td>
<td>2604</td>
<td>3320</td>
<td>4698</td>
<td>7512</td>
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</table>

* The zonings are shown in Fig. 8.

... has little impact on the improvement of the interpolation (Fig. 11).

3.3.3 Effect of the interpolation method

For the $R$-factor, cross-validation of ordinary kriging and universal kriging with the mean annual rainfall as the co-variable (Table 5) shows that universal kriging improved the interpolation accuracy by 2.3%–9.0% (sMAPE) compared to ordinary kriging. In the western (W) region, the NSE increased from 0.285 (ordinary kriging) to 0.599 (universal kriging). Therefore, it is better to use universal kriging instead of ordinary kriging when generating the $R$-factor map.
especially in western China where the station density is low. For the 1-in-10-year EI$_{30}$, universal kriging improved the accuracy by 0.4%–9.7% (sMAPE). In the western (W) region, the accuracy improved by 9.7 % and the NSE increased from 0.094 (ordinary kriging) to 0.293 (universal kriging).

4 Discussion

This study has produced quality $R$-factor and 1-in-10-year EI$_{30}$ maps with hourly data from 2381 stations over mainland China, which are shown to be a noticeable improvement over the maps that are currently available for China (Yin et al., 2019; Table 1). The improvement of the $R$-factor map over previously published $R$-factor maps can be attributed to...
the increase in the temporal resolution from daily to hourly data, whereas that of 1-in-10-year EI$_{30}$ map to the increase of the station density in comparison with those of Yin et al. (2019). There are mainly two reasons for this. First, 1-in-10-year event EI$_{30}$ values estimated from the daily data had already been adjusted to those from the 1 min data by multiplying a conversion factor of 1.17 (Yin et al., 2019), which resulted in no obvious improvement from the daily data to the hourly data. Second, the 1-in-10-year event EI$_{30}$ associated with extreme rainfall event intrinsically has a high spatial variability in comparison to the R-factor as shown in Table 4. The accuracy of spatially interpolated rainfall erosivity was more sensitive to the station density when the station density is low. Hence the improvement of the map of the 1-in-10-year EI$_{30}$ was mainly a result of the increase of the station density, especially for the western (W) and the mid-western (MW) regions with a low station density.

Comparison with a world map of rainfall erosivity was also undertaken for mainland China. Panagos et al. (2017) produced the Global Rainfall Erosivity Database with hourly and sub-hourly rainfall data from 3625 stations from 63 countries. This database could be used for comparison of rainfall erosivity among different regions in the world. In their study, hourly data from 387 stations in China were used. Figure 12 shows that the R-factor for China extracted from Panagos et al. (2017) is systematically underestimated by about 30 % for most areas in China, whereas it is overestimated in the Tibetan Plateau (cf. Fig. 7a). The reason for the underestimation may be that the R-factor calculated from hourly data applied a conversion factor (CF$_{30}$) that was developed from the R-factor values computed with 60 min data to those with 30 min data in Panagos et al. (2015b), rather than using an adjustment factor based on breakpoint data (CF$_{bp}$) or 1 min data (CF$_{1}$). Breakpoint data were used for the USLE (Wischmeier and Smith, 1965, 1978), RUSLE (Renard et al., 1997) and 1 min data for this study. Previous research has shown the difference between CF$_{30}$ and CF$_{bp}$ (CF$_{1}$) can result in an underestimation of R-factor by about 20 % (Auerswald et al., 2015; Yue et al., 2020a). Table 6 shows that the relative error of the map from Panagos et al. (2017) could reduce by about 6.2 % after multiplying by a conversion factor of 1.253, which was calibrated by Yue et al. (2019).
et al. (2020a) for converting the $R$-factor from 30 min data to 1 min data. Because the cross-validation values from the map of Panagos et al. (2017) were not available, values extracted from the maps were used instead to compare with the values from 1 min data at the 62 stations. Erosivity values based on the adjusted maps are still generally underestimated. The reason could be that the equation for estimating the storm energy ($E$) from rainfall intensity used in Panagos et al. (2017) was from the RUSLE (Renard et al., 1997), and the equation is known to cause underestimation of the storm energy up to 10% in previous studies (McGregor et al., 1995; Yin et al., 2017). Because of this, the equation for estimating the storm energy ($E$) in RUSLE (Renard et al., 1997) was then modified in RUSLE2 (USDA-ARS, 2013), which was adopted in this study.

Figure 9. Differences of the $R$-factor (a) and the 1-in-10-year $EI_{30}$ (b) comparing with the previous study.
The $R$-factor in the Tibetan Plateau varies from 0 to 12 326 MJ mm$^{-1}$ h$^{-1}$ a$^{-1}$ in Panagos et al. (2017) and from 5 to 4442 MJ mm$^{-1}$ h$^{-1}$ a$^{-1}$ in this study. The former was derived from a Gaussian process regression (GPR) model and a number of monthly climate variables from the WorldClim database, such as the mean monthly precipitation, mean minimum, and average and maximum monthly temperature. The GPR model was calibrated using the site-specific $R$-factor values and these climate variables, which may not applicable for sites at high altitude, as none of the observation sites was located in the Tibetan Plateau region. The GPR model might be the main reason for the overestimation of the $R$-factor in the Tibetan Plateau where the $R$-factor was expected to be underestimated just like any other regions.

Although this study provides improved erosivity maps in comparison with previous studies, errors remain inevitably. The uncertainty of the estimated $R$-factor and 1-in-10-year erosivity values from this study mainly comes from the following sources: first, the KE–I model for estimating kinetic

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**Table 5.** Cross-validation of the interpolated $R$-factor and 1-in-10-year event $E_{10}$ using ordinary kriging and universal kriging.

<table>
<thead>
<tr>
<th>Region</th>
<th>Interpolation method</th>
<th>$R$-factor sMAPE</th>
<th>$R$-factor NSE</th>
<th>1-in-10-year $E_{10}$ sMAPE</th>
<th>1-in-10-year $E_{10}$ NSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>W</td>
<td>Ordinary kriging</td>
<td>62.3% 0.285</td>
<td>41.5% 0.094</td>
<td>53.3% 0.599</td>
<td>31.8% 0.293</td>
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<td>Universal kriging</td>
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<td></td>
<td></td>
<td></td>
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<tr>
<td>MW</td>
<td>Ordinary kriging</td>
<td>24.8% 0.861</td>
<td>24.9% 0.838</td>
<td>19.6% 0.951</td>
<td>24.5% 0.886</td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NE</td>
<td>Ordinary kriging</td>
<td>12.0% 0.926</td>
<td>16.5% 0.865</td>
<td>9.7% 0.962</td>
<td>14.9% 0.895</td>
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<tr>
<td></td>
<td>Universal kriging</td>
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<td></td>
</tr>
<tr>
<td>SE</td>
<td>Ordinary kriging</td>
<td>11.2% 0.911</td>
<td>14.8% 0.844</td>
<td>8.3% 0.959</td>
<td>14.0% 0.824</td>
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<tr>
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<td>Universal kriging</td>
<td></td>
<td></td>
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</table>
Table 6. Comparison of the statistical characteristics of the relative errors of the R-factor extracted from the map generated in this study and extracted from Panagos et al. (2017) (original and adjusted). The adjusted map of Panagos et al. (2017) was the original map multiplying by a conversion factor of 1.253, which was calibrated by Yue et al. (2020a) for converting the R-factor from 30 min data to 1 min data.

<table>
<thead>
<tr>
<th></th>
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<th>Panagos et al. (2017) adjusted</th>
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<td>25th percentile</td>
<td>7.1 %</td>
<td>14.8 %</td>
<td>10.4 %</td>
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<tr>
<td>Median</td>
<td>16.1 %</td>
<td>28.3 %</td>
<td>22.1 %</td>
</tr>
<tr>
<td>75th percentile</td>
<td>28.0 %</td>
<td>40.5 %</td>
<td>43.2 %</td>
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<tr>
<td>Mean</td>
<td>20.1 %</td>
<td>33.8 %</td>
<td>33.1 %</td>
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</table>

Figure 11. Improvement of the interpolation with the increase of station density. Data were from the 774 and 2381 stations in the 4 different regions.

5 Data availability

The rainfall erosivity maps (R-factor and 1-in-10-year EI30) are available at: https://doi.org/10.12275/bnu.clicia.rainfallerosivity.CN.001 (Yue et al., 2020b).

6 Conclusions

This study has generated new R-factor and 1-in-10-year EI30 maps using hourly and daily rainfall data for the period from 1951 to 2018 from 2381 stations over mainland China. The improvement in the accuracy of these erosivity maps over what are currently available was evaluated in terms of the median absolute relative error and was explained in terms of temporal resolution of data used, station density, and interpolation methods. The following conclusions can be drawn from this study:

1. Comparing with the existing maps for the 62 reference sites, the median absolute relative error in the R-factor map generated in this study was reduced from 18.1 % to 17.8 % for the mid-western and eastern regions, from 161.6 % to 16.2 % for the western region, and for the 1-in-10-year EI30, and from 20.6 % to 13.5 % in the mid-western and eastern regions.

2. The R-factor value varied from 0 to 25 300 MJ mm ha⁻¹ h⁻¹ a⁻¹, and the 1-in-10-year EI30 value was from 0 to 11 246 MJ mm ha⁻¹ h⁻¹. In comparison with the existing maps, new maps of the R-factor and 1-in-10-year event EI30 show a clear decreasing trend from south-eastern to north-eastern China.

3. Improvement in the R-factor map can be mainly attributed to an increase in the temporal resolution from daily to hourly, whereas that in the 1-in-10-year EI30 map to an increase of the station density. The increased station density has led to an improved R-factor and 1-in-10-year EI30 maps for the western regions primarily. The benefit from an increased station density is limited once the station density reached about 1 station per 10 000 km². As for the interpolation method, universal kriging with the mean annual rainfall as the co-variable

Figure 12. R-factor map of the study area extracted from Panagos et al. (2017) and the evaluation of the map based on 62 stations with 1 min data.

performed better than ordinary kriging for all regions, especially for the western regions with sparse weather stations.

Author contributions. TY did the formal analysis, visualization, and original draft writing. SY did the methodology, formal analysis, review, and editing. YX, BY, and BL did the review and editing.

Competing interests. The contact author has declared that neither they nor their co-authors have any competing interests.

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